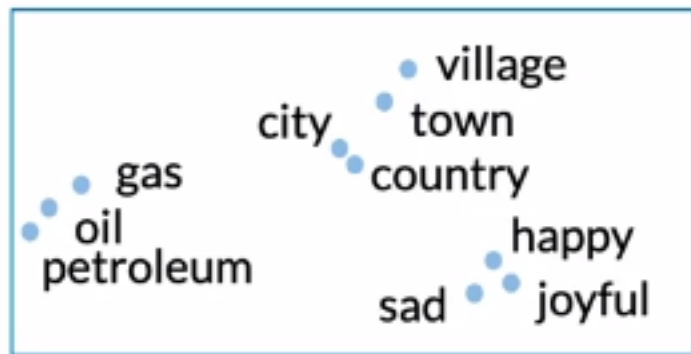


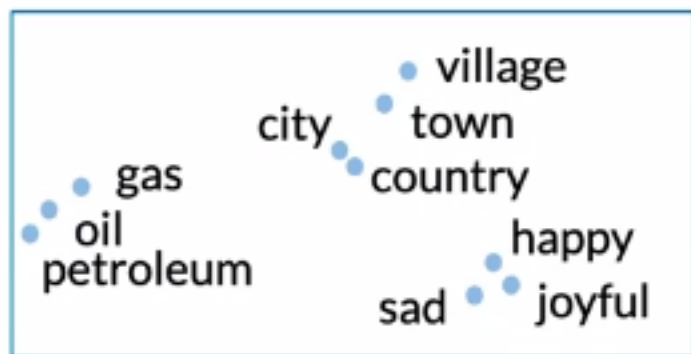
# Some basic applications of word embeddings

# Some basic applications of word embeddings



Semantic analogies  
and similarity

# Some basic applications of word embeddings



Semantic analogies  
and similarity



Sentiment analysis

# Some basic applications of word embeddings



Semantic analogies  
and similarity



Sentiment analysis



Classification of  
customer feedback



# Advanced applications of word embeddings



Machine translation

# Advanced applications of word embeddings



Machine translation



Information extraction

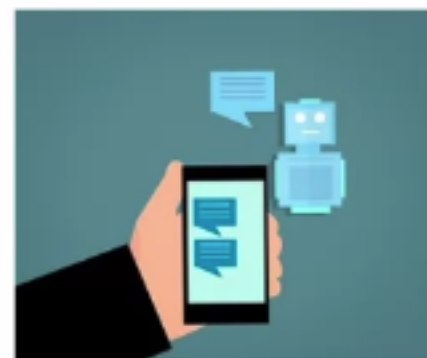
# Advanced applications of word embeddings



Machine translation



Information extraction



Question answering

# Learning objectives

- Identify the key concepts of word representations

# Learning objectives

- Identify the key concepts of word representations
- Generate word embeddings

# Learning objectives

- Identify the key concepts of word representations
- Generate word embeddings
- Prepare text for machine learning

# Learning objectives

- Identify the key concepts of word representations
- Generate word embeddings
- Prepare text for machine learning
- Implement the continuous bag-of-words model

# Learning objectives

Prerequisite: neural networks

- Identify the key concepts of word representations
- Generate word embeddings
- Prepare text for machine learning
- Implement the continuous bag-of-words model



# Integers

Word	Number
a	1
able	2
about	3
...	...
hand	615
...	...
happy	621
...	...
zebra	1000

# Integers

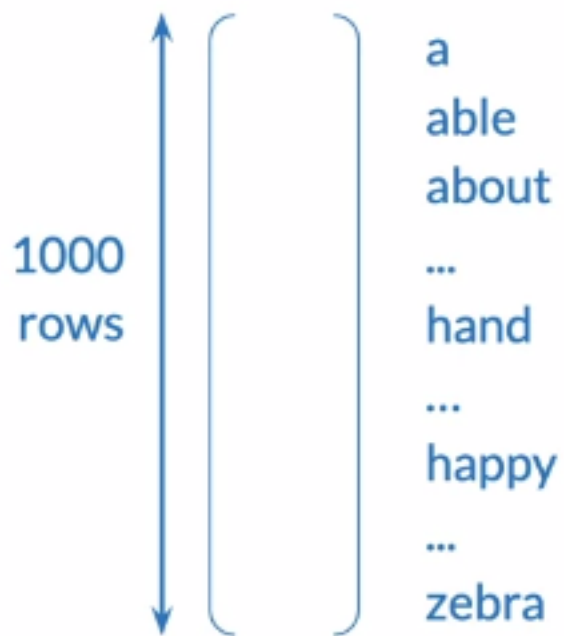
- + Simple
- Ordering: little semantic sense

# Integers

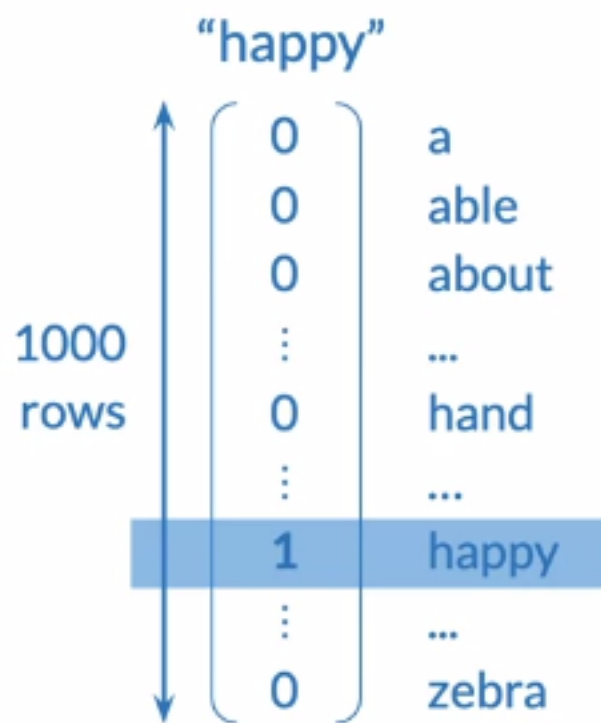
- + Simple
- Ordering: little semantic sense

hand < happy < zebra  
615 621 1000  
?! ?!

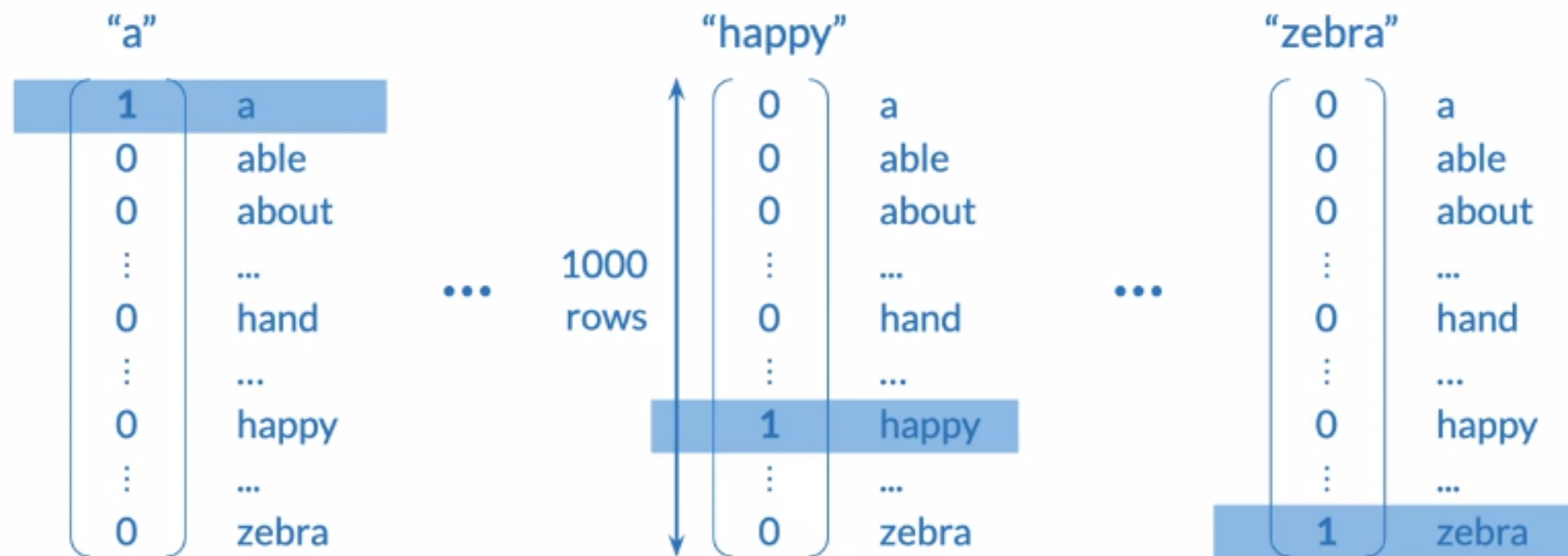
# One-hot vectors



# One-hot vectors



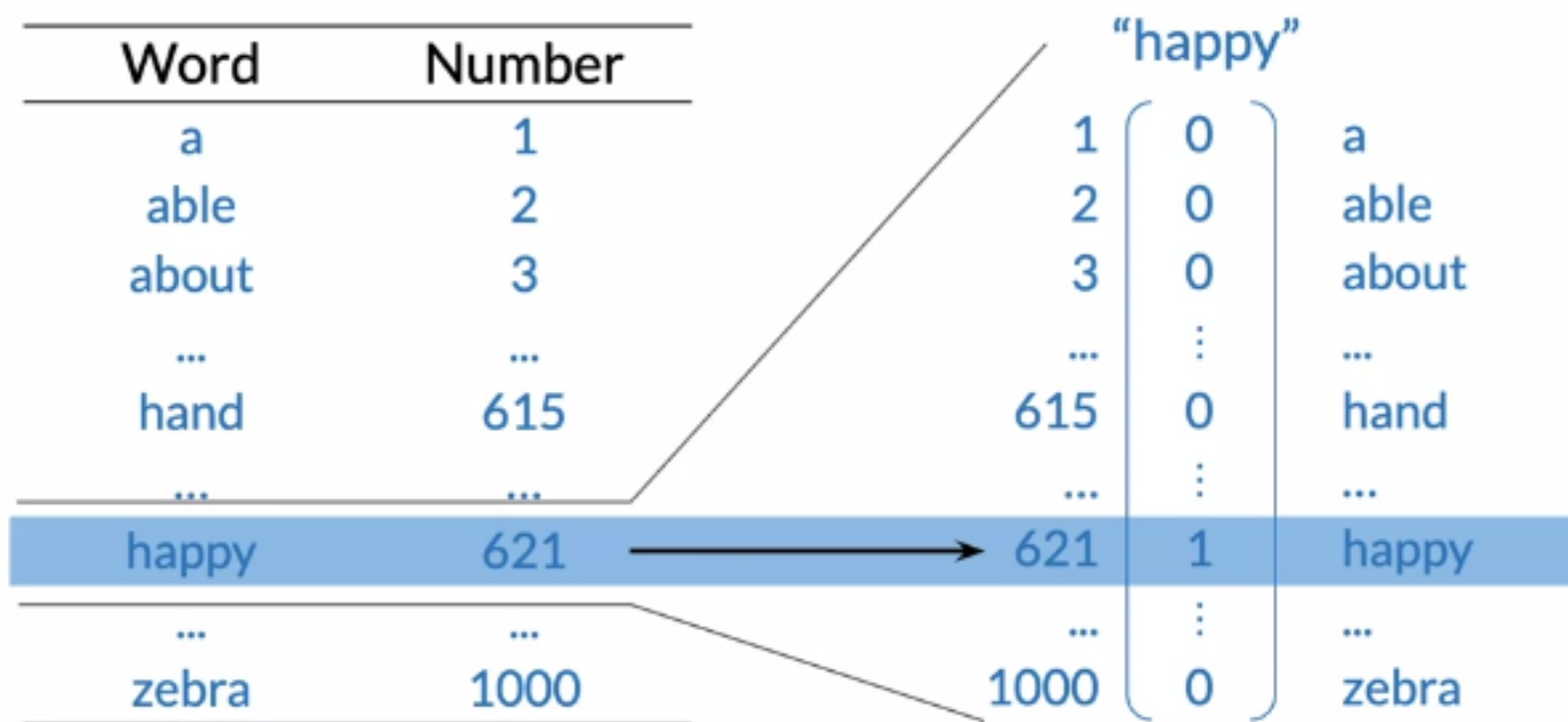
# One-hot vectors



# One-hot vectors

Word	Number		"happy"		
a	1		1	0	a
able	2		2	0	able
about	3		3	0	about
...	...		...	⋮	...
hand	615		615	0	hand
...	...		...	⋮	...
happy	621		621	1	happy
...	...		...	⋮	...
zebra	1000		1000	0	zebra

# One-hot vectors





# One-hot vectors

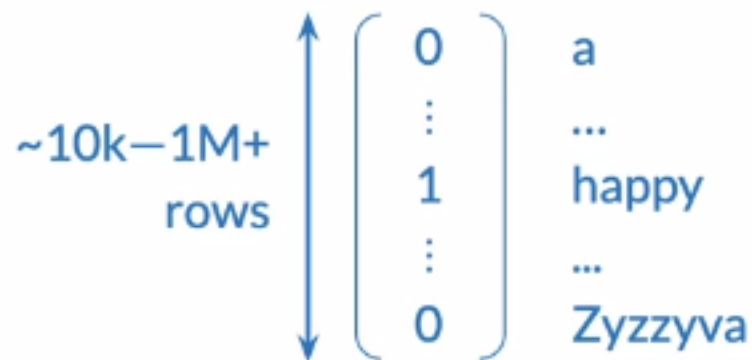
- + Simple
- + No implied ordering

# One-hot vectors

- + Simple
- + No implied ordering
- Huge vectors

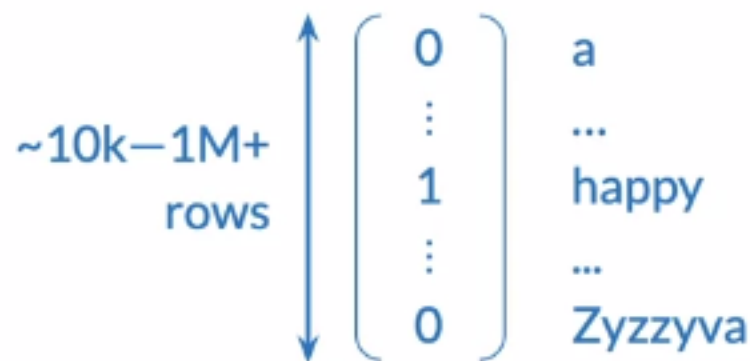
# One-hot vectors

- + Simple
- + No implied ordering
- Huge vectors



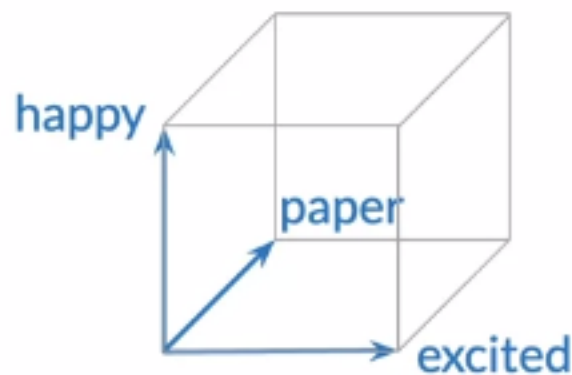
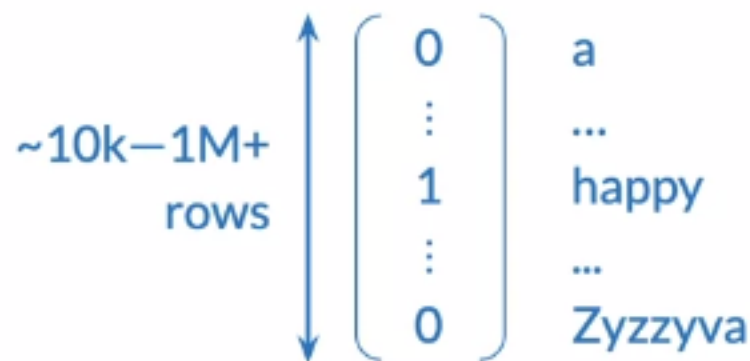
# One-hot vectors

- + Simple
- + No implied ordering
- Huge vectors
- No embedded meaning



# One-hot vectors

- + Simple
- + No implied ordering
- Huge vectors
- No embedded meaning



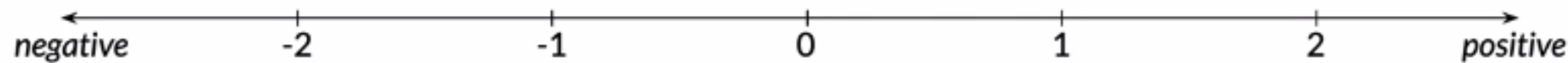
$$\begin{aligned} d(\text{paper}, \text{excited}) \\ &= d(\text{paper}, \text{happy}) \\ &= d(\text{excited}, \text{happy}) \end{aligned}$$



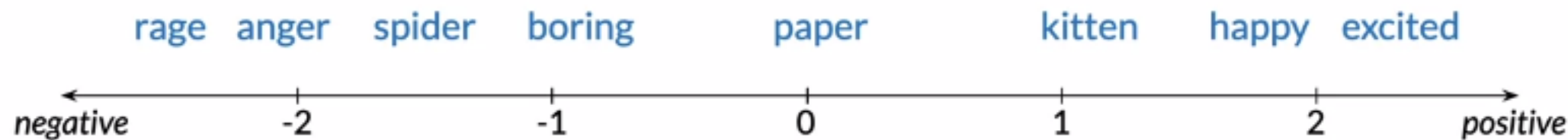
deeplearning.ai

# Word Embeddings

# Meaning as vectors

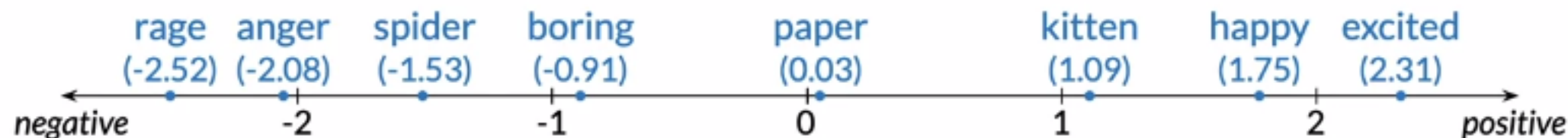


# Meaning as vectors

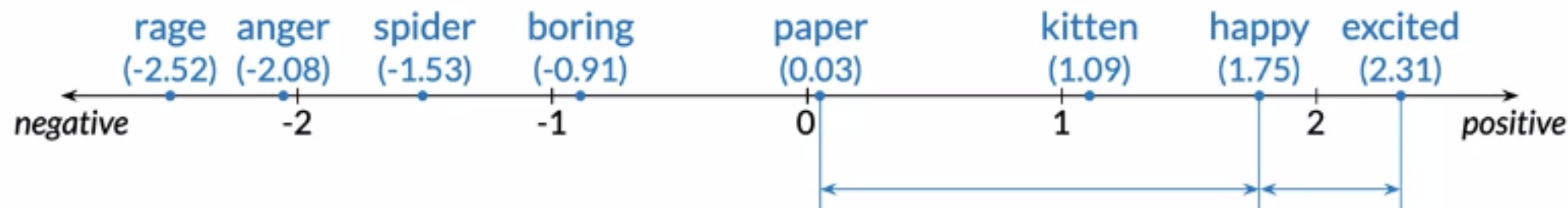




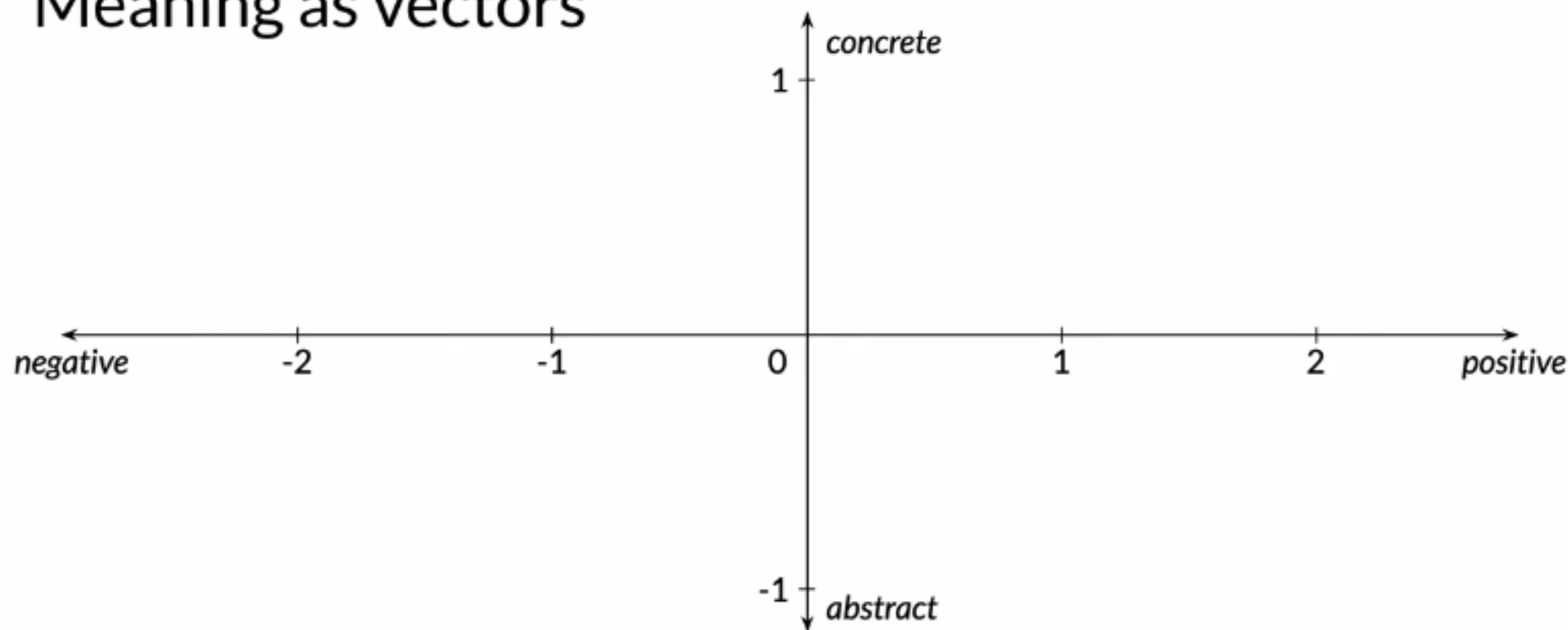
# Meaning as vectors



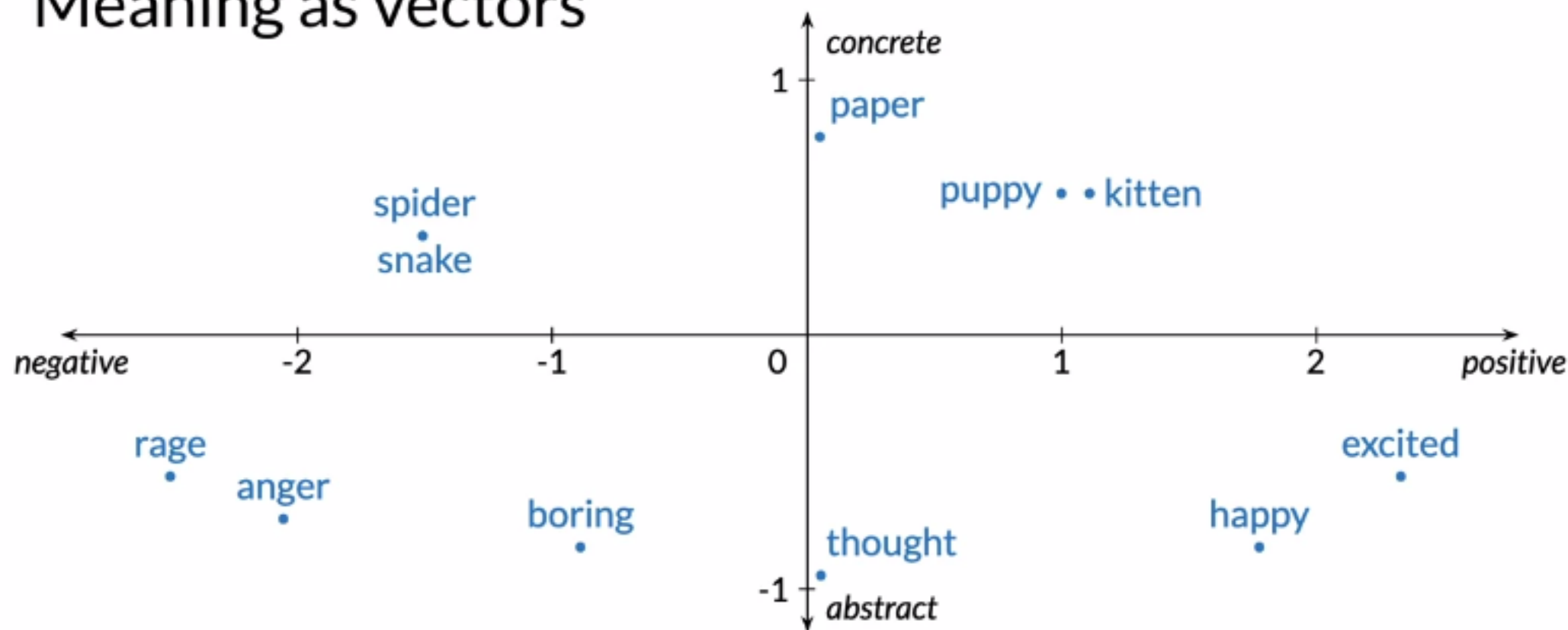
# Meaning as vectors



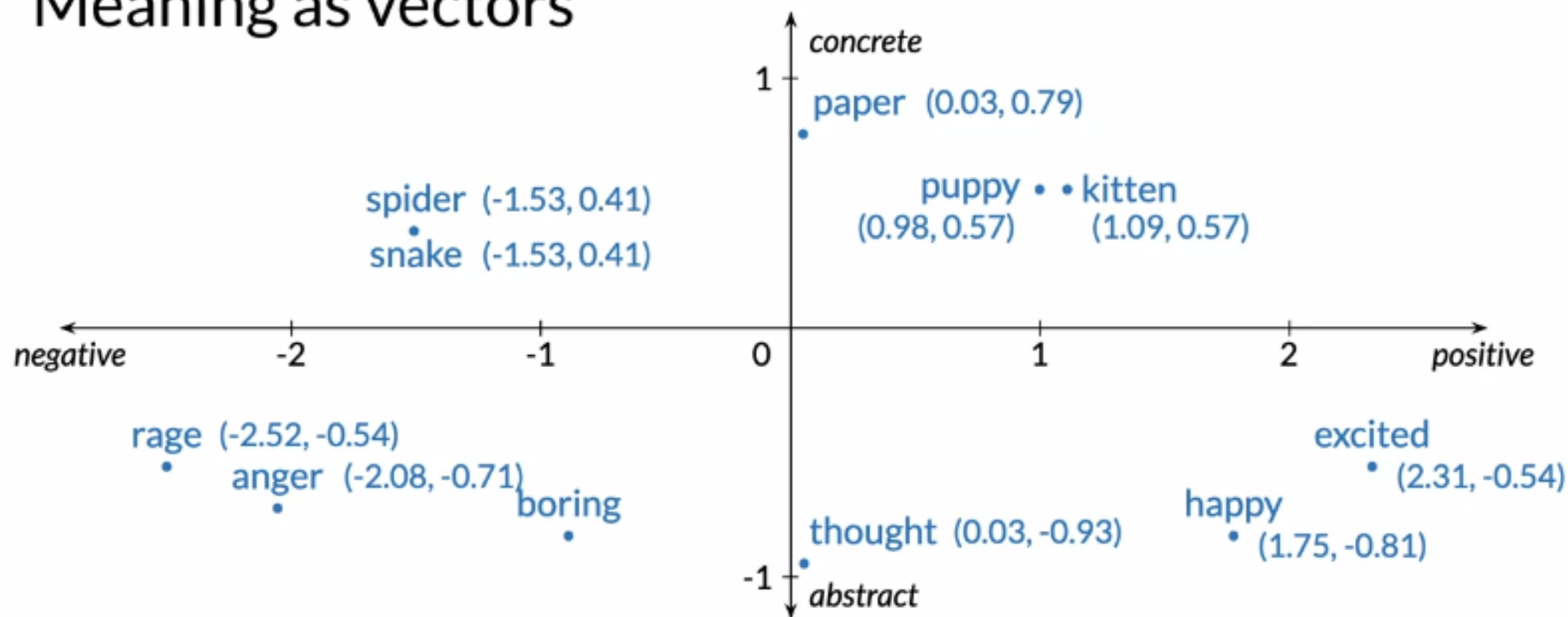
# Meaning as vectors



# Meaning as vectors



# Meaning as vectors



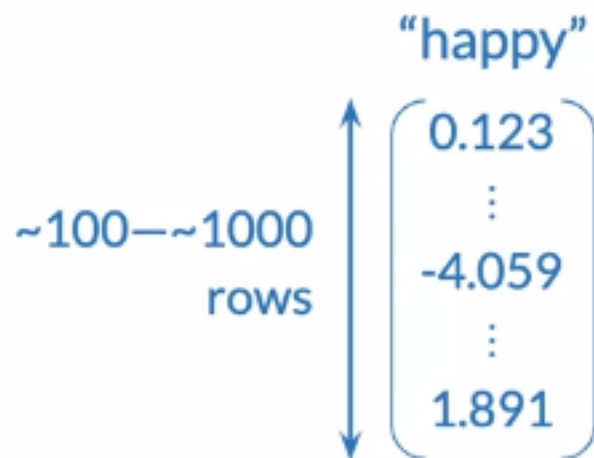
# Word embedding vectors

# Word embedding vectors

- + Low dimension

# Word embedding vectors

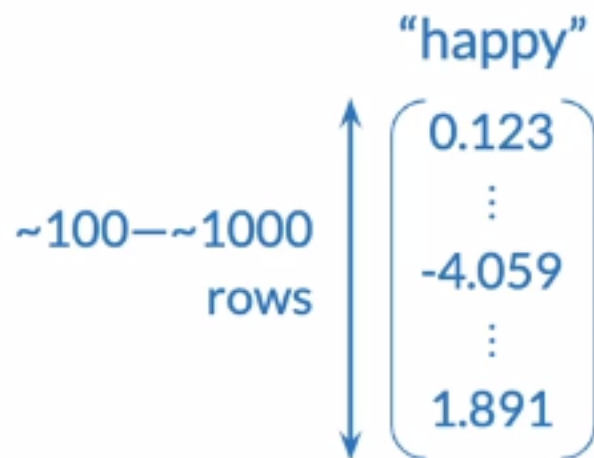
+ Low dimension





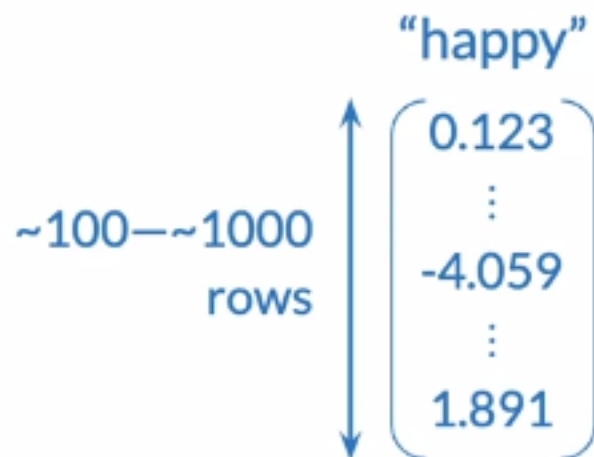
# Word embedding vectors

- + Low dimension
- + Embed meaning



# Word embedding vectors

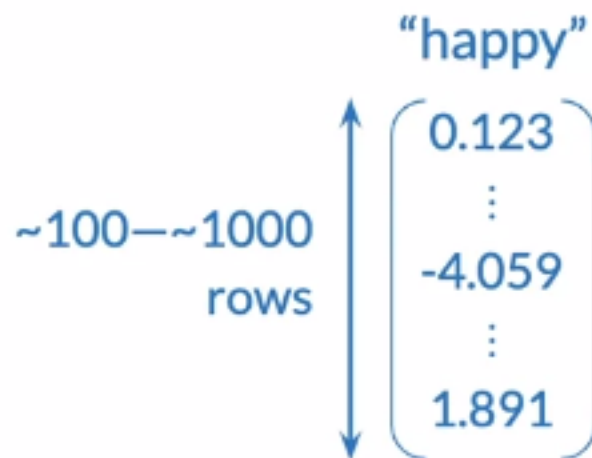
- + Low dimension
- + Embed meaning
  - e.g. semantic distance



# Word embedding vectors

- + Low dimension
- + Embed meaning
  - e.g. semantic distance

forest  $\approx$  tree      forest  $\neq$  ticket

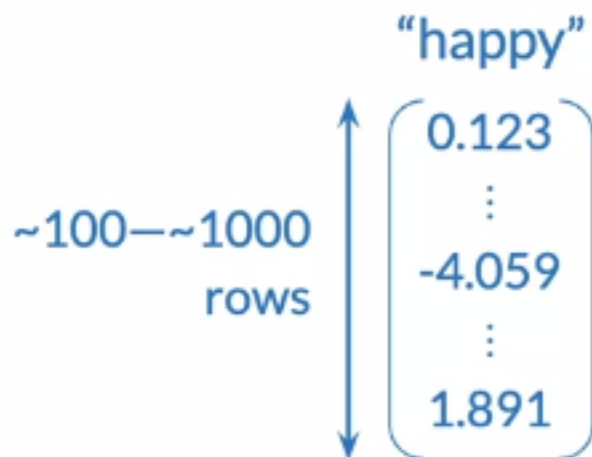


# Word embedding vectors

- + Low dimension
- + Embed meaning
  - e.g. semantic distance

forest  $\approx$  tree      forest  $\neq$  ticket

- e.g. analogies



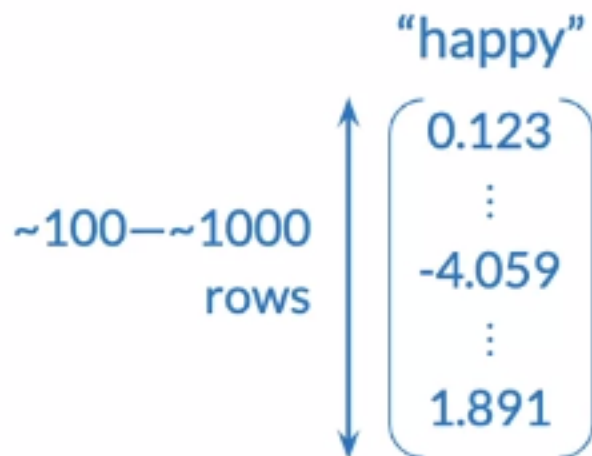
# Word embedding vectors

- + Low dimension
- + Embed meaning
  - e.g. semantic distance

forest  $\approx$  tree      forest  $\neq$  ticket

- e.g. analogies

Paris:France :: Rome:?



# Terminology

integers

one-hot vectors

word embedding vectors

# Terminology

integers

**word vectors**

one-hot vectors

word embedding vectors

# Terminology

integers

**word vectors**

one-hot vectors

word embedding vectors

“word vectors”

word embeddings



# Summary

- Words as integers
- Words as vectors
  - One-hot vectors
  - Word embedding vectors
- Benefits of word embeddings for NLP

# Word embedding process

**Corpus**

**Embedding method**

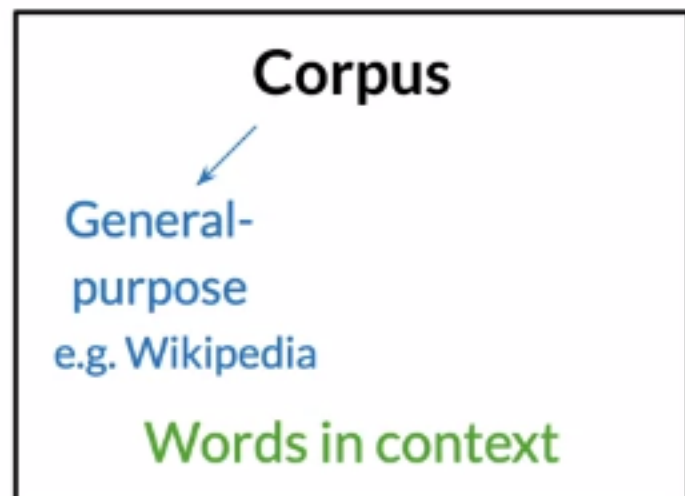
# Word embedding process

**Corpus**

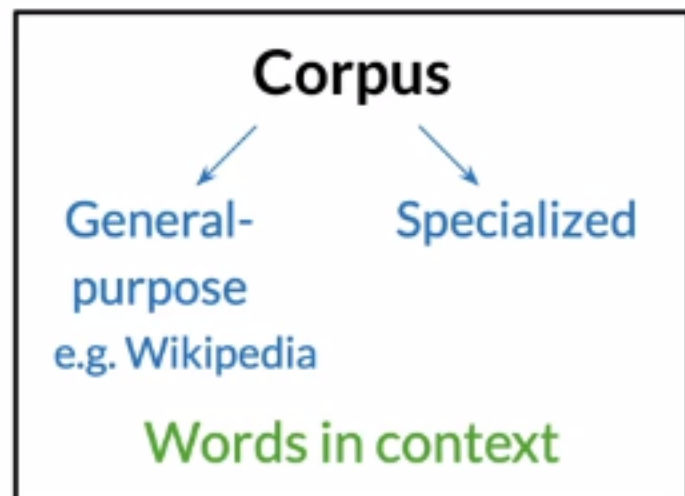
Words in context

**Embedding method**

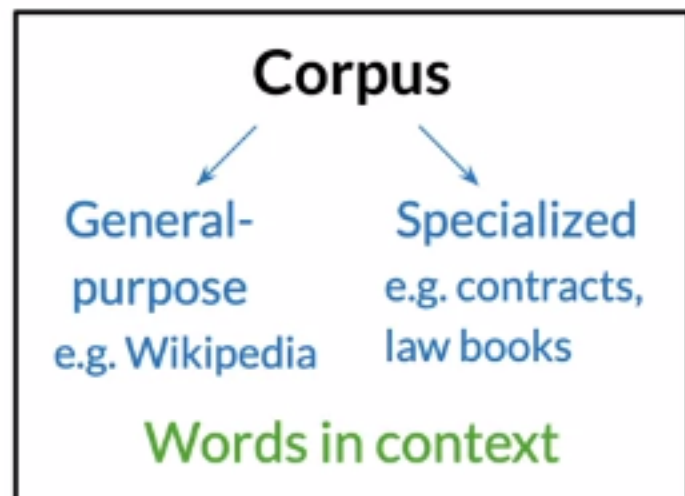
# Word embedding process



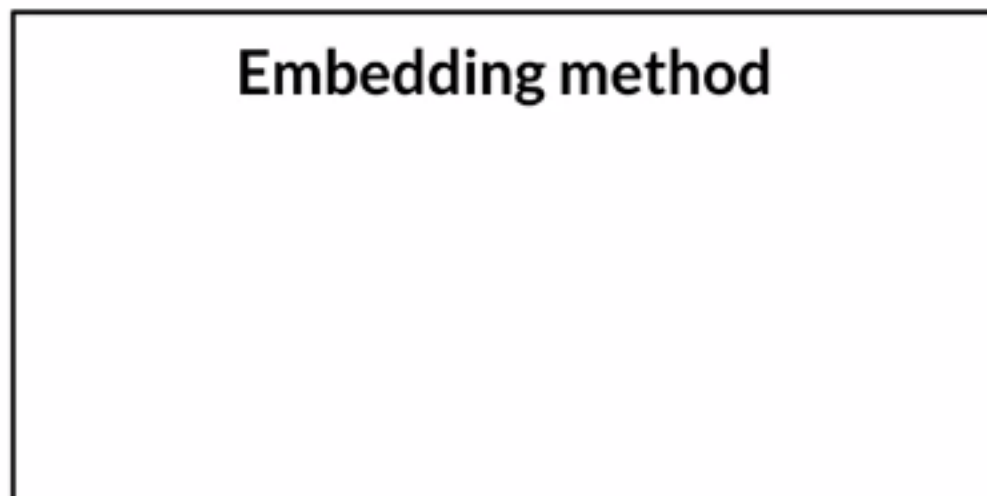
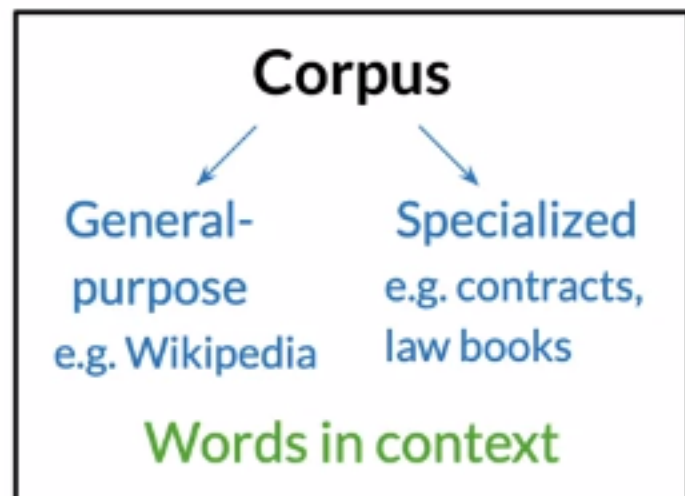
# Word embedding process



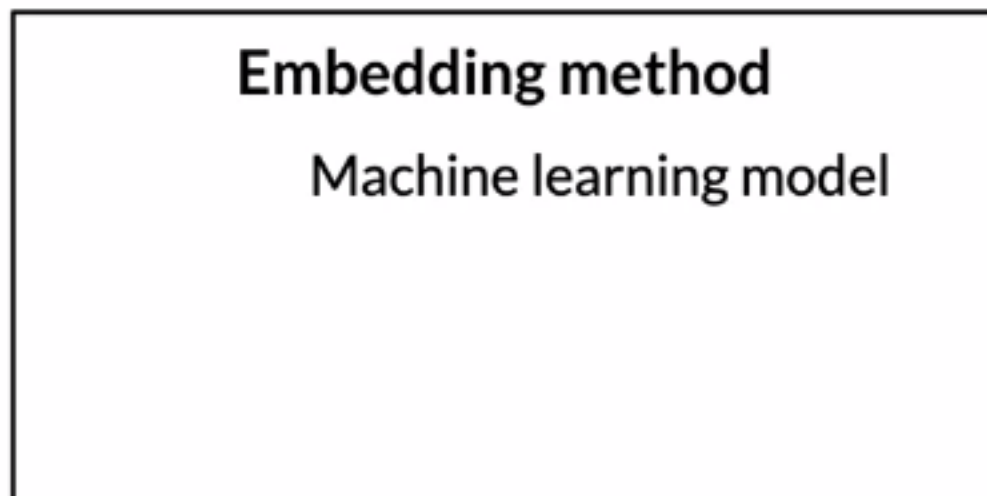
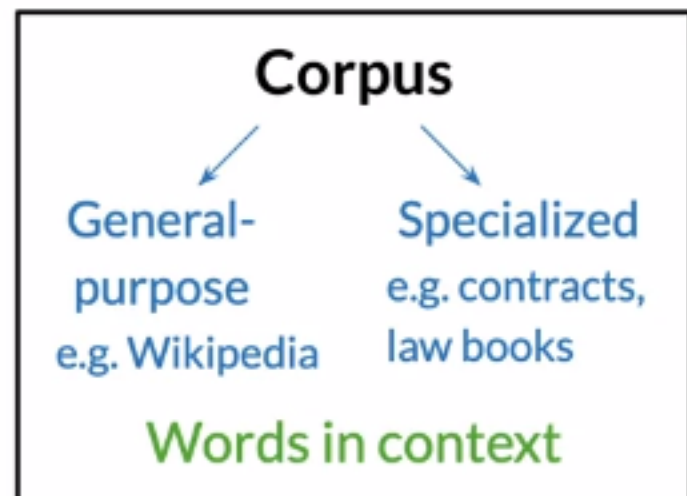
# Word embedding process



# Word embedding process

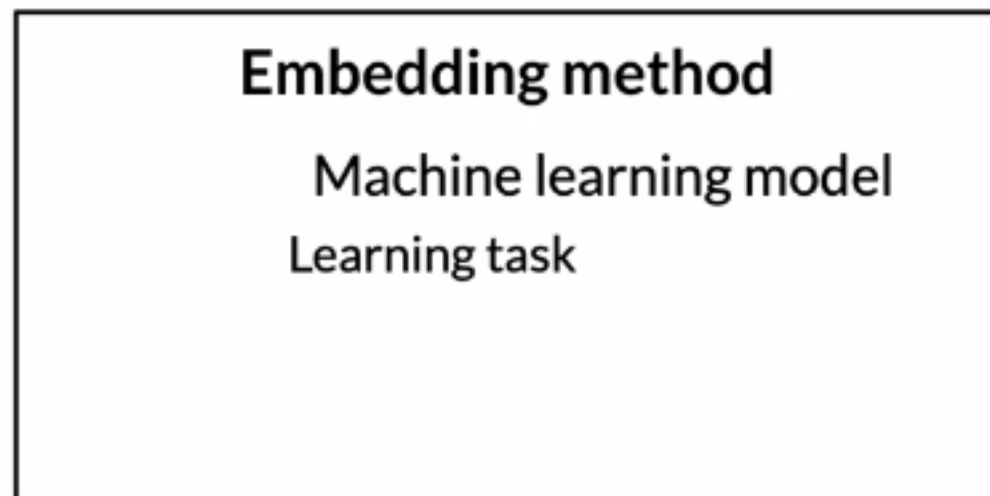
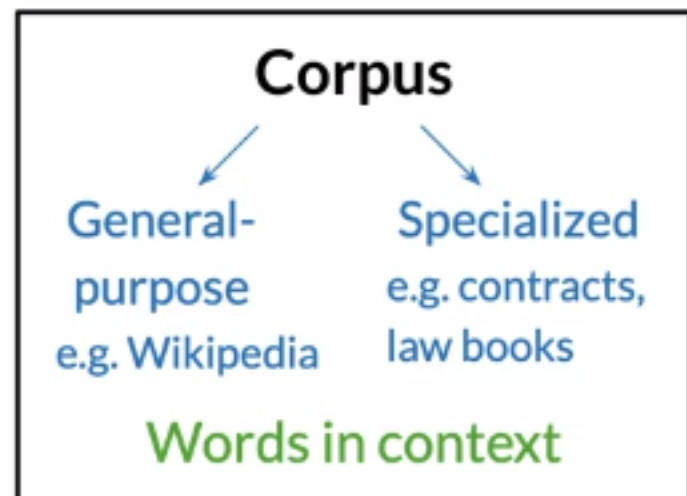


# Word embedding process



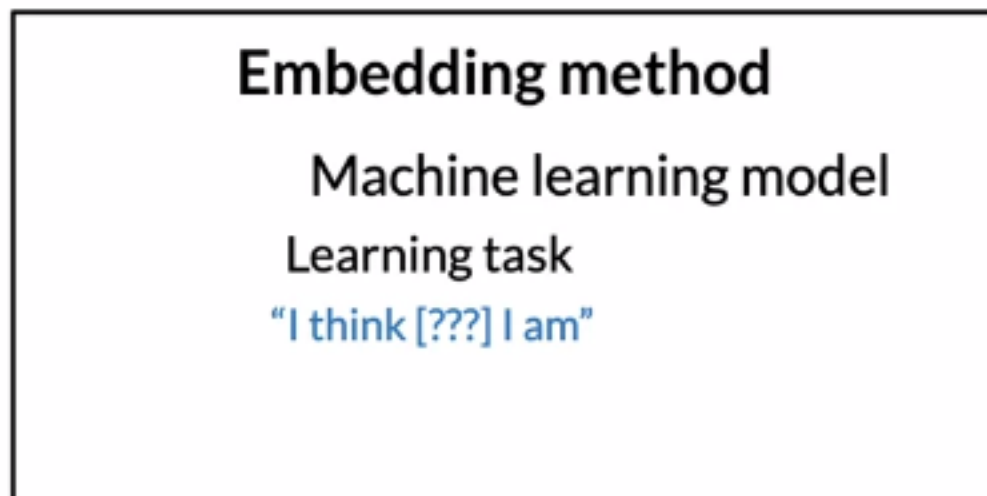
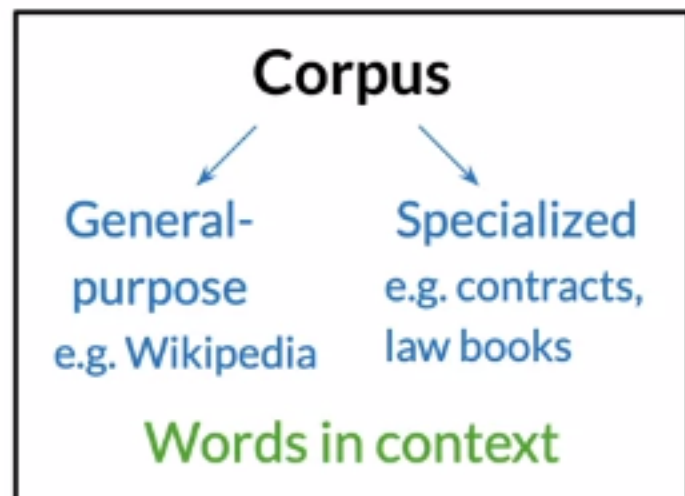


# Word embedding process



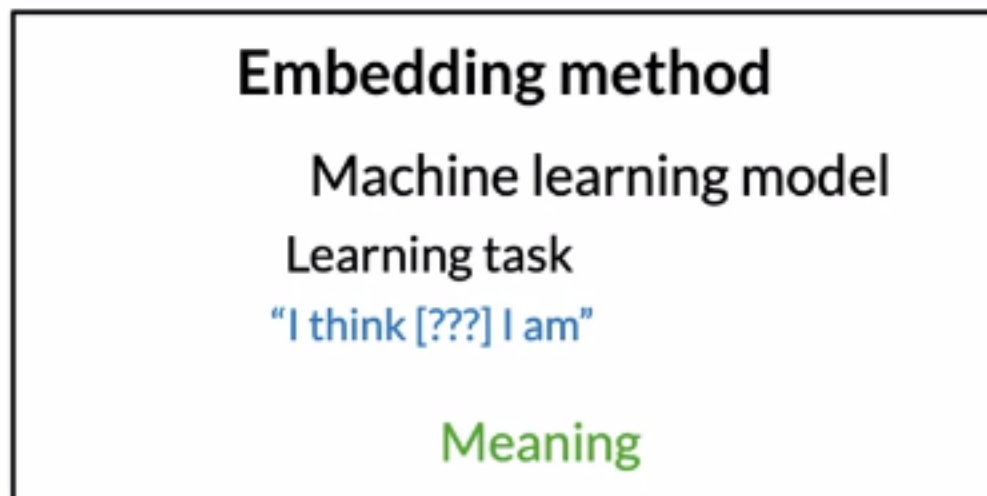
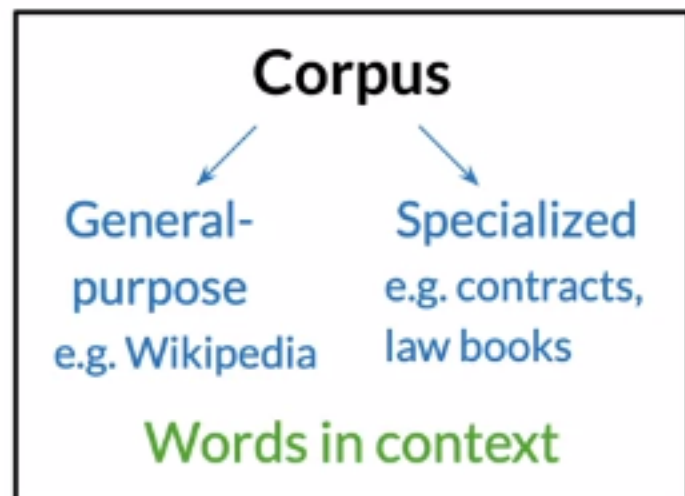
**Word embeddings**

# Word embedding process



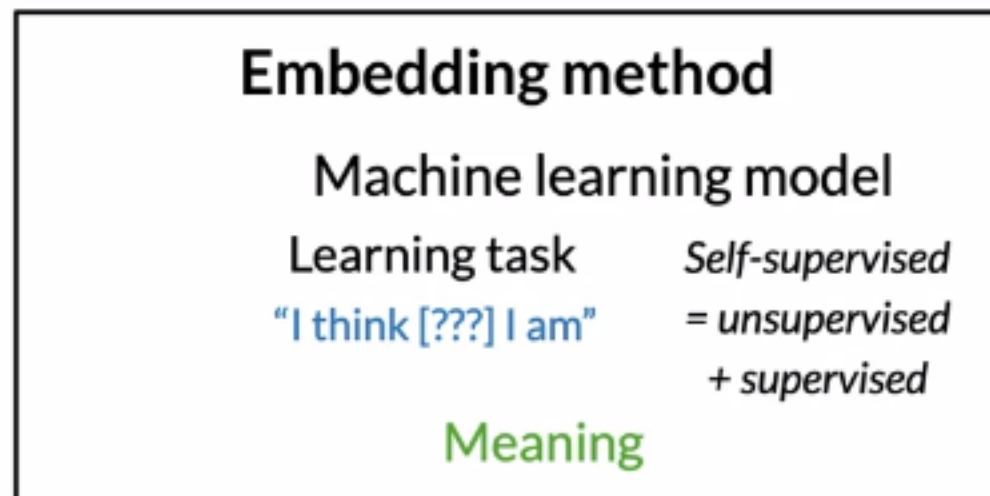
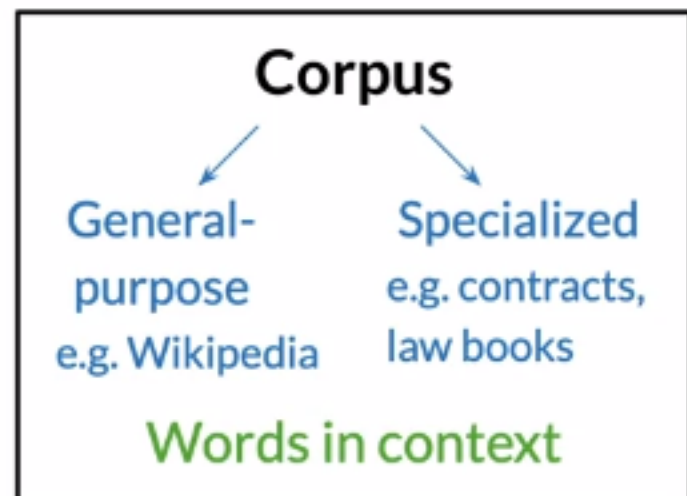
**Word embeddings**

# Word embedding process



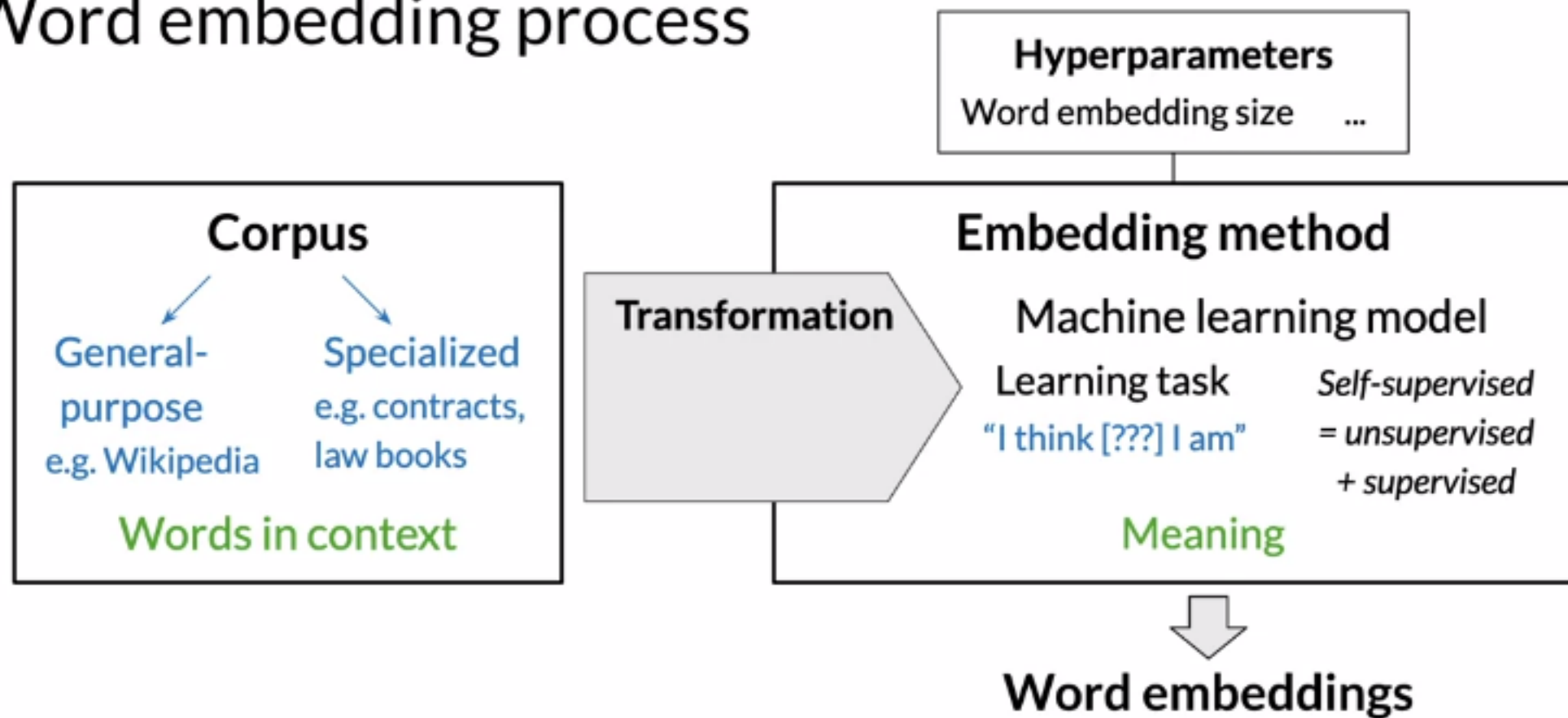
**Word embeddings**

# Word embedding process

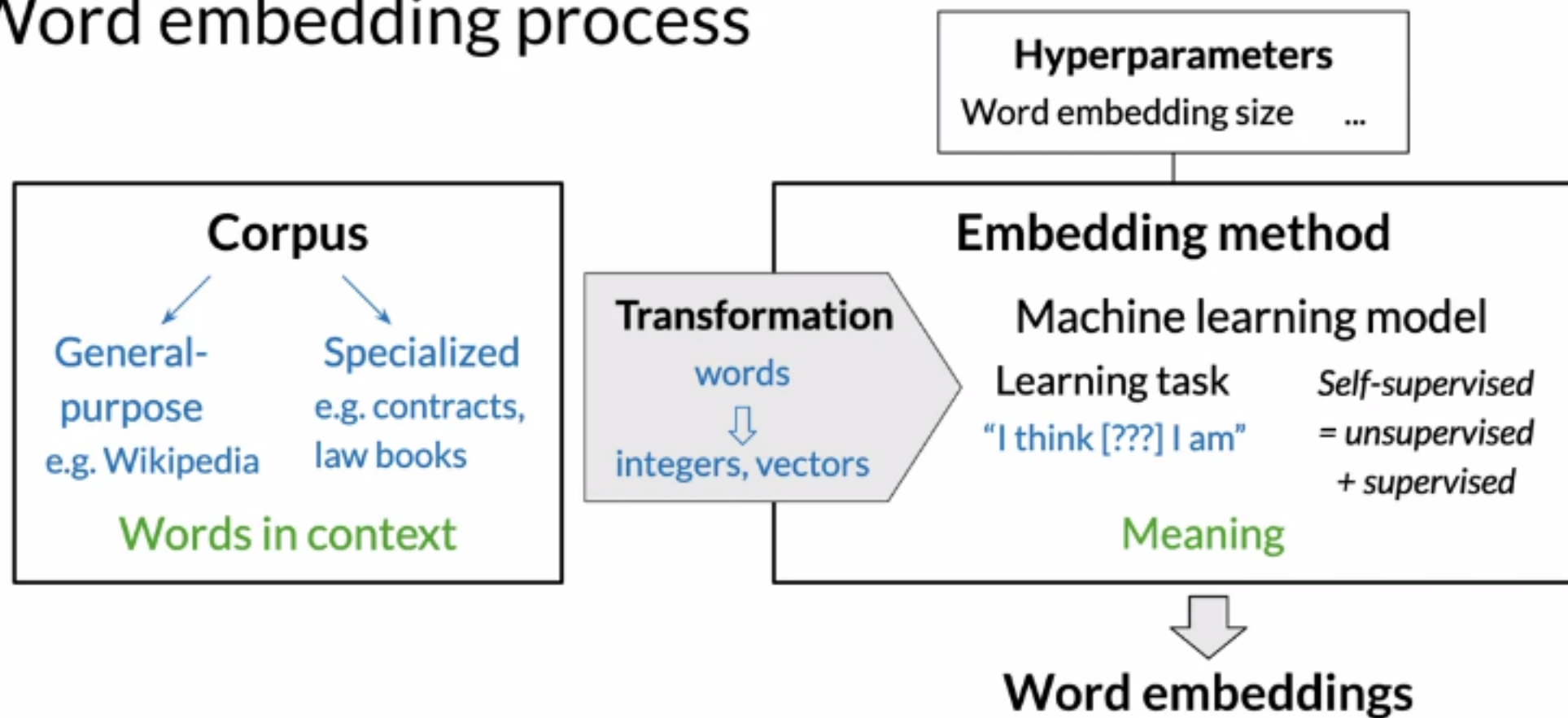


**Word embeddings**

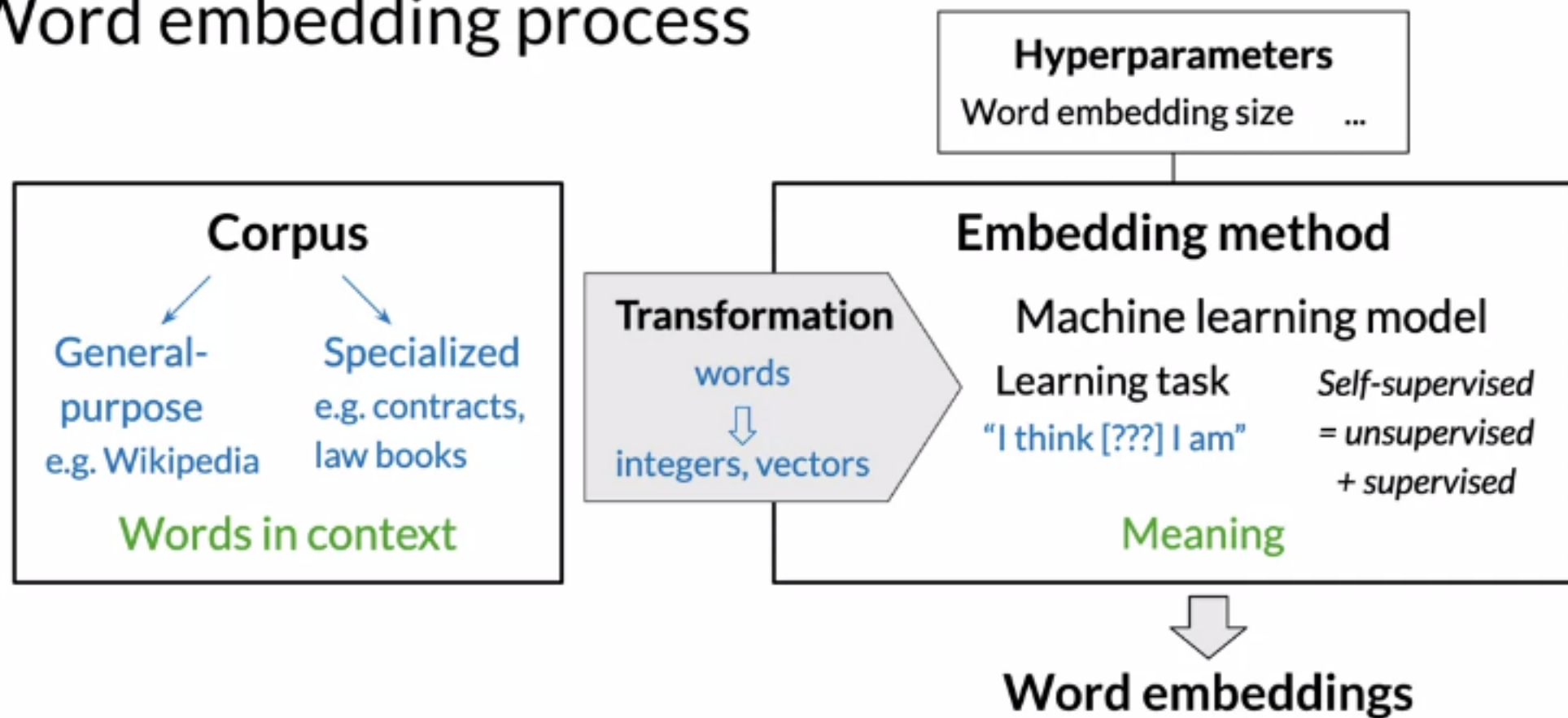
# Word embedding process



# Word embedding process



# Word embedding process





deeplearning.ai

# Word Embedding Methods

---



# Basic word embedding methods

- word2vec (Google, 2013)
  - Continuous bag-of-words (CBOW)

# Basic word embedding methods

- word2vec (Google, 2013)
  - Continuous bag-of-words (CBOW)
  - Continuous skip-gram / Skip-gram with negative sampling (SGNS)

# Basic word embedding methods

- word2vec (Google, 2013)
  - Continuous bag-of-words (CBOW)
  - Continuous skip-gram / Skip-gram with negative sampling (SGNS)
- Global Vectors (GloVe) (Stanford, 2014)

# Basic word embedding methods

- word2vec (Google, 2013)
  - Continuous bag-of-words (CBOW)
  - Continuous skip-gram / Skip-gram with negative sampling (SGNS)
- Global Vectors (GloVe) (Stanford, 2014)
- fastText (Facebook, 2016)
  - Supports out-of-vocabulary (OOV) words

# Advanced word embedding methods

Deep learning, contextual embeddings

# Advanced word embedding methods

Deep learning, contextual embeddings

- BERT (Google, 2018)

# Advanced word embedding methods

Deep learning, contextual embeddings

- BERT (Google, 2018)
- ELMo (Allen Institute for AI, 2018)

# Advanced word embedding methods

Deep learning, contextual embeddings

- BERT (Google, 2018)
- ELMo (Allen Institute for AI, 2018)
- GPT-2 (OpenAI, 2018)



# Advanced word embedding methods

Deep learning, contextual embeddings

- BERT (Google, 2018)
- ELMo (Allen Institute for AI, 2018)
- GPT-2 (OpenAI, 2018)

} Tunable pre-trained  
models available

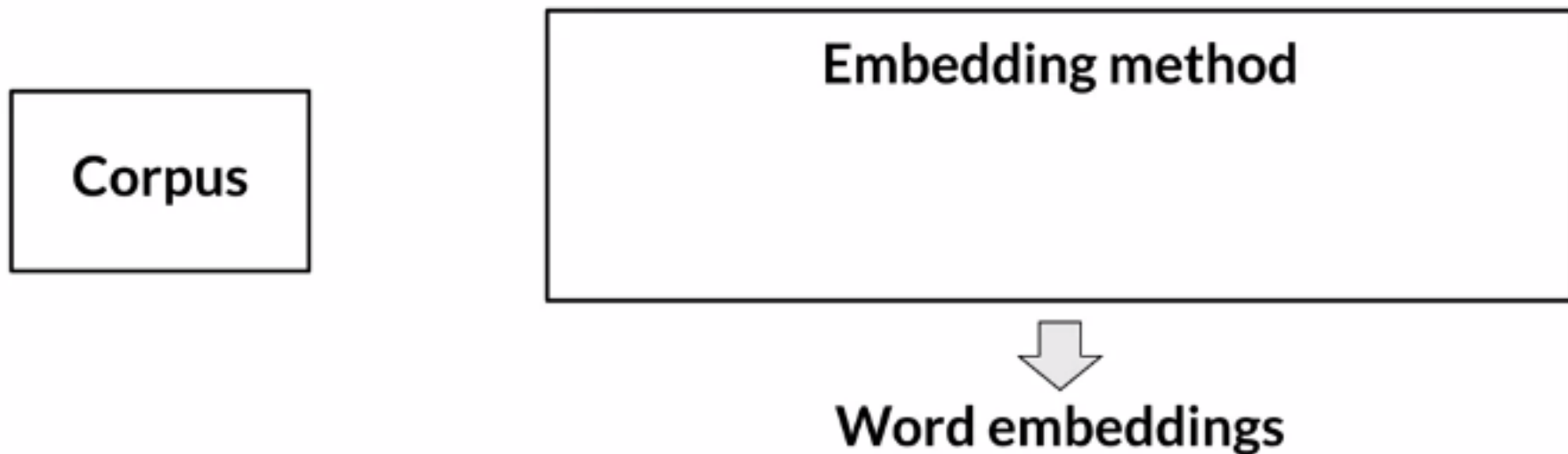
# Continuous bag-of-words word embedding process

# Continuous bag-of-words word embedding process

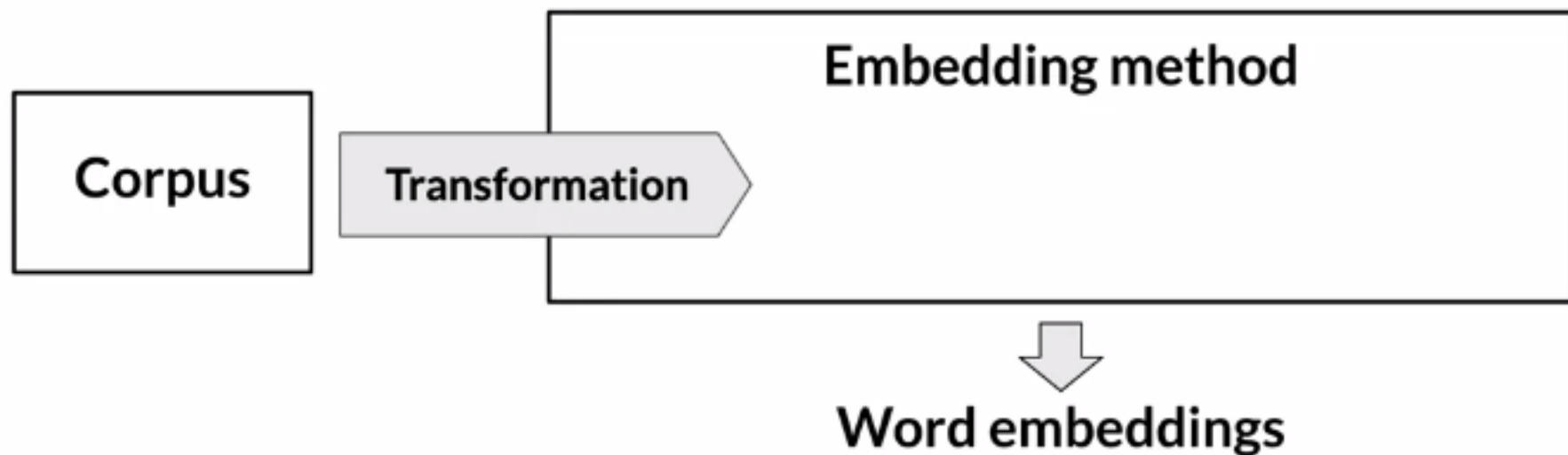
Corpus

Embedding method

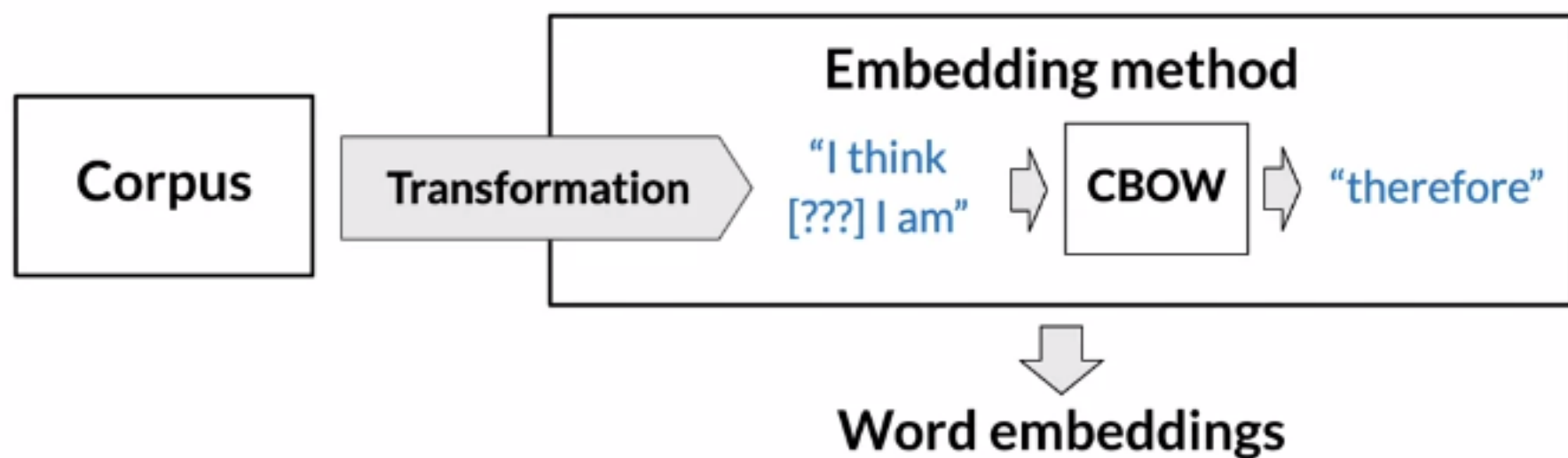
# Continuous bag-of-words word embedding process



# Continuous bag-of-words word embedding process



# Continuous bag-of-words word embedding process



Corpus

Transformation

CBOW

# Center word prediction: rationale

Corpus

Transformation

CBOW

## Center word prediction: rationale

The little \_\_\_\_\_ is barking



# Center word prediction: rationale

The little ? is barking



*dog*  
*puppy*  
*hound*  
*terrier*

...

## Creating a training example

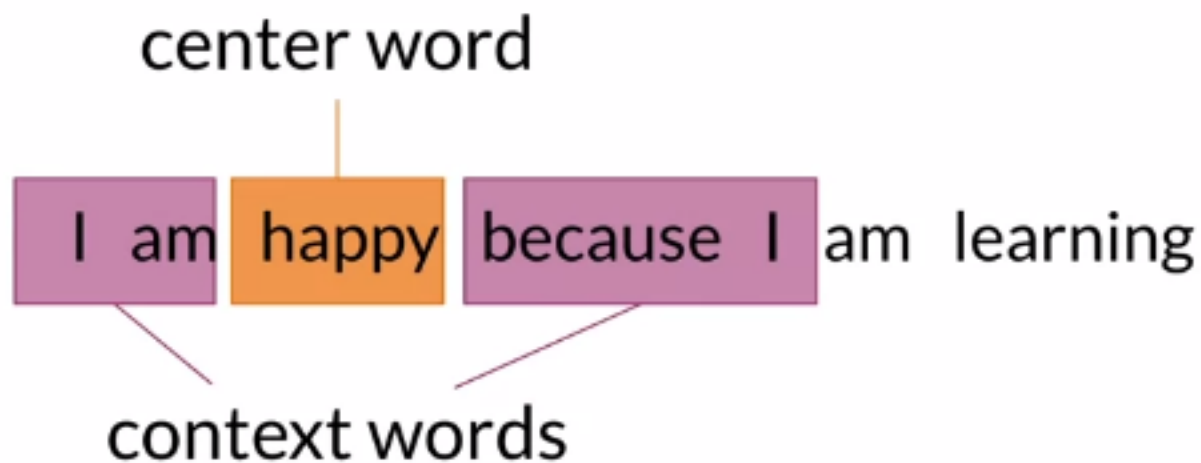
I am happy because I am learning

## Creating a training example

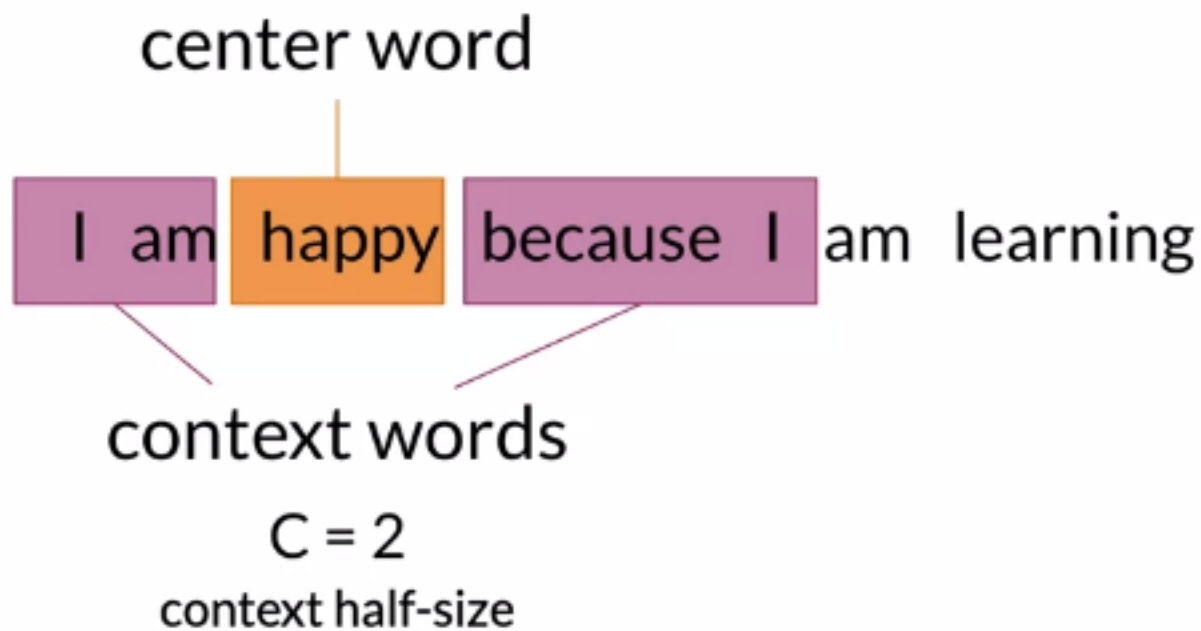
center word

I am **happy** because I am learning

## Creating a training example



# Creating a training example

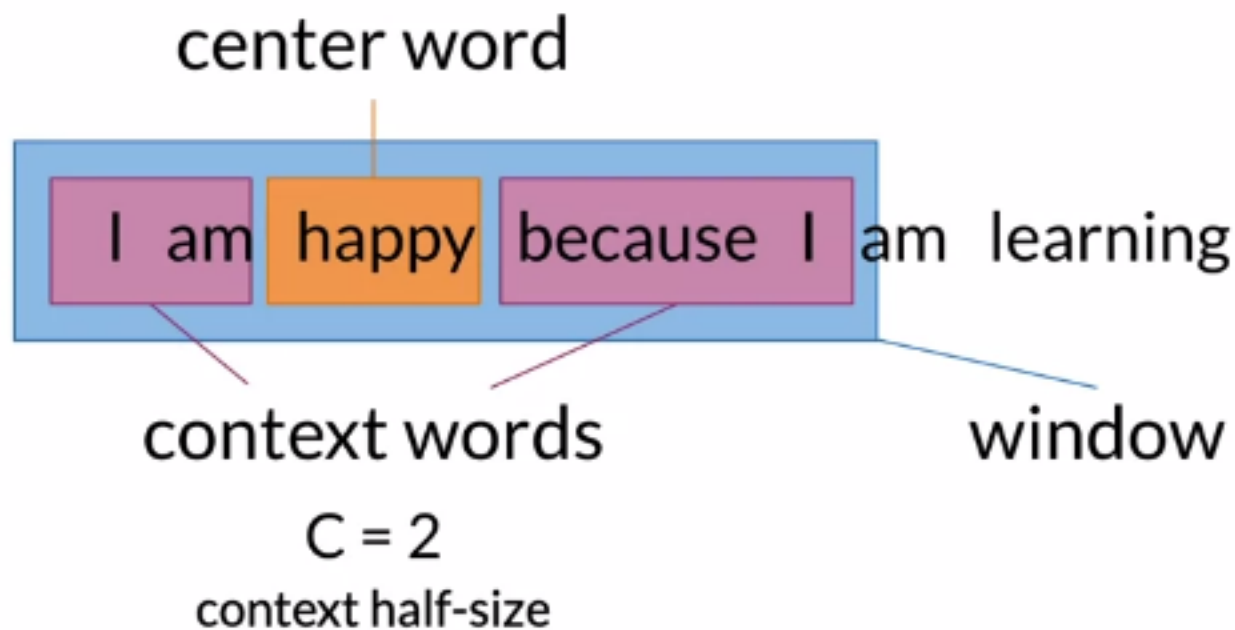


Corpus

Transformation

CBOW

## Creating a training example

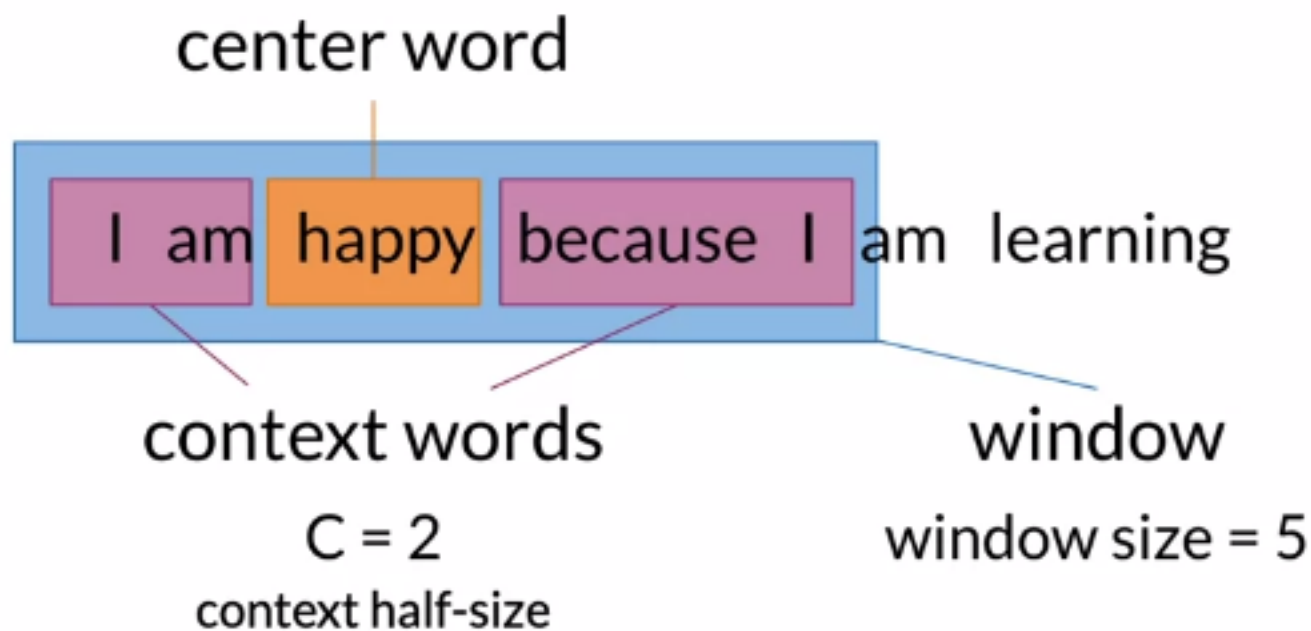


Corpus

Transformation

CBOW

## Creating a training example

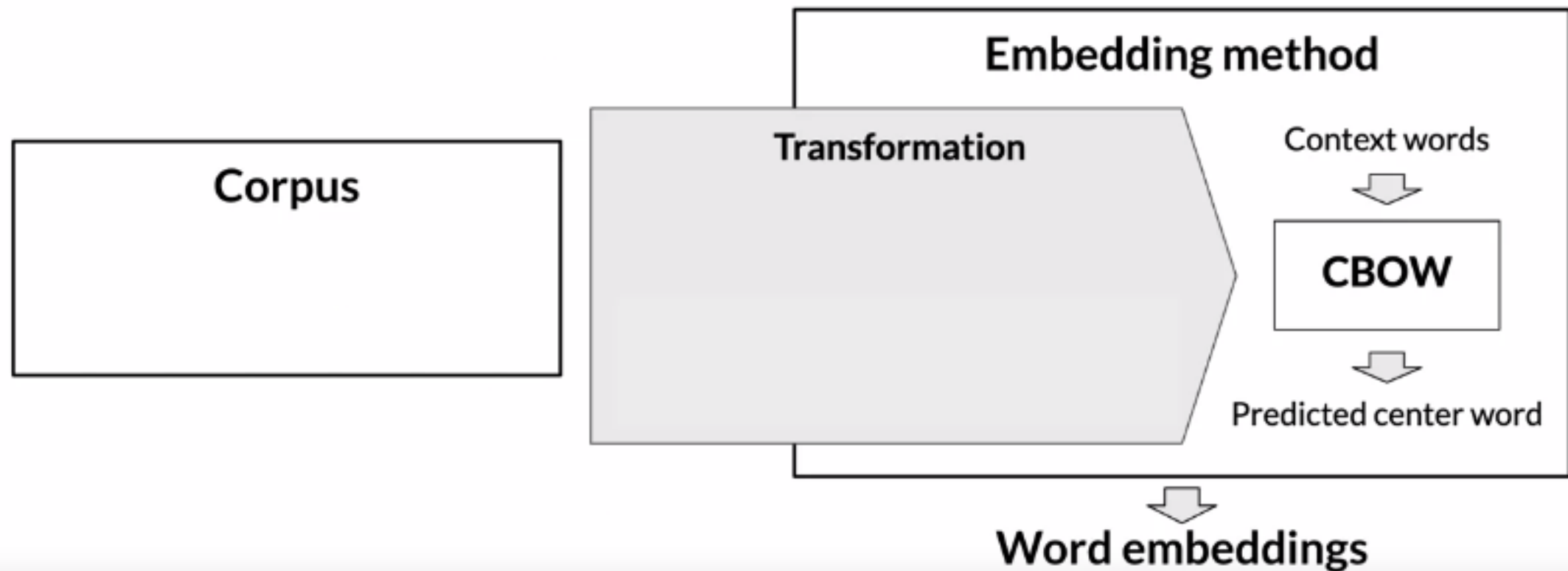


# From corpus to training

Corpus

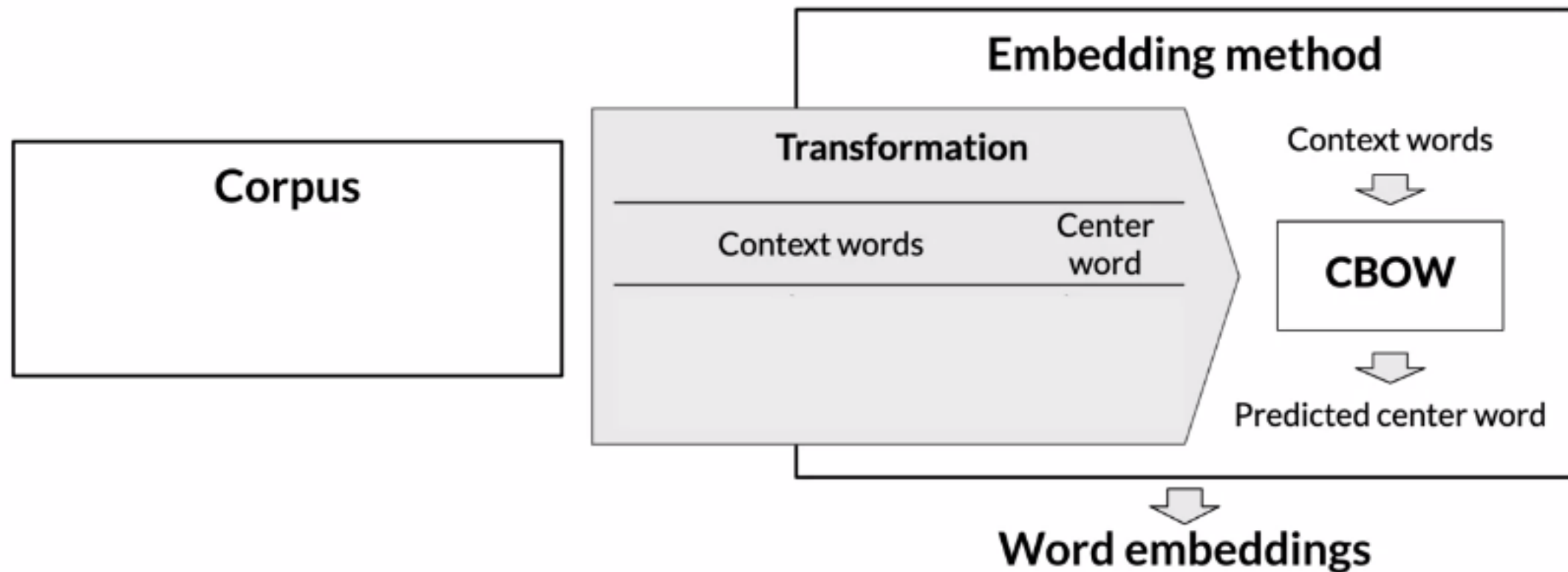
Transformation

CBOW

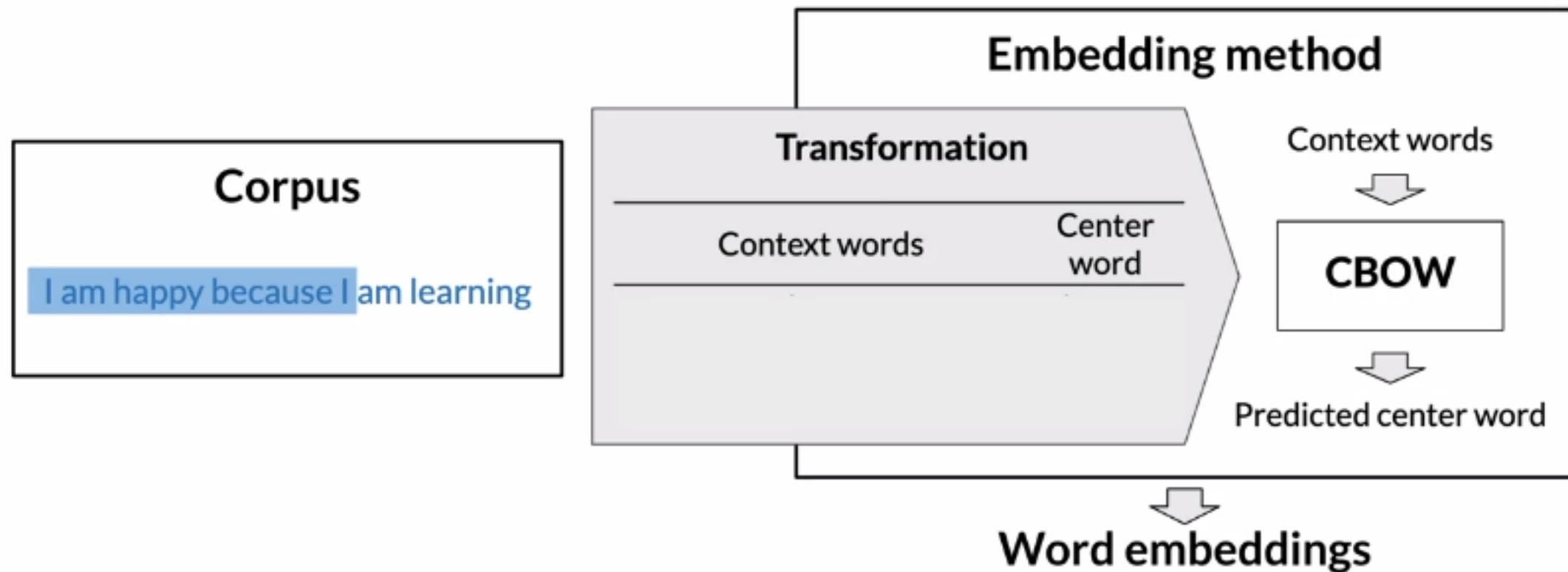




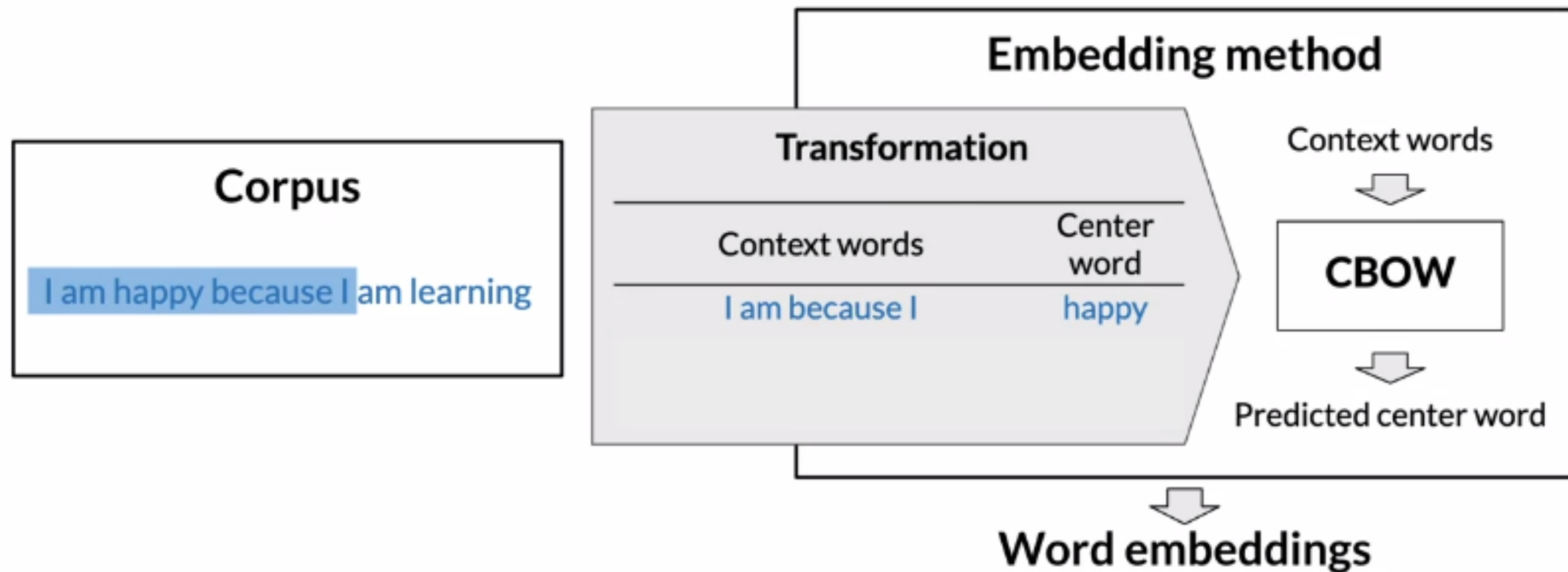
# From corpus to training



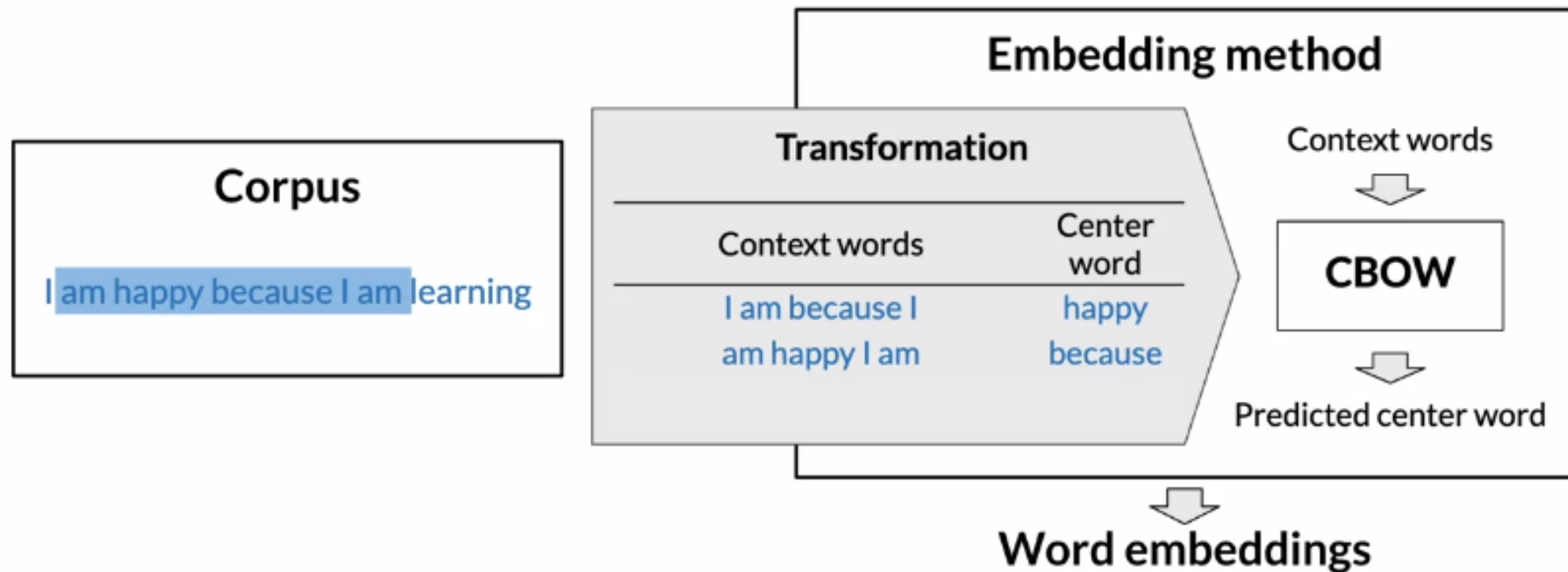
# From corpus to training



# From corpus to training



# From corpus to training

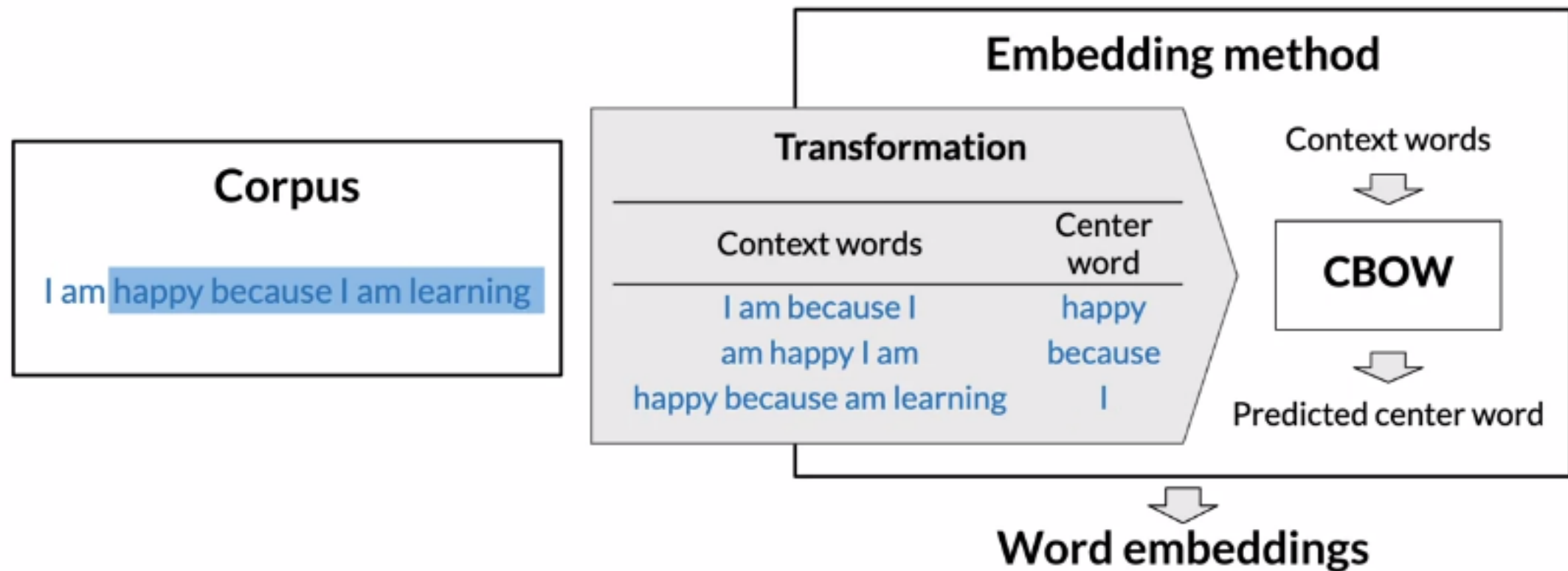


# From corpus to training

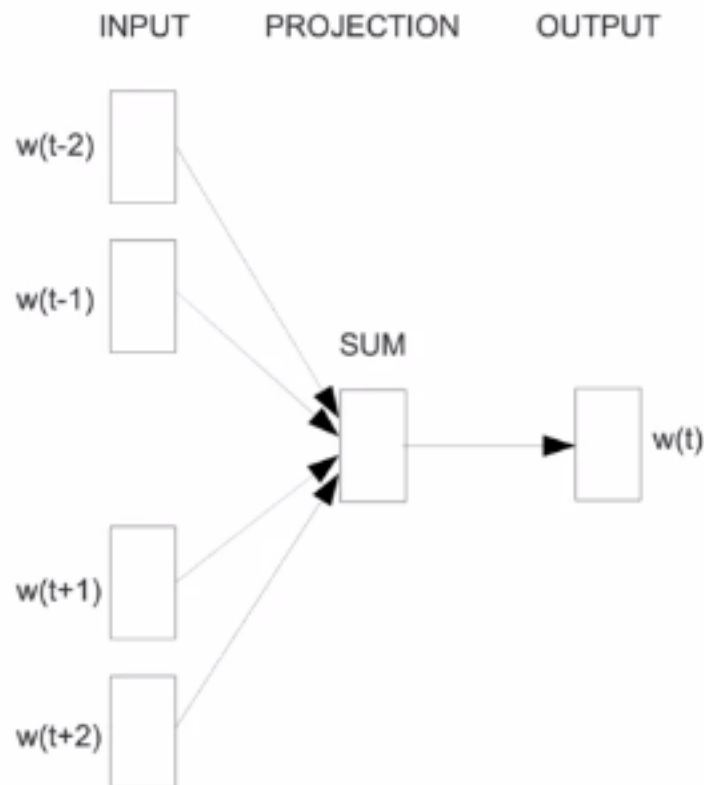
Corpus

Transformation

CBOW



# CBOW in a nutshell



Source: Mikolov, T., Chen, K., Corrado, G.S., & Dean, J. (2013).  
[Efficient Estimation of Word Representations in Vector Space](#)



deeplearning.ai

# Cleaning and Tokenization

# Cleaning and tokenization matters



# Cleaning and tokenization matters

- Letter case

# Cleaning and tokenization matters

- Letter case      `"The" == "the" == "THE"`

# Cleaning and tokenization matters

- Letter case                      “The” == “the” == “THE”    → *lowercase / upper case*

# Cleaning and tokenization matters

- Letter case                      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation

# Cleaning and tokenization matters

- Letter case                      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation                    , ! . ? → .

# Cleaning and tokenization matters

- Letter case      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅

# Cleaning and tokenization matters

- Letter case      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .

# Cleaning and tokenization matters

- Letter case      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers



# Cleaning and tokenization matters

- Letter case      "The" == "the" == "THE"    → lowercase / upper case
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210

# Cleaning and tokenization matters

- Letter case      "The" == "the" == "THE"    → lowercase / upper case
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210

# Cleaning and tokenization matters

- Letter case      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210 → *as is / <NUMBER>*

# Cleaning and tokenization matters

- Letter case      “The” == “the” == “THE”    → *lowercase / upper case*
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210 → *as is / <NUMBER>*
- Special characters

# Cleaning and tokenization matters

- Letter case      "The" == "the" == "THE"    → lowercase / upper case
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210 → as is / <NUMBER>
- Special characters      ∇ \$ € § ¶ \*\*

# Cleaning and tokenization matters

- Letter case      "The" == "the" == "THE"    → lowercase / upper case
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210 → as is / <NUMBER>
- Special characters      ∇ \$ € § ¶ \*\* → ∅

# Cleaning and tokenization matters

- Letter case      "The" == "the" == "THE"    → lowercase / upper case
- Punctuation      , ! . ? → .      “ ‘ « » ’ ” → ∅      ... !! ??? → .
- Numbers      1 2 3 5 8 → ∅      3.14159 90210 → as is / <NUMBER>
- Special characters      ∇ \$ € § ¶ \*\* → ∅
- Special words

# Cleaning and tokenization matters

- Letter case "The" == "the" == "THE" → lowercase / upper case
- Punctuation , ! . ? → . " ' « » ' " → ∅ ... !! ??? → .
- Numbers 1 2 3 5 8 → ∅ 3.14159 90210 → as is / <NUMBER>
- Special characters ∇ \$ € § ¶ \*\* → ∅
- Special words 😊 #nlp



# Cleaning and tokenization matters

- Letter case "The" == "the" == "THE" → lowercase / upper case
- Punctuation , ! . ? → . " ' « » ' " → ∅ ... !! ??? → .
- Numbers 1 2 3 5 8 → ∅ 3.14159 90210 → as is / <NUMBER>
- Special characters ∇ \$ € § ¶ \*\* → ∅
- Special words 😊 #nlp → :happy: #nlp

## Example in Python: corpus

Who ❤️ "word embeddings" in 2020? I do!!!

## Example in Python: corpus

Who  "word embeddings" in 2020? I do!!!

emoji

punctuation

number

# Example in Python: libraries

```
# pip install nltk  
# pip install emoji
```

```
import nltk  
from nltk.tokenize import word_tokenize  
import emoji
```

```
nltk.download('punkt') # download pre-trained Punkt tokenizer for English
```

## Example in Python: code

```
corpus = 'Who ❤️ "word embeddings" in 2020? I do!!!'  
  
data = re.sub(r'[,!?;-]+', '.', corpus)
```

## Example in Python: code

```
corpus = 'Who ❤️ "word embeddings" in 2020? I do!!!'
```

```
data = re.sub(r'[,!?;-]+', '.', corpus)
```

→ Who ❤️ "word embeddings" in 2020. I do.

## Example in Python: code

```
corpus = 'Who ❤️ "word embeddings" in 2020? I do!!!'
```

```
data = re.sub(r'[,!?;-]+', '.', corpus)
```

```
data = nltk.word_tokenize(data) # tokenize string to words
```

```
→ ['Who', '❤️', '``', 'word', 'embeddings', '"', 'in', '2020', '.', 'I',  
    'do', '.']
```

## Example in Python: code

```
corpus = 'Who ❤️ "word embeddings" in 2020? I do!!!'

data = re.sub(r'[,!?;-]+' , '.', corpus)
data = nltk.word_tokenize(data) # tokenize string to words
data = [ ch.lower() for ch in data
         if ch.isalpha()
         or ch == '.'
         or emoji.get_emoji_regexp().search(ch)
       ]
```



## Example in Python: code

```
corpus = 'Who ❤️ "word embeddings" in 2020? I do!!!'

data = re.sub(r'[,!?;-]+', '.', corpus)
data = nltk.word_tokenize(data) # tokenize string to words
data = [ ch.lower() for ch in data
         if ch.isalpha()
         or ch == '.'
         or emoji.get_emoji_regexp().search(ch)
       ]
```

→ ['who', '❤️', 'word', 'embeddings', 'in', '.', 'i', 'do', '.']



deeplearning.ai

# Sliding Window of Words in Python

---

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
---	----	-------	---------	---	----	----------

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
0	1	2	3	4	5	6

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
0	1	2	3	4	5	6



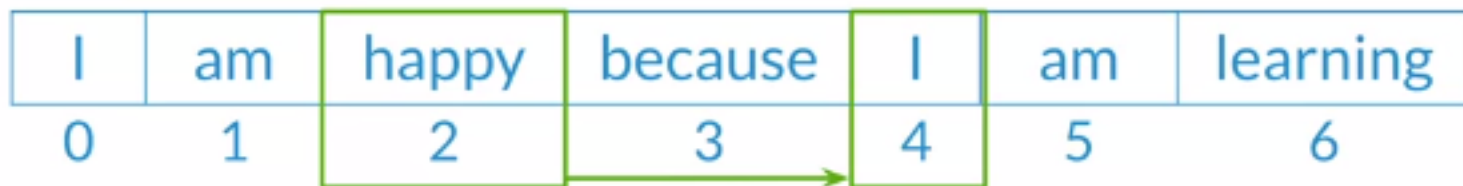
# Sliding window of words in Python

```
def get_windows(words, C):  
    i = 0  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
0	1	2	3	4	5	6

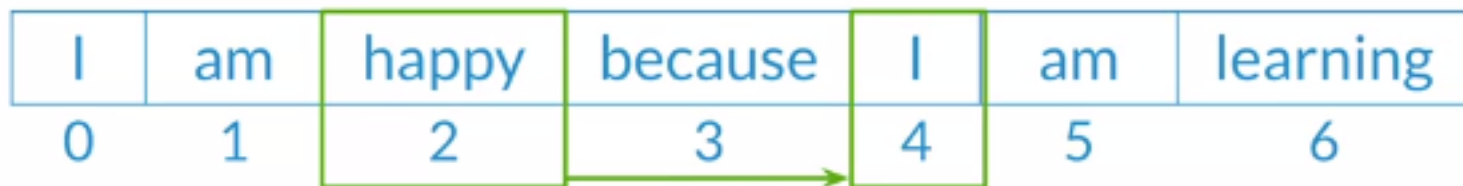
# Sliding window of words in Python

```
def get_windows(words, C):  
    i = 0  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```



# Sliding window of words in Python

```
def get_windows(words, C):  
    i = 0  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```



# Sliding window of words in Python

```
def get_windows(words, C):  
    i = C  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
0	1	2	3	4	5	6

# Sliding window of words in Python

```
def get_windows(words, C):  
    i = 0  
    while i < len(words) - C:  
        center_word = words[i]  
        context_words = words[(i - C):i] + words[(i+1):(i+C+1)]  
        yield context_words, center_word  
        i += 1
```

I	am	happy	because	I	am	learning
0	1	2	3	4	5	6

# Sliding window of words in Python

```
def get_windows(words, C):  
    ...  
    yield context_words, center_word
```

```
for x, y in get_windows(  
    ['i', 'am', 'happy', 'because', 'i', 'am', 'learning'],  
    2  
):  
    print(f'{x}\t{y}')
```

# Sliding window of words in Python

```
def get_windows(words, C):  
    ...  
    yield context_words, center_word
```

```
for x, y in get_windows(  
    ['i', 'am', 'happy', 'because', 'i', 'am', 'learning'],  
    2  
):  
    print(f'{x}\t{y}')
```

# Sliding window of words in Python

```
for x, y in get_windows(  
    ['i', 'am', 'happy', 'because', 'i', 'am', 'learning'],  
    2  
):  
    print(f'{x}\t{y}')
```

→ ['I', 'am', 'because', 'I']      happy  
   ['am', 'happy', 'I', 'am']      because  
   ['happy', 'because', 'am', 'learning']    I





deeplearning.ai

# Transforming Words into Vectors

# Transforming center words into vectors

Corpus      I am happy because I am learning

# Transforming center words into vectors

Corpus      I am happy because I am learning

Vocabulary      am, because, happy, I, learning

# Transforming center words into vectors

Corpus      I am happy because I am learning

Vocabulary      am, because, happy, I, learning

One-hot  
vector

am  
because  
happy  
I  
learning

 $\left( \begin{array}{c} \\ \\ \\ \\ \end{array} \right)$

# Transforming center words into vectors

Corpus      I am happy because I am learning

Vocabulary    am, because, happy, I, learning

One-hot  
vector

	am
am	1
because	0
happy	0
I	0
learning	0

# Transforming center words into vectors

Corpus      I am happy because I am learning

Vocabulary    am, because, happy, I, learning

One-hot vector	am	because
am	$\begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$
because		
happy		
I		
learning		

# Transforming center words into vectors

Corpus      I am happy because I am learning

Vocabulary    am, because, happy, I, learning

One-hot vector	am	because	happy	I	learning
am	$\begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$
because					
happy					
I					
learning					

# Transforming context words into vectors

Average of individual one-hot vectors



# Transforming context words into vectors

Average of individual one-hot vectors

I am because I

# Transforming context words into vectors

Average of individual one-hot vectors

	I	am	because	I
am	0			
because	0			
happy	0			
I	1			
learning	0			

# Transforming context words into vectors

Average of individual one-hot vectors

	I	am	because	I
am	0			
because	0			
happy	0			
I	1			
learning	0			

# Transforming context words into vectors

Average of individual one-hot vectors

	I	am	because	I
am	0	1		
because	0	0		
happy	0	0		
I	1	0		
learning	0	0		

# Transforming context words into vectors

Average of individual one-hot vectors

	I	am	because	I
am	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}$
because				
happy				
I				
learning				

# Transforming context words into vectors

Average of individual one-hot vectors

$$\left( \begin{array}{c} \text{I} \\ \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{array} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} + \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} \right) / 4 = \begin{pmatrix} 0.25 \\ 0.25 \\ 0 \\ 0.5 \\ 0 \end{pmatrix}$$

I am because I

# Transforming context words into vectors

Average of individual one-hot vectors

$$\left( \begin{array}{c} \text{I} \\ \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{array} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} + \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} \right) / 4 = \begin{pmatrix} 0.25 \\ 0.25 \\ 0 \\ 0.5 \\ 0 \end{pmatrix}$$

I am because I

# Final prepared training set

<i>Context words</i>	Context words vector	<i>Center word</i>	Center word vector
<i>I am because I</i>	[0.25; 0.25; 0; 0.5; 0]	<i>happy</i>	[0; 0; 1; 0; 0]



# Final prepared training set

<i>Context words</i>	<i>Context words vector</i>	<i>Center word</i>	<i>Center word vector</i>
<i>I am because I</i>	<i>[0.25; 0.25; 0; 0.5; 0]</i>	<i>happy</i>	<i>[0; 0; 1; 0; 0]</i>
<i>am happy I am</i>	<i>[0.5; 0; 0.25; 0.25; 0]</i>	<i>because</i>	<i>[0; 1; 0; 0; 0]</i>
<i>happy because am learning</i>	<i>[0.25; 0.25; 0.25; 0; 0.25]</i>	<i>I</i>	<i>[0; 0; 0; 1; 0]</i>

# Architecture of the CBOW model

# Architecture of the CBOW model

Input layer



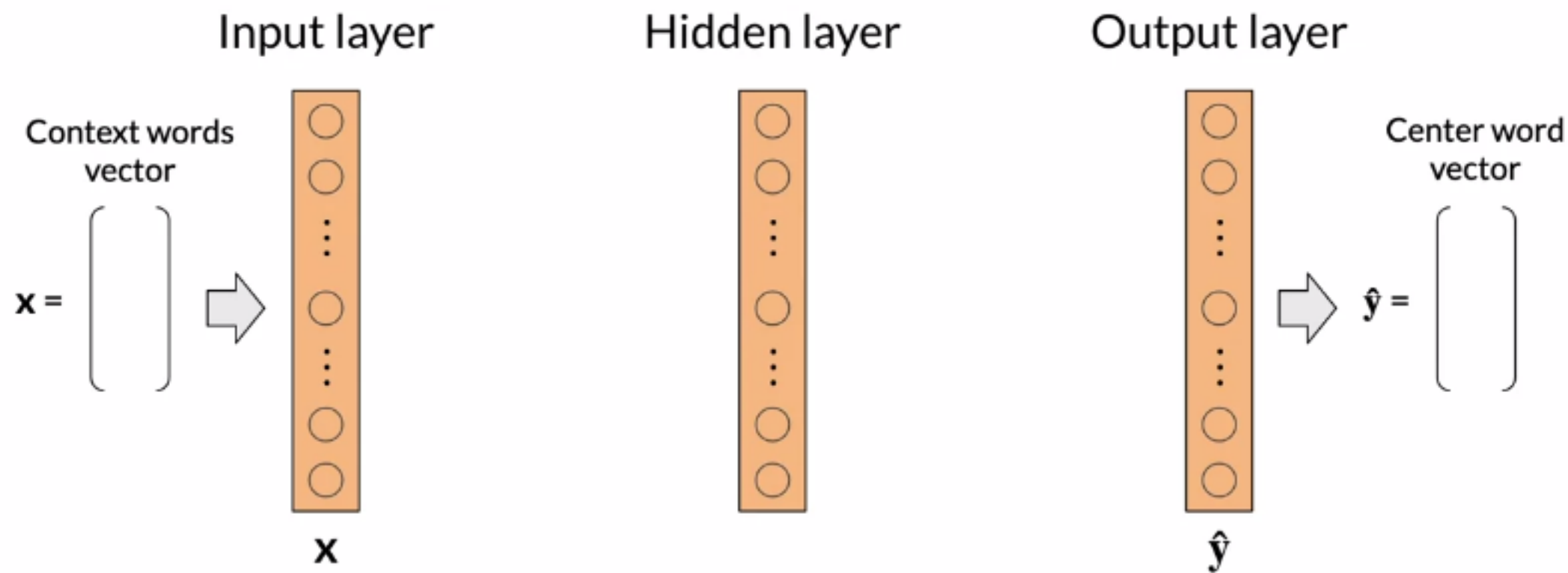
Hidden layer



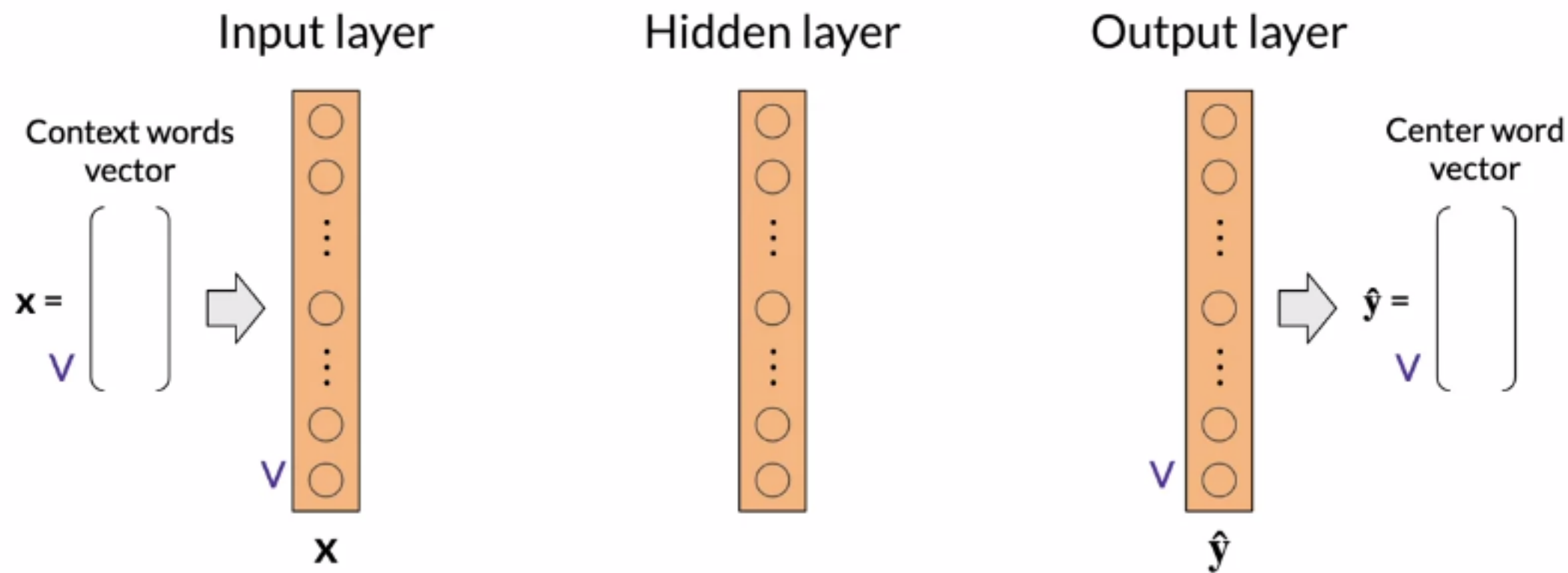
Output layer



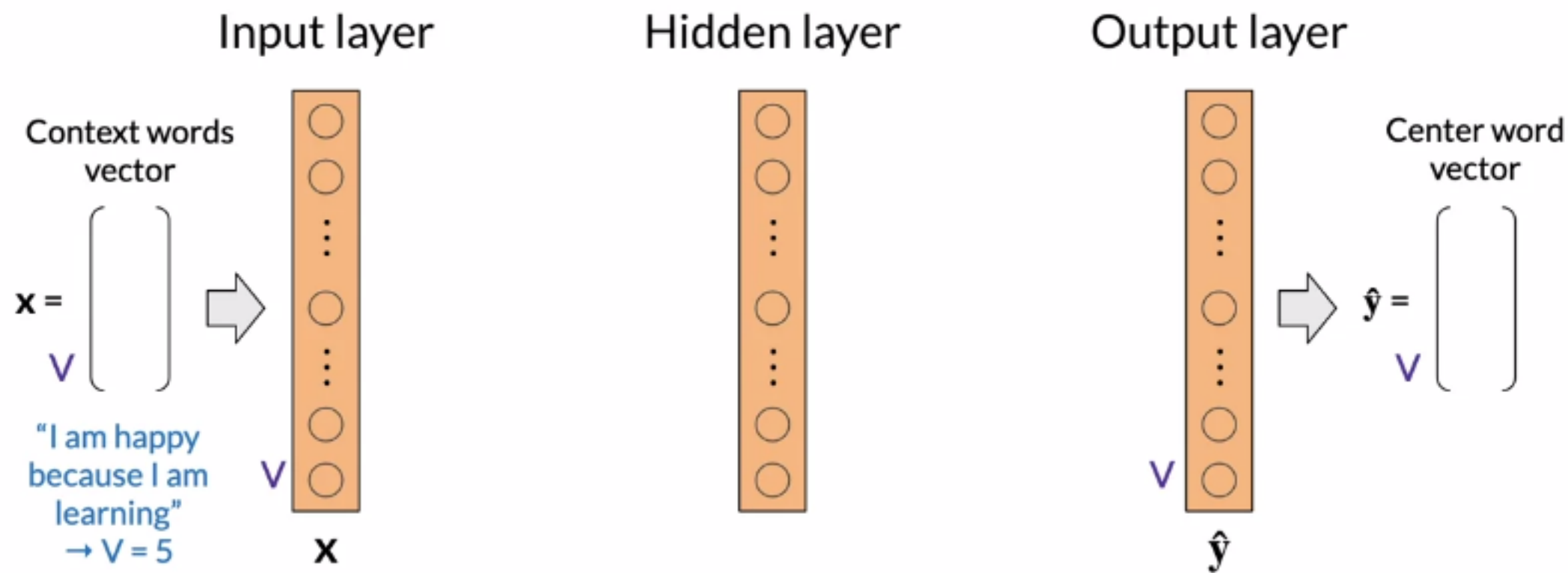
# Architecture of the CBOW model



# Architecture of the CBOW model



# Architecture of the CBOW model

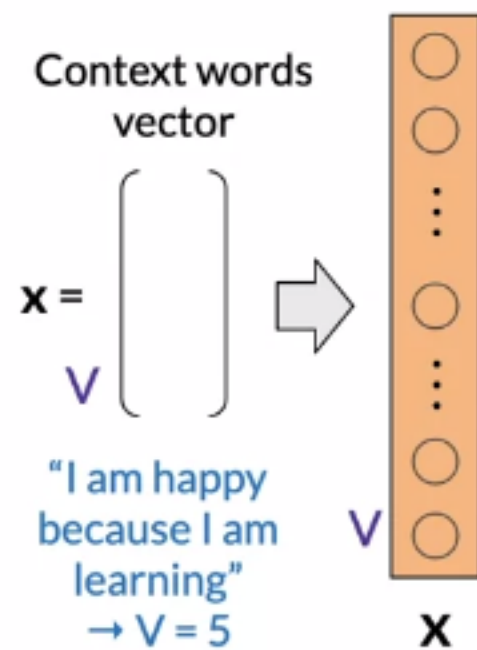


# Architecture of the CBOW model

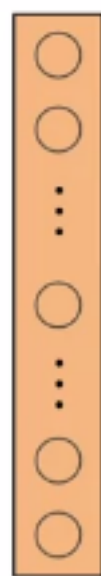
## Hyperparameters

Word embedding size ...

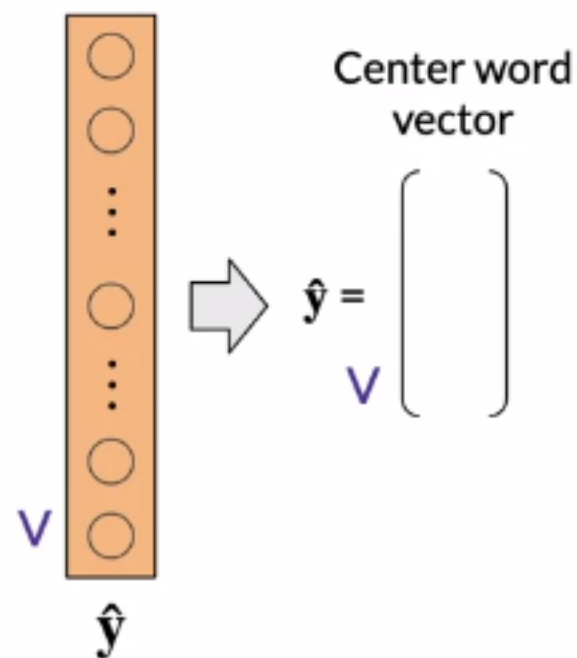
Input layer



Hidden layer



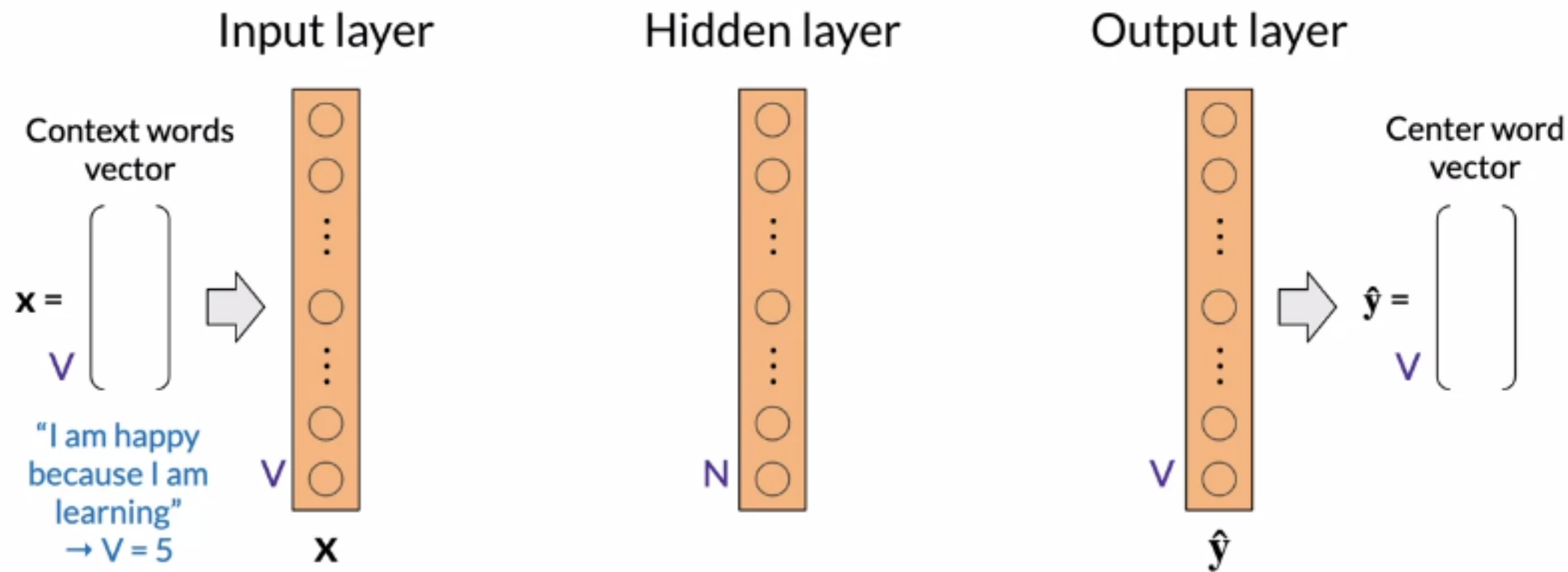
Output layer



# Architecture of the CBOW model

## Hyperparameters

$N$ : Word embedding size ...

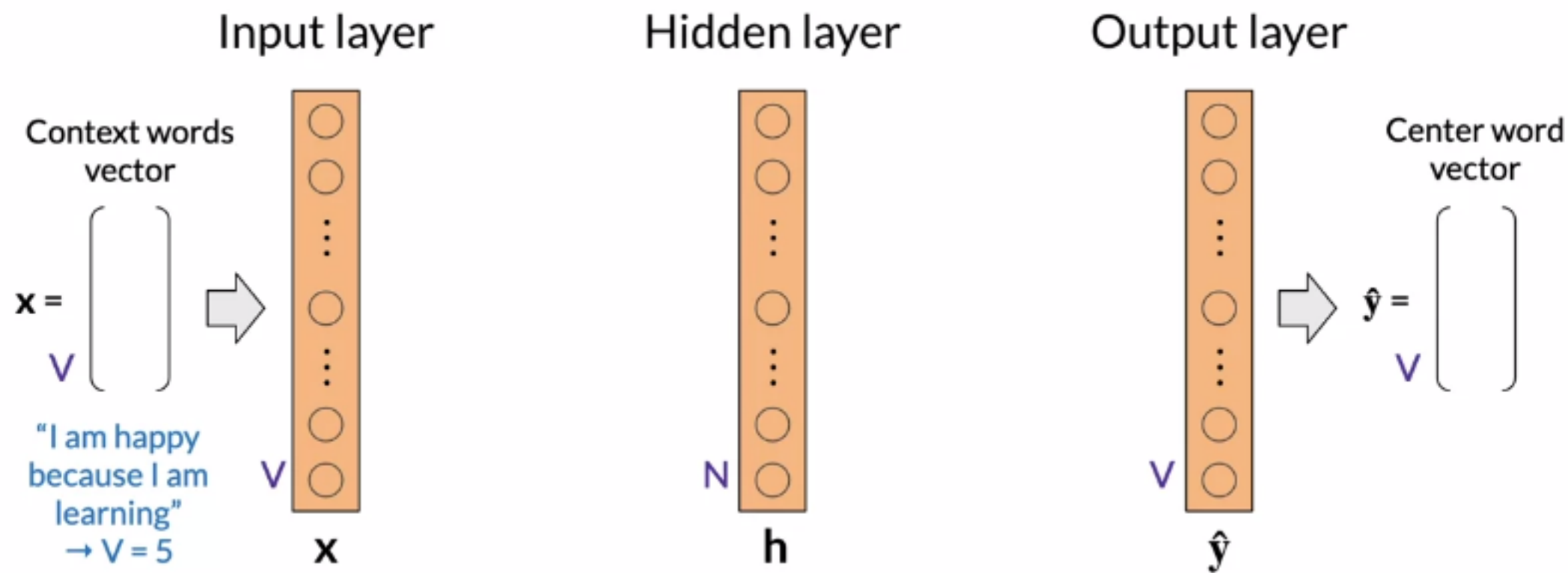




# Architecture of the CBOW model

## Hyperparameters

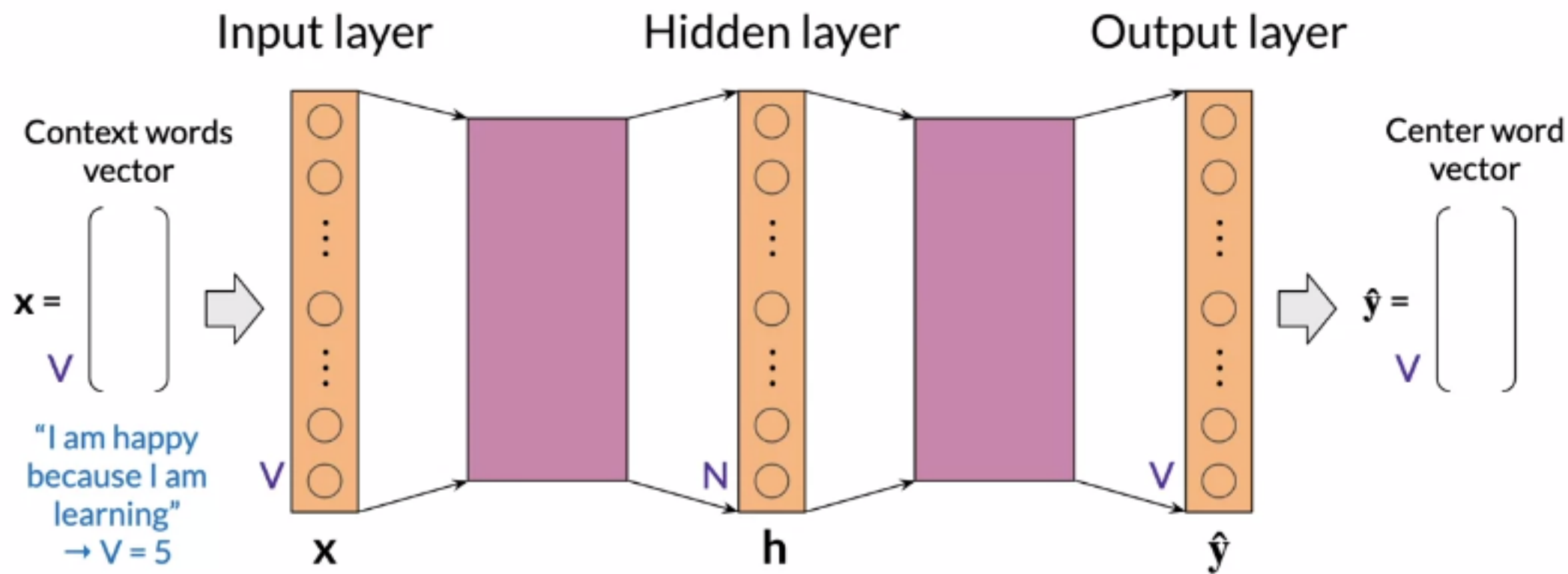
$N$ : Word embedding size ...



# Architecture of the CBOW model

## Hyperparameters

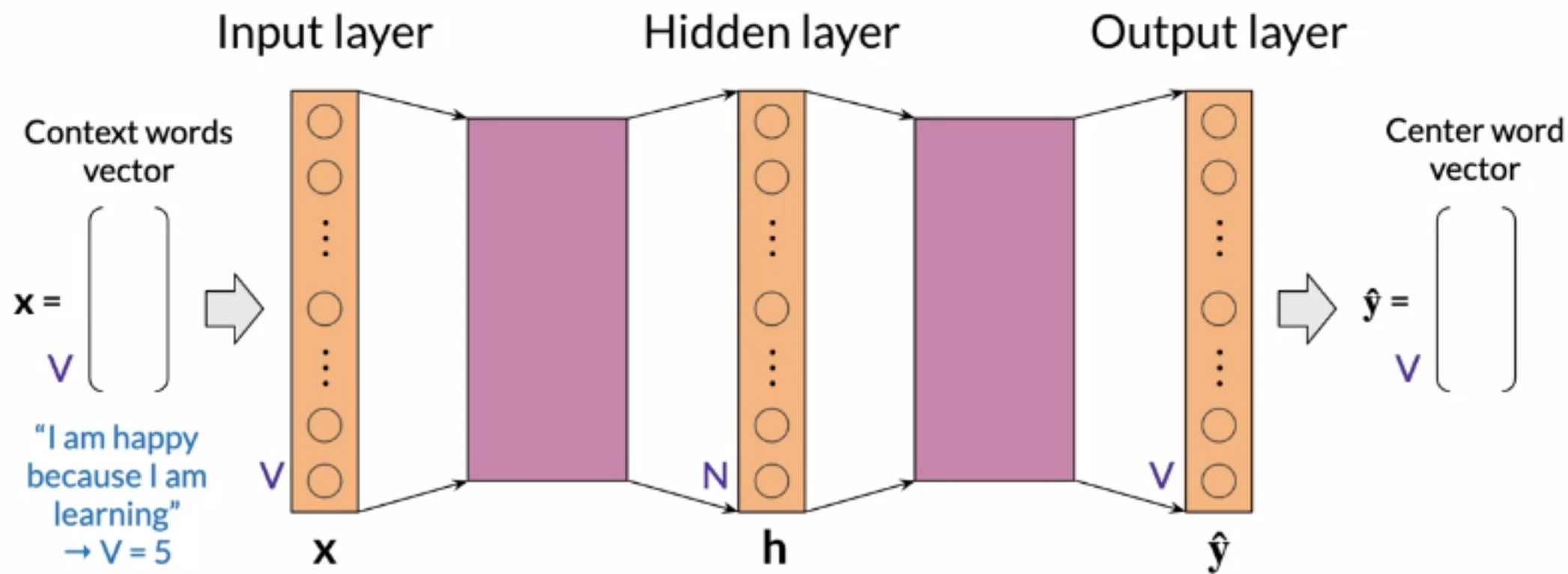
$N$ : Word embedding size ...



# Architecture of the CBOW model

## Hyperparameters

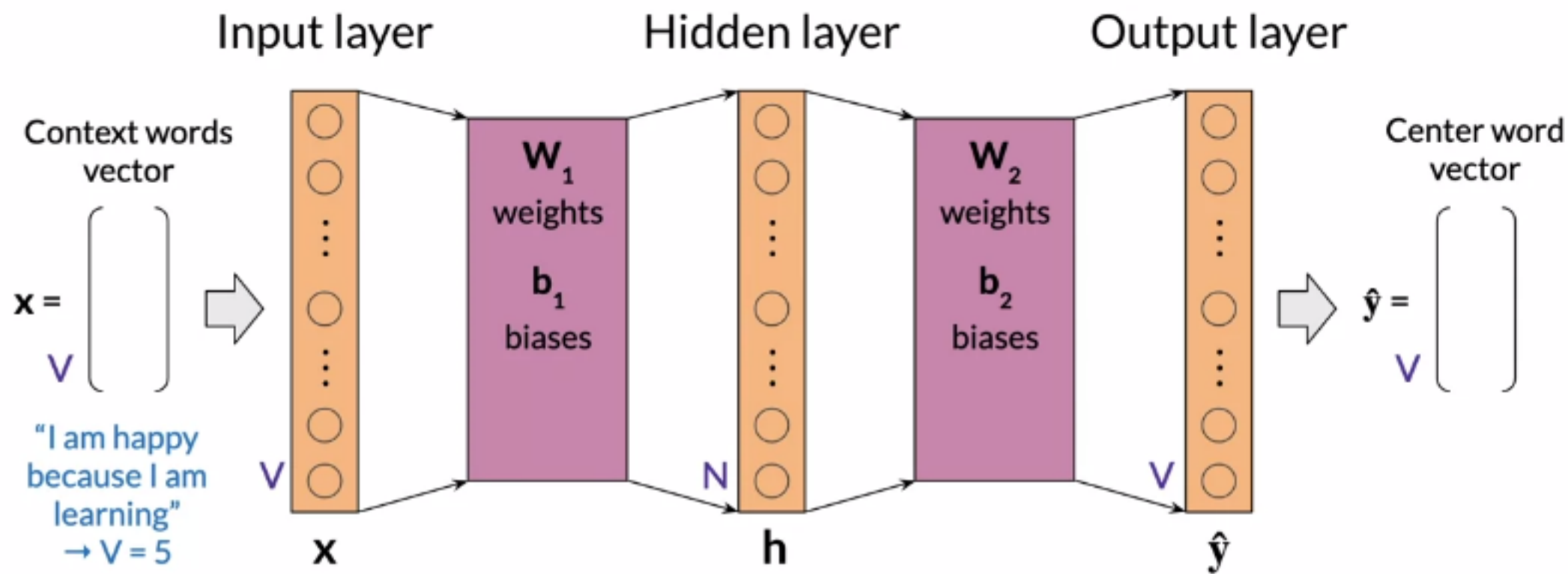
$N$ : Word embedding size ...



# Architecture of the CBOW model

## Hyperparameters

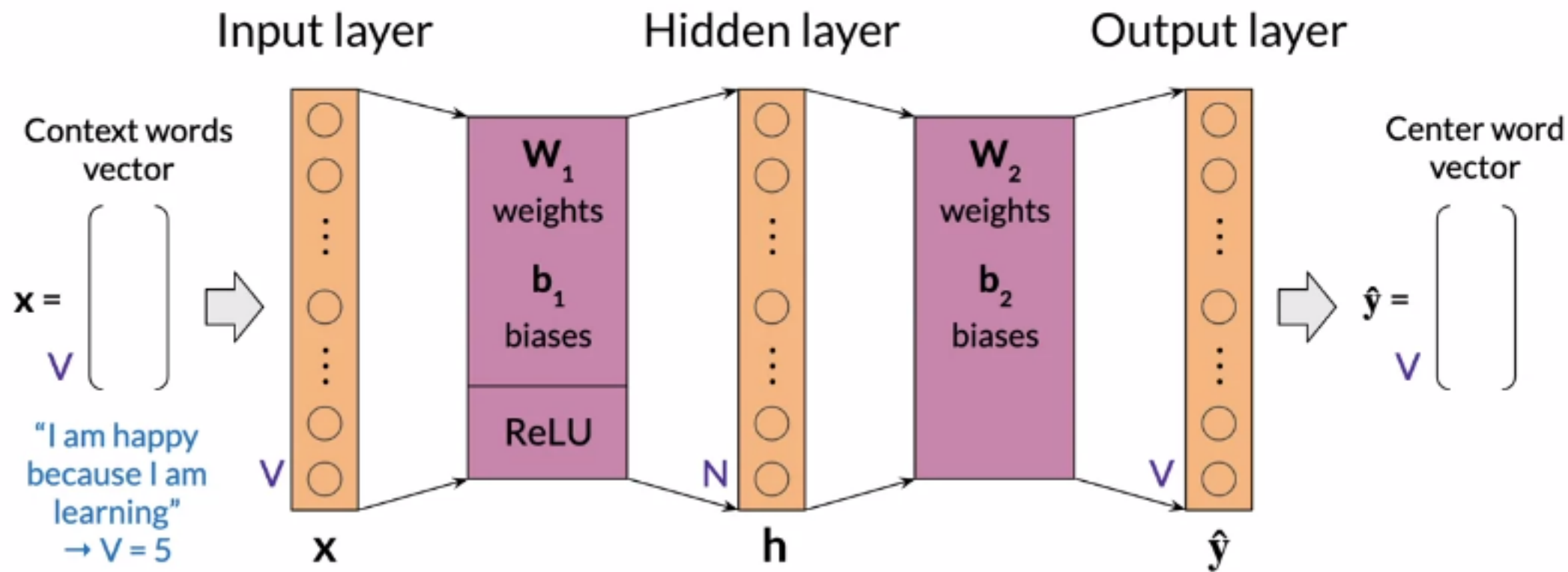
$N$ : Word embedding size ...



# Architecture of the CBOW model

## Hyperparameters

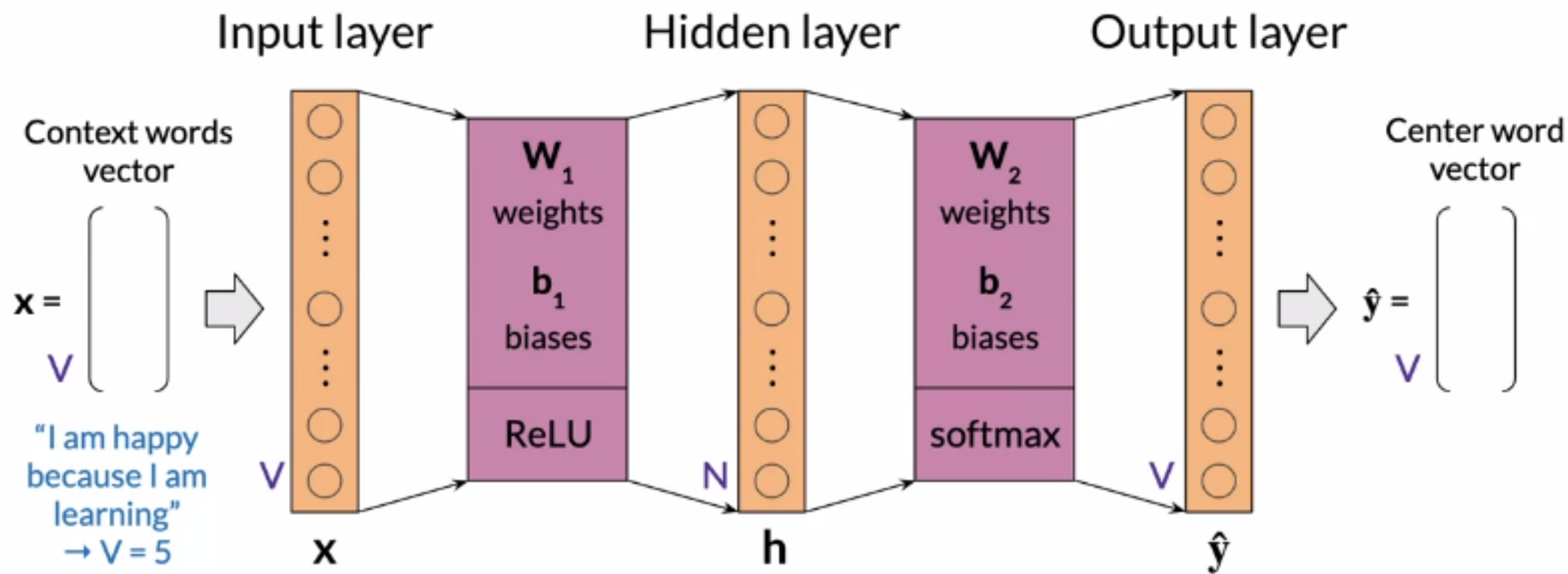
$N$ : Word embedding size ...



# Architecture of the CBOW model

## Hyperparameters

$N$ : Word embedding size ...





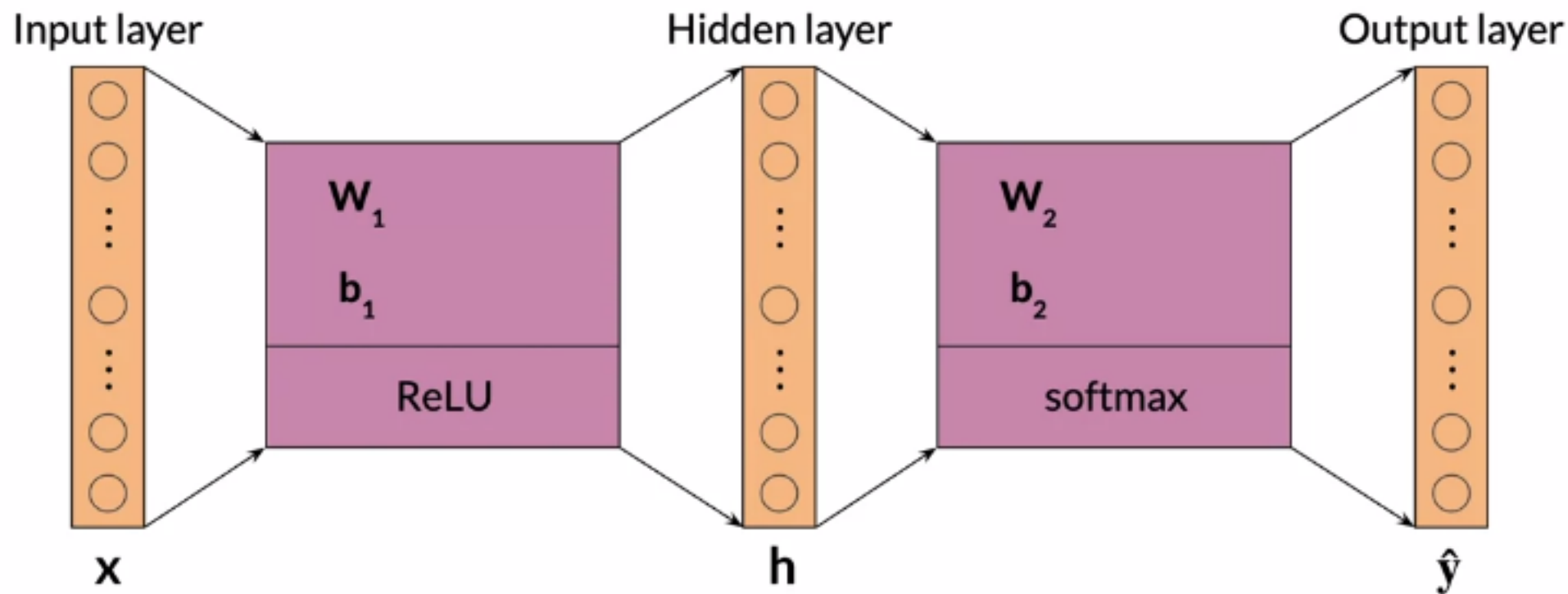
deeplearning.ai

# Architecture of the CBOW Model:

---

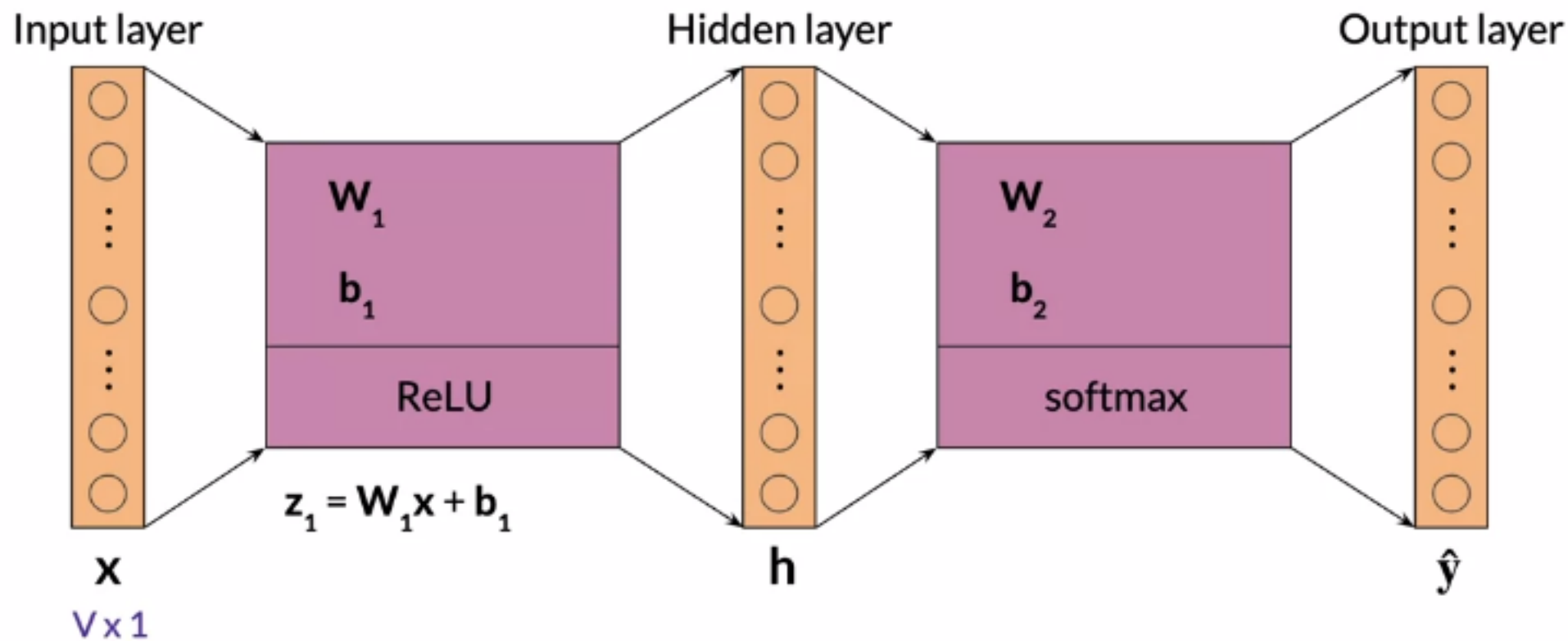
Dimensions

# Dimensions (single input)

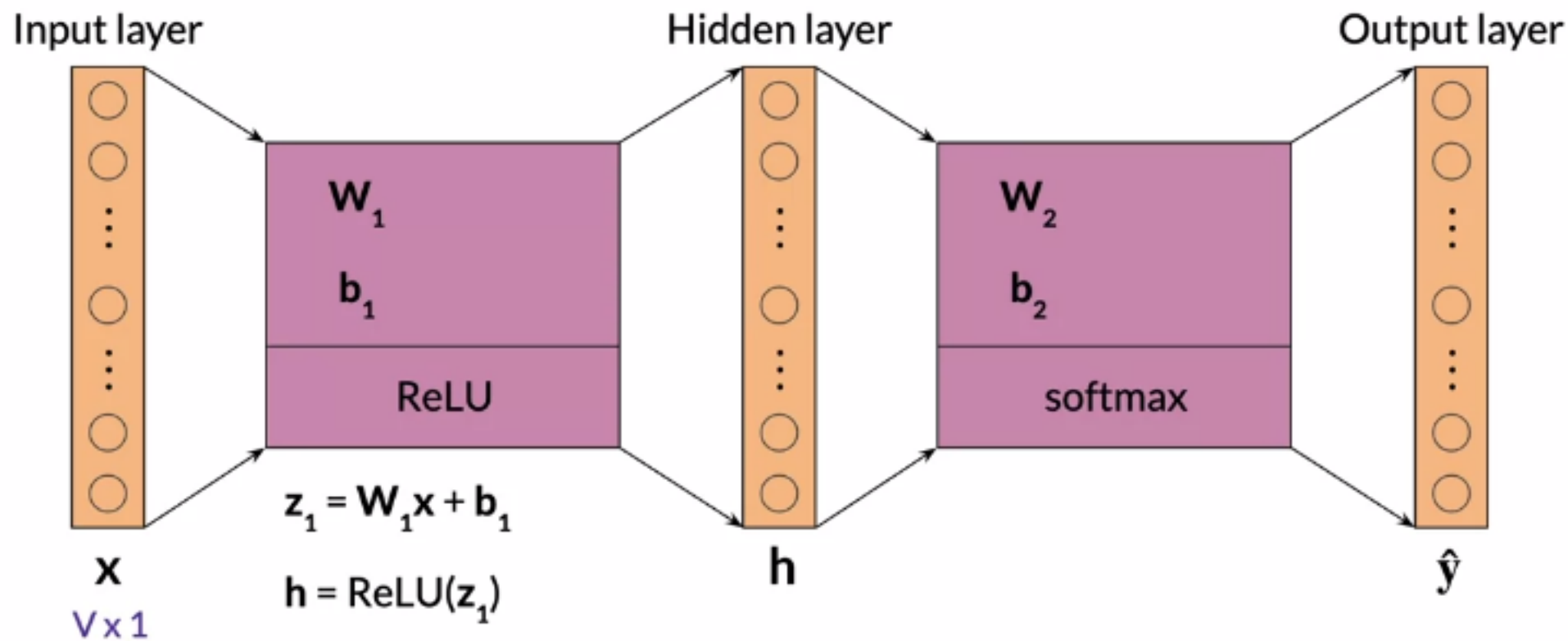




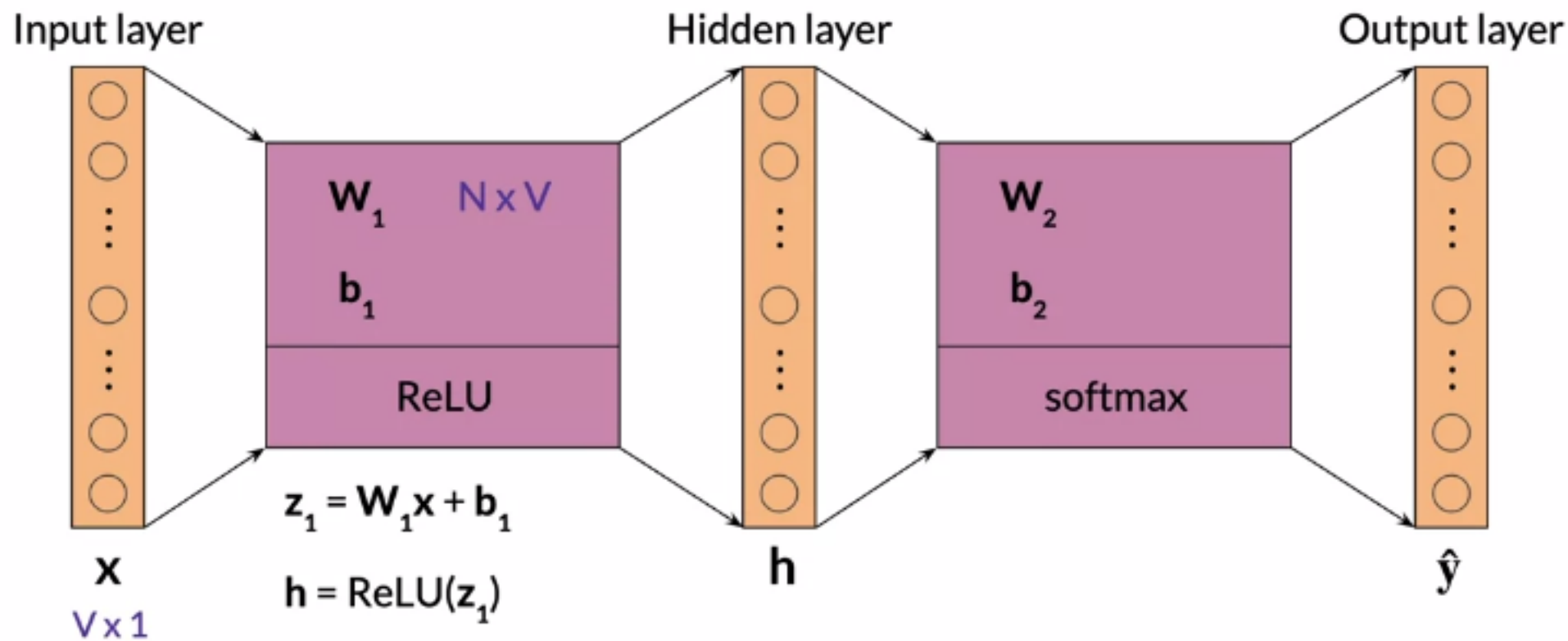
# Dimensions (single input)



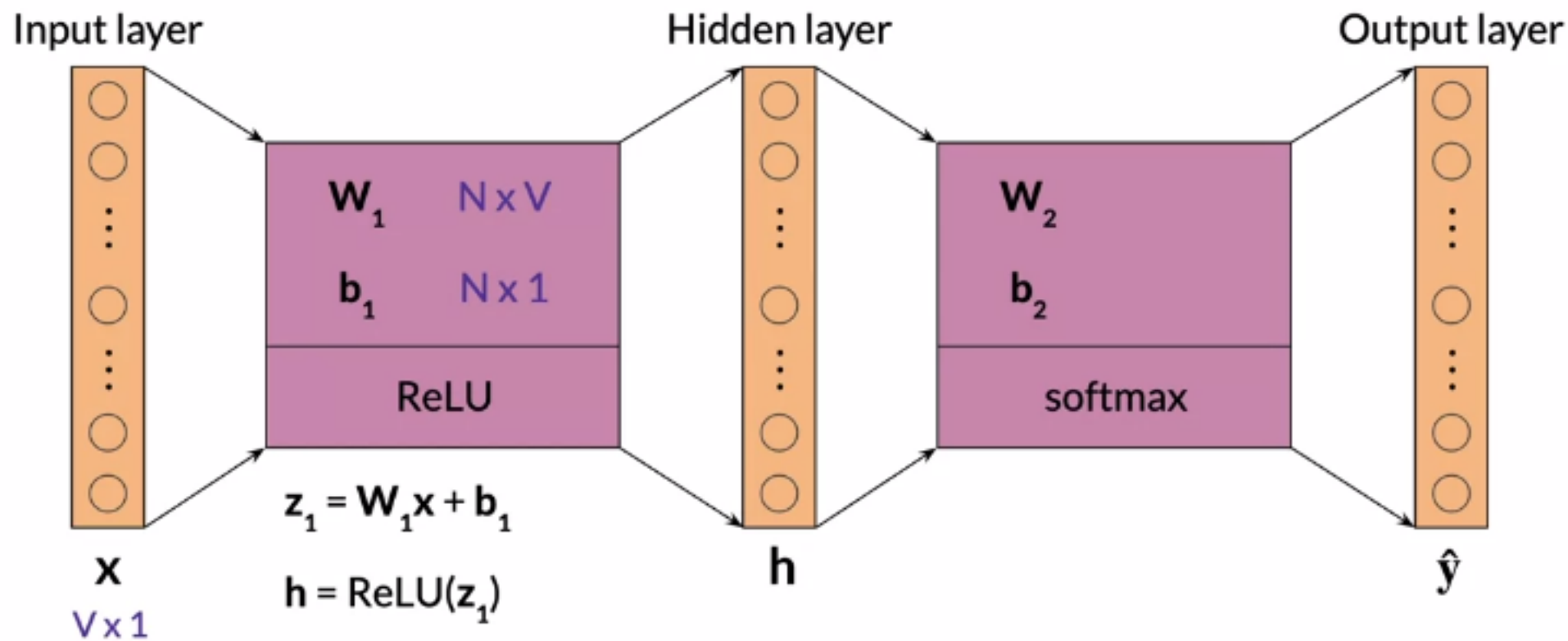
# Dimensions (single input)



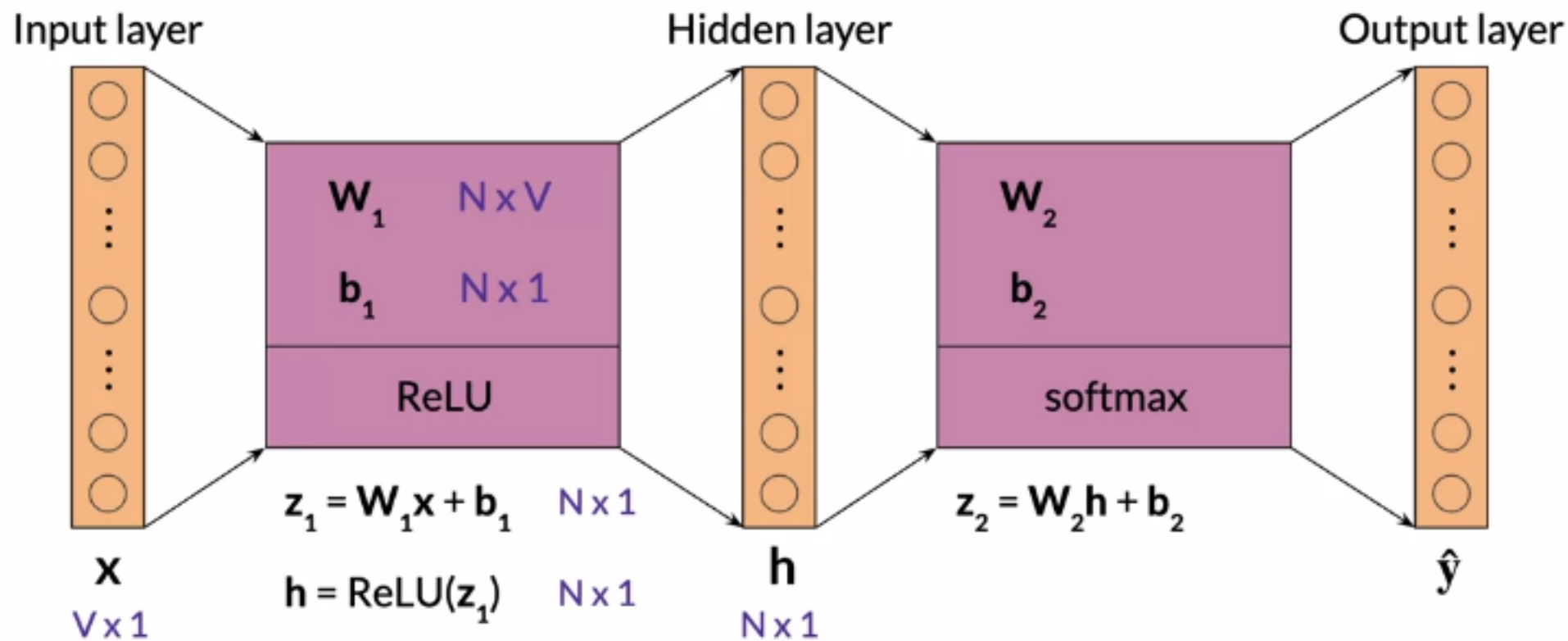
# Dimensions (single input)



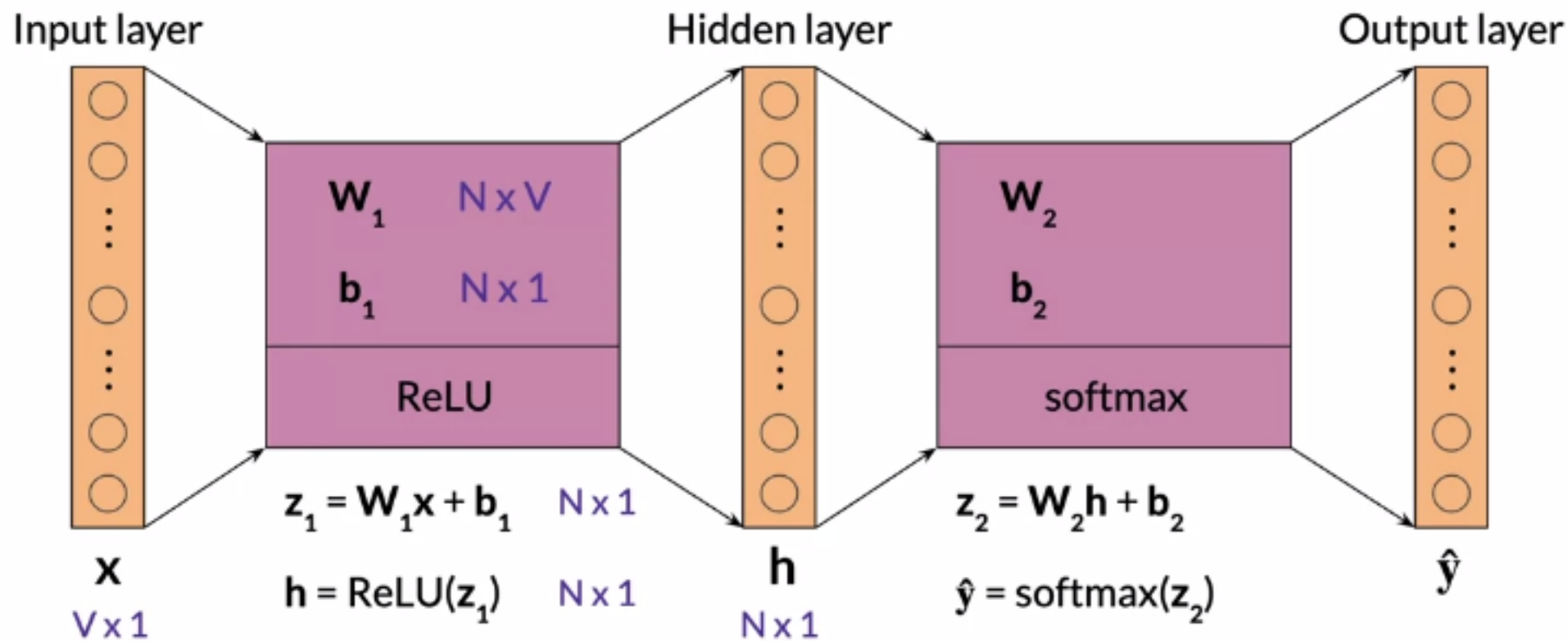
# Dimensions (single input)



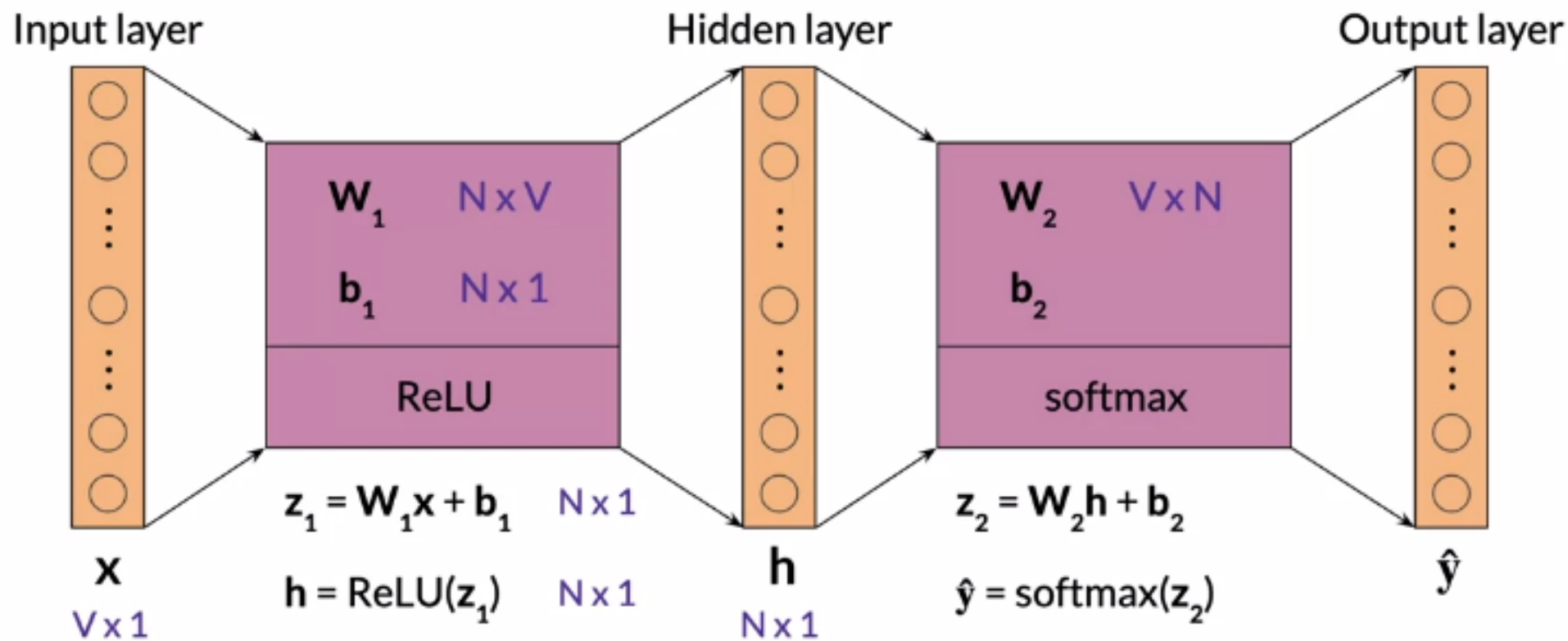
# Dimensions (single input)



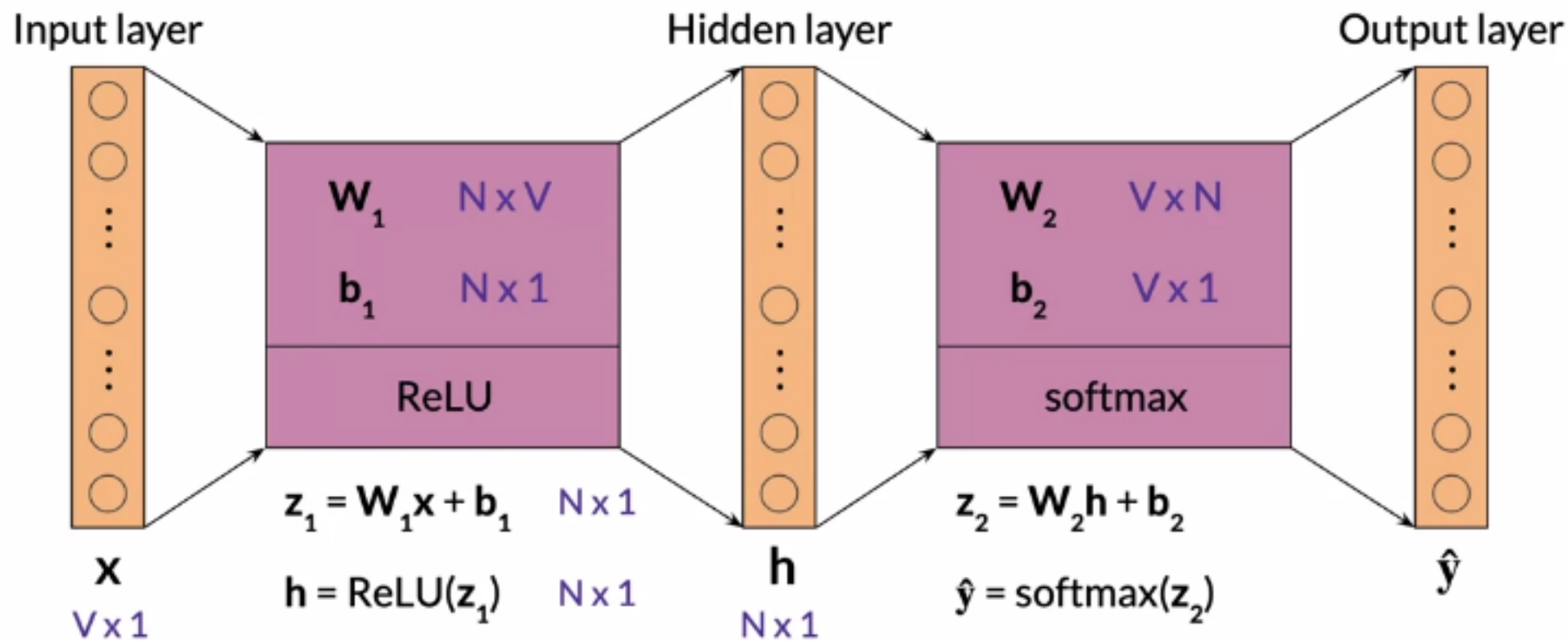
# Dimensions (single input)



# Dimensions (single input)

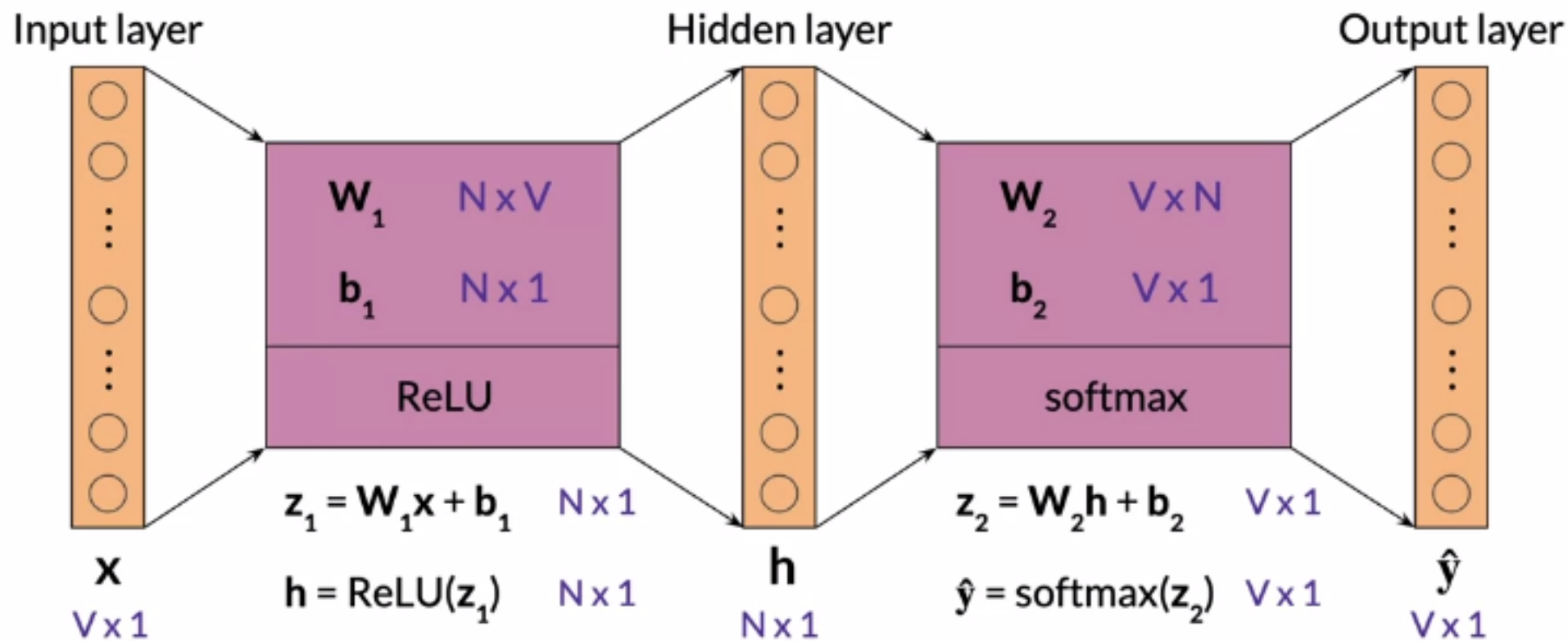


# Dimensions (single input)





# Dimensions (single input)



# Dimensions (single input)

Column vectors

$$\mathbf{z}_1 = \mathbf{W}_1 \mathbf{x} + \mathbf{b}_1$$
$$\mathbf{z}_1 = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{N \times 1} \quad \mathbf{W}_1 = \begin{pmatrix} \phantom{0} & \phantom{0} \\ \phantom{0} & \phantom{0} \end{pmatrix}_{N \times V} \quad \mathbf{x} = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{V \times 1} \quad \mathbf{b}_1 = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{N \times 1}$$

# Dimensions (single input)

Column vectors

$$\mathbf{z}_1 = \mathbf{W}_1 \mathbf{x} + \mathbf{b}_1$$
$$\mathbf{z}_1 = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{N \times 1} \quad \mathbf{W}_1 = \begin{pmatrix} \phantom{0} & \phantom{0} \\ \phantom{0} & \phantom{0} \end{pmatrix}_{N \times V} \quad \mathbf{x} = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{V \times 1} \quad \mathbf{b}_1 = \begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}_{N \times 1}$$

# Dimensions (single input)

Column vectors

$$\mathbf{z}_1 = \mathbf{W}_1 \mathbf{x} + \mathbf{b}_1 \quad \mathbf{z}_1 = \begin{pmatrix} \\ \\ \end{pmatrix}_{N \times 1} \quad \mathbf{W}_1 = \begin{pmatrix} N \times V \end{pmatrix} \quad \mathbf{x} = \begin{pmatrix} \\ \\ \end{pmatrix}_{V \times 1} \quad \mathbf{b}_1 = \begin{pmatrix} \\ \\ \end{pmatrix}_{N \times 1}$$

Row vectors

$$\mathbf{z}_1 = \mathbf{x} \mathbf{W}_1^T + \mathbf{b}_1 \quad \mathbf{b}_1 = \begin{pmatrix} 1 \times N \end{pmatrix} \quad \mathbf{W}_1 = \begin{pmatrix} N \times V \end{pmatrix} \quad \mathbf{b}_1 = \begin{pmatrix} 1 \times N \end{pmatrix} \\ \mathbf{x} = \begin{pmatrix} 1 \times V \end{pmatrix}$$



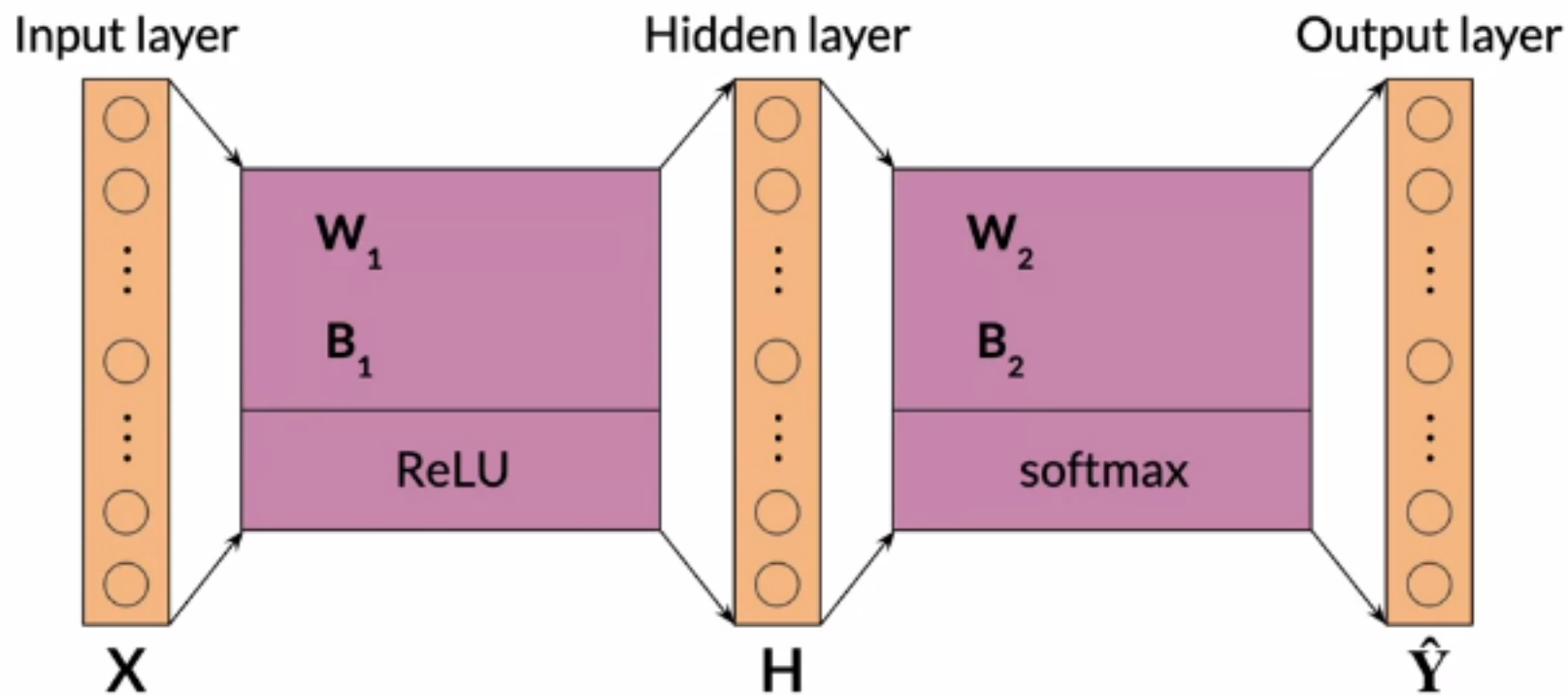
deeplearning.ai

# Architecture of the CBOW Model:

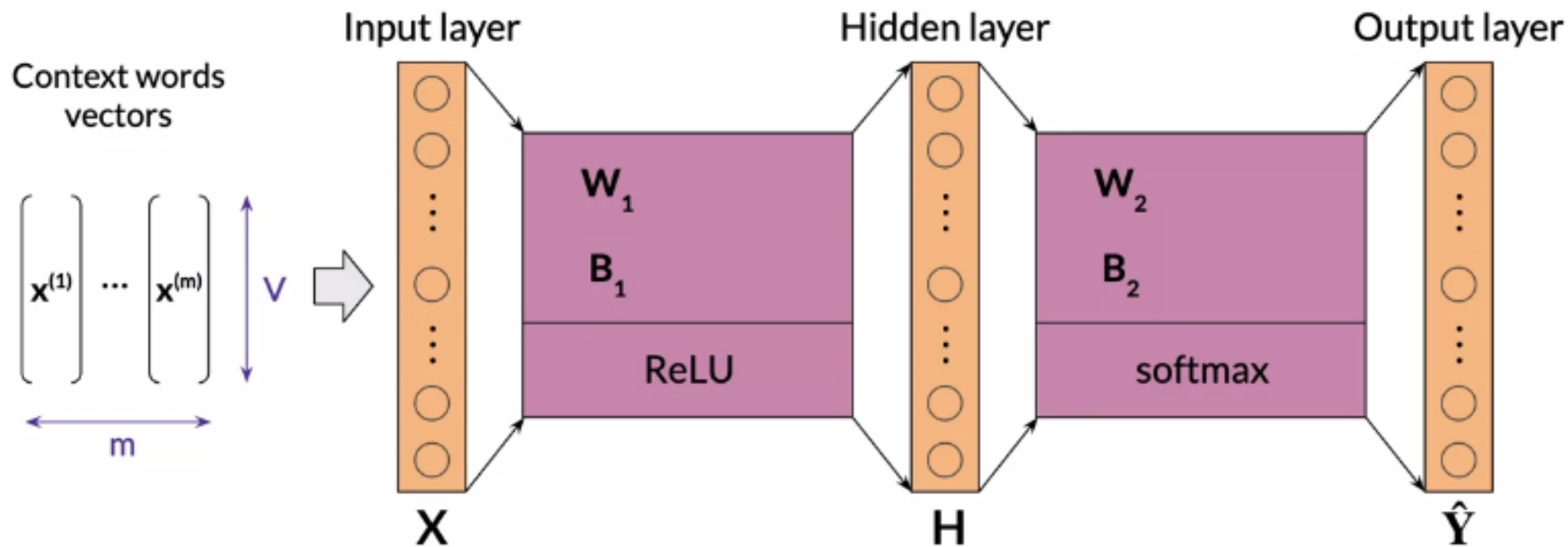
---

Dimensions 2

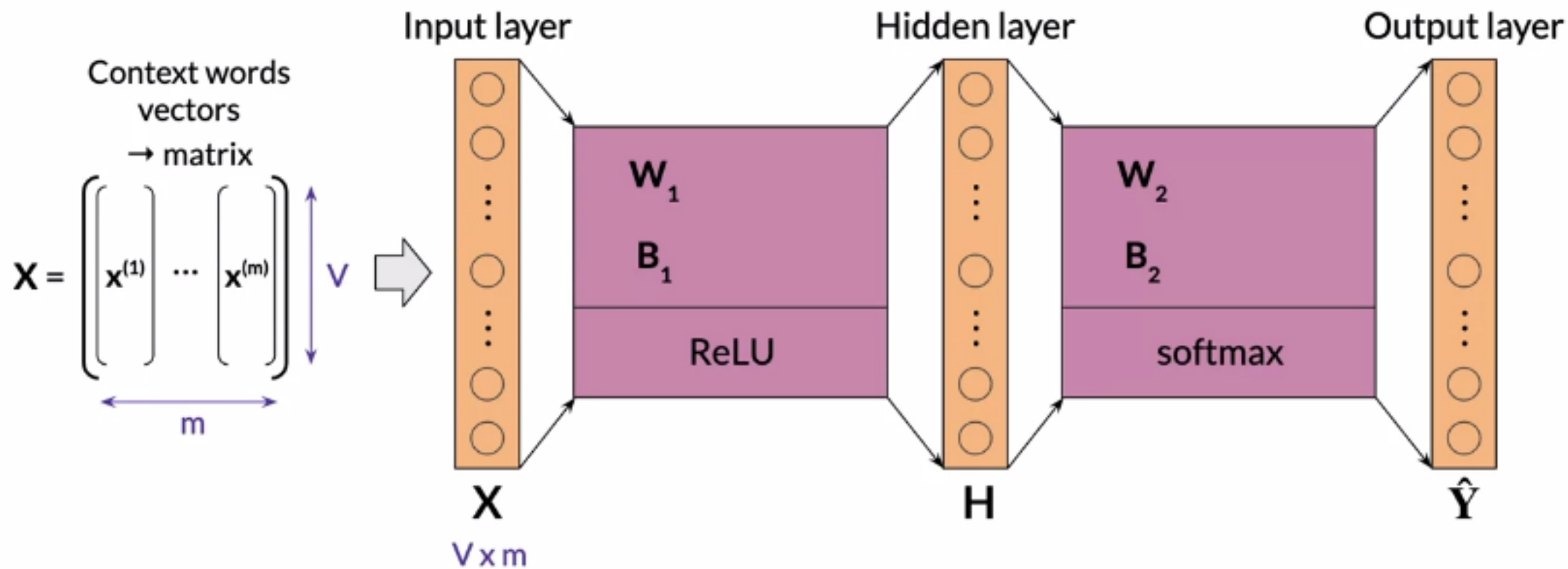
# Dimensions (batch input)



# Dimensions (batch input)

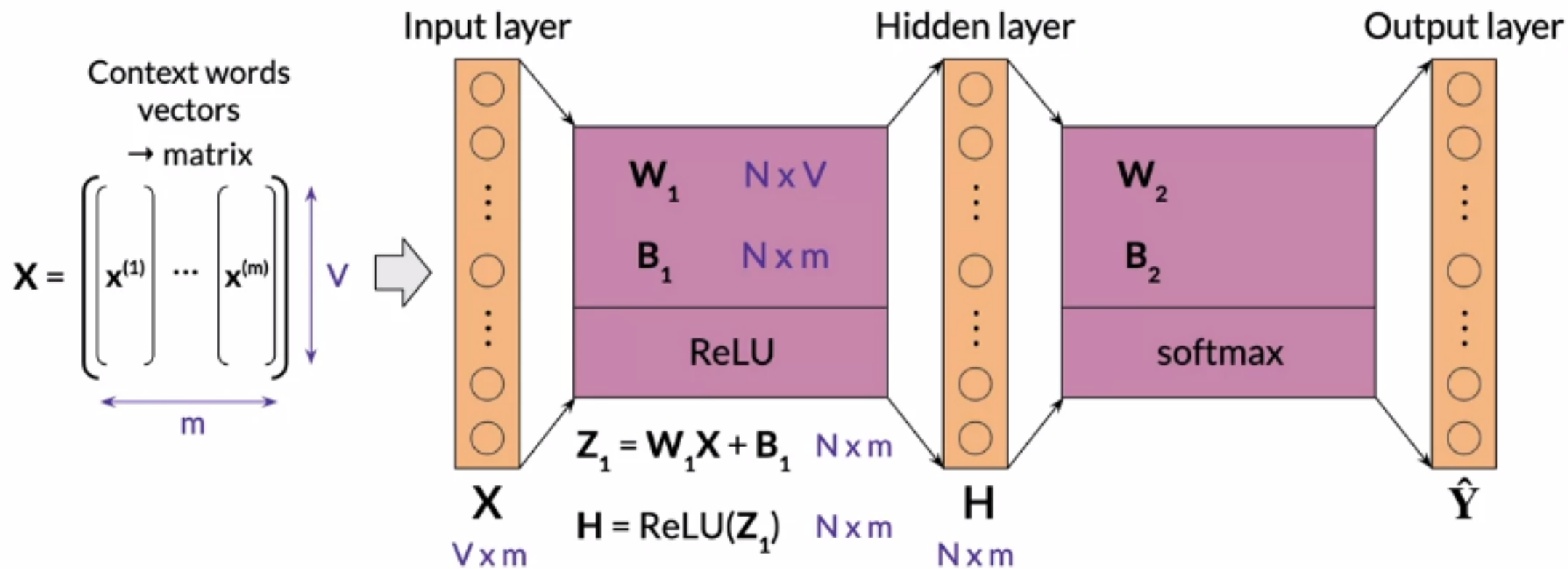


# Dimensions (batch input)

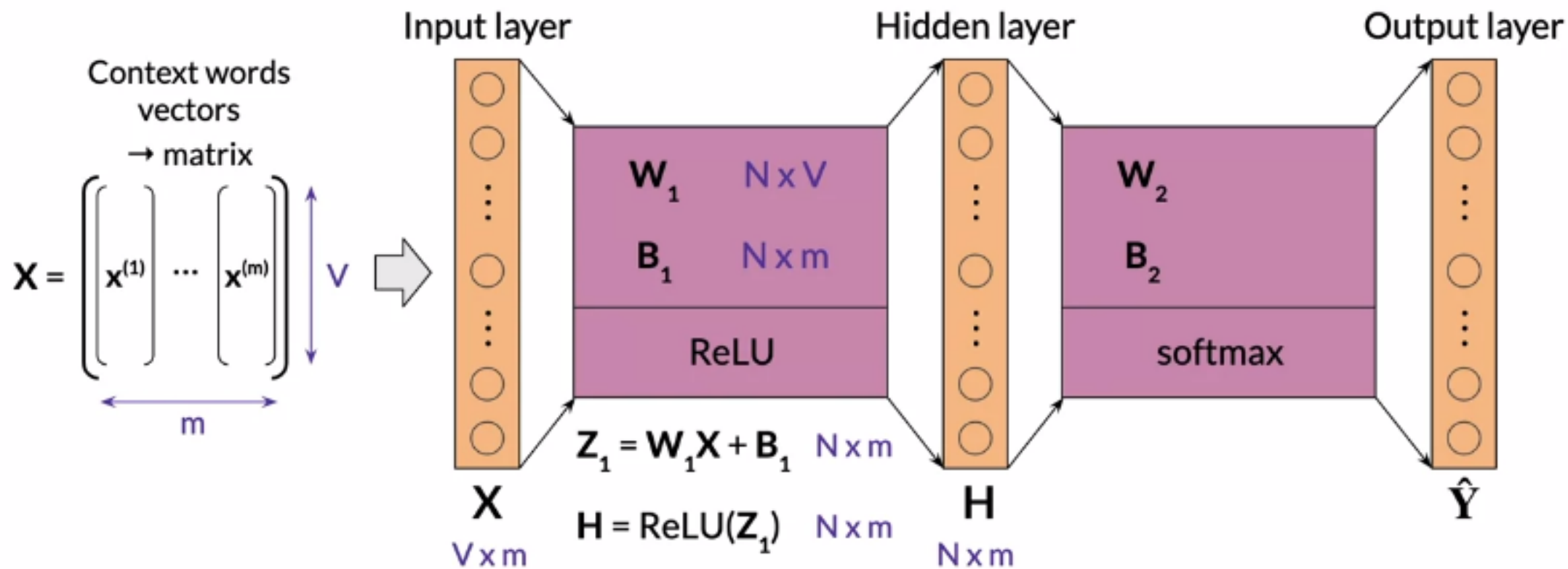




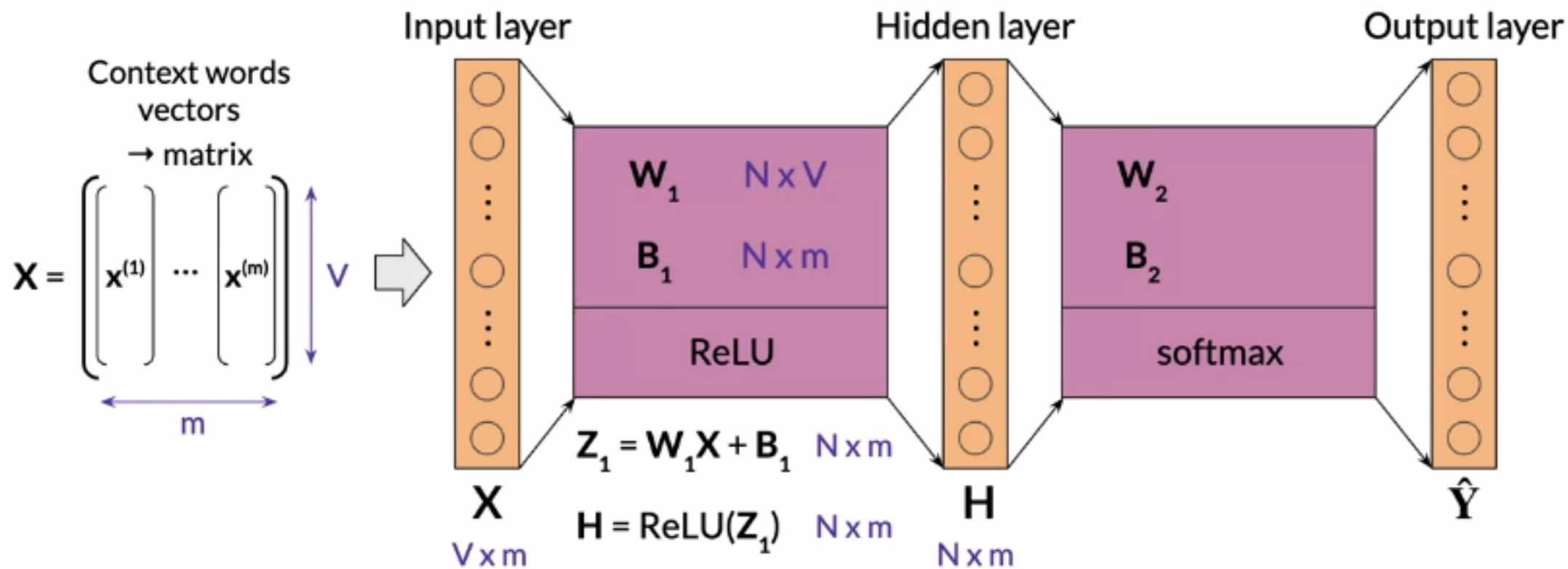
# Dimensions (batch input)



# Dimensions (batch input)

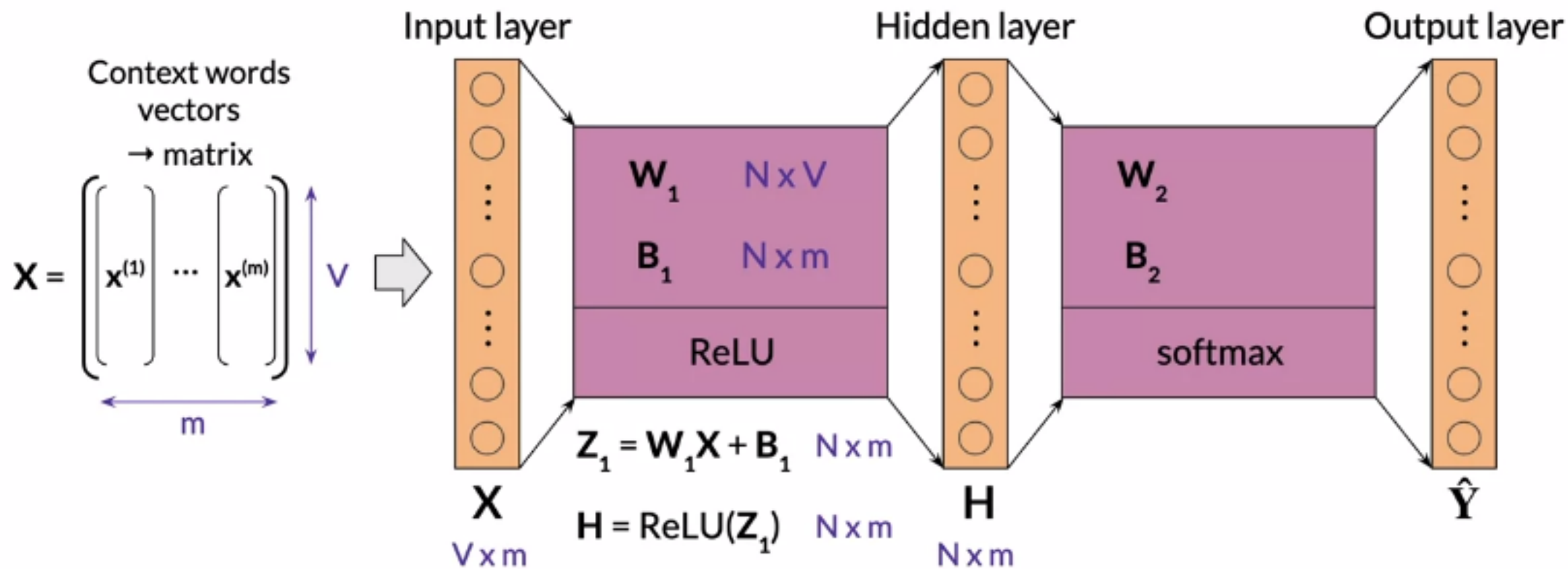


# Dimensions (batch input)



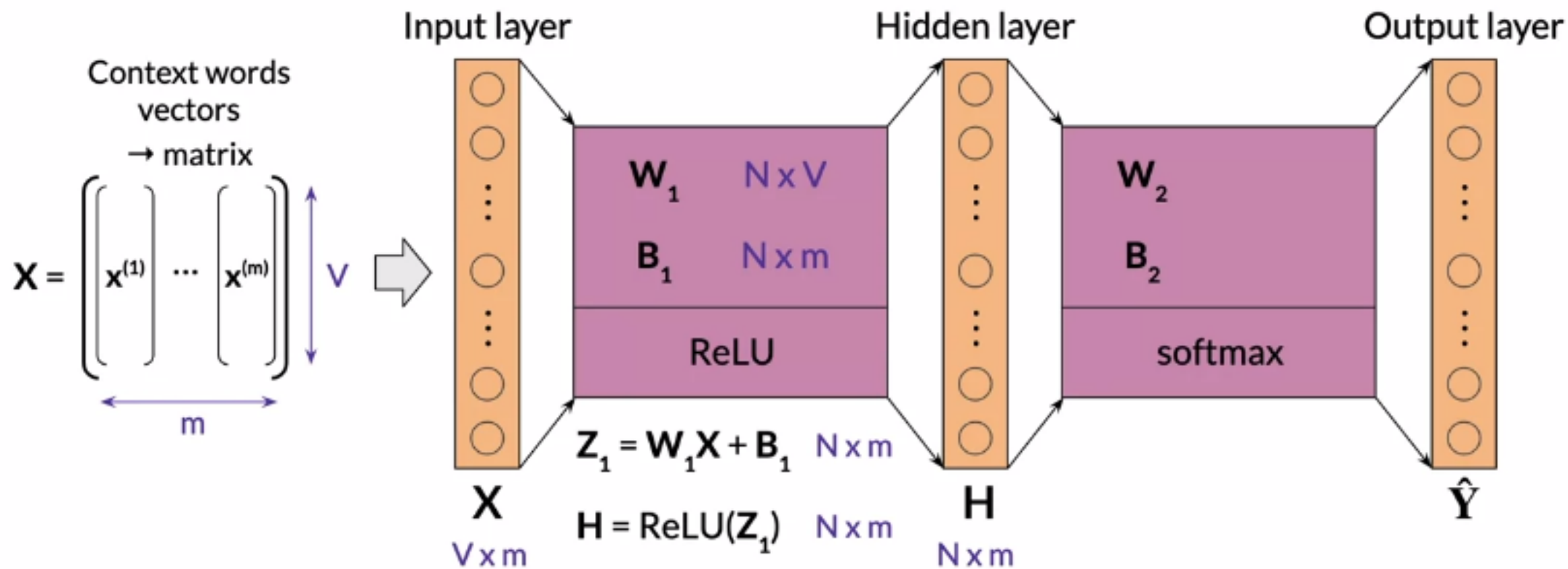
# Dimensions (batch input)

$$\begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \rightarrow \mathbf{B}_1 = \begin{bmatrix} \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \end{bmatrix} \begin{matrix} \updownarrow N \\ \leftarrow m \rightarrow \end{matrix}$$



# Dimensions (batch input)

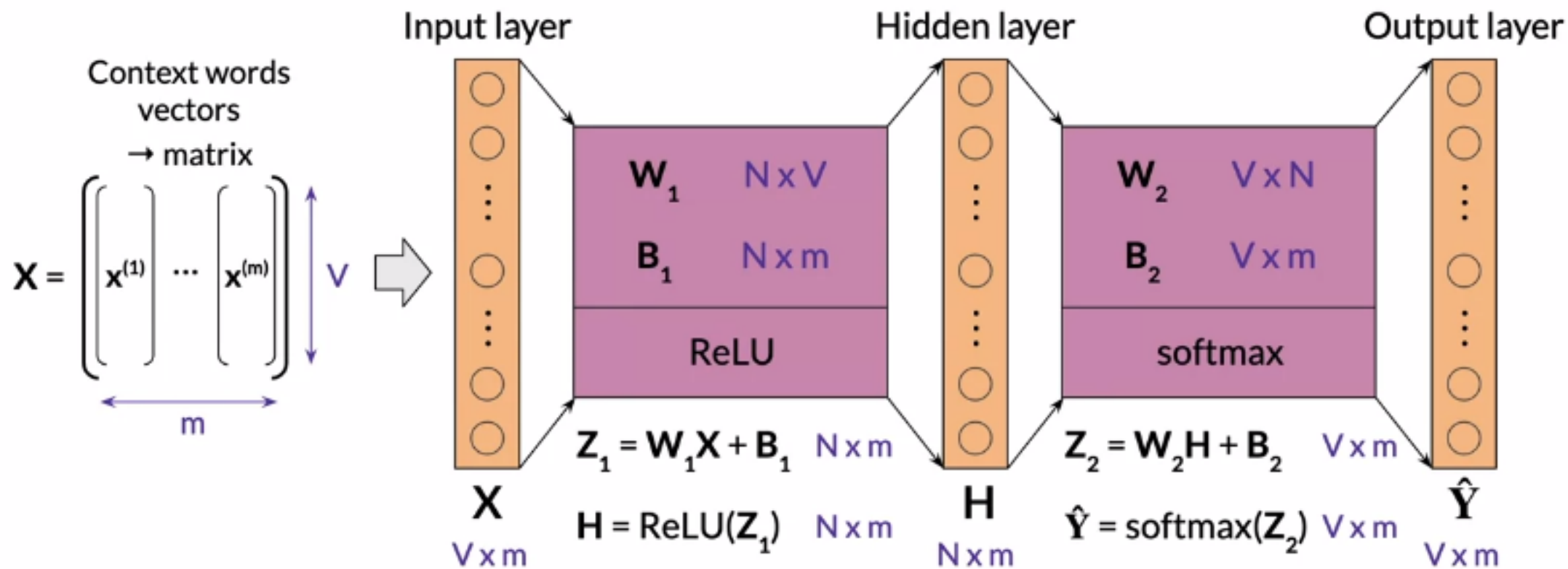
$$\begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \rightarrow \mathbf{B}_1 = \begin{bmatrix} \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \\ \underbrace{\hspace{1cm}}_m \end{bmatrix} \begin{matrix} \updownarrow N \\ \text{broadcasting} \end{matrix}$$



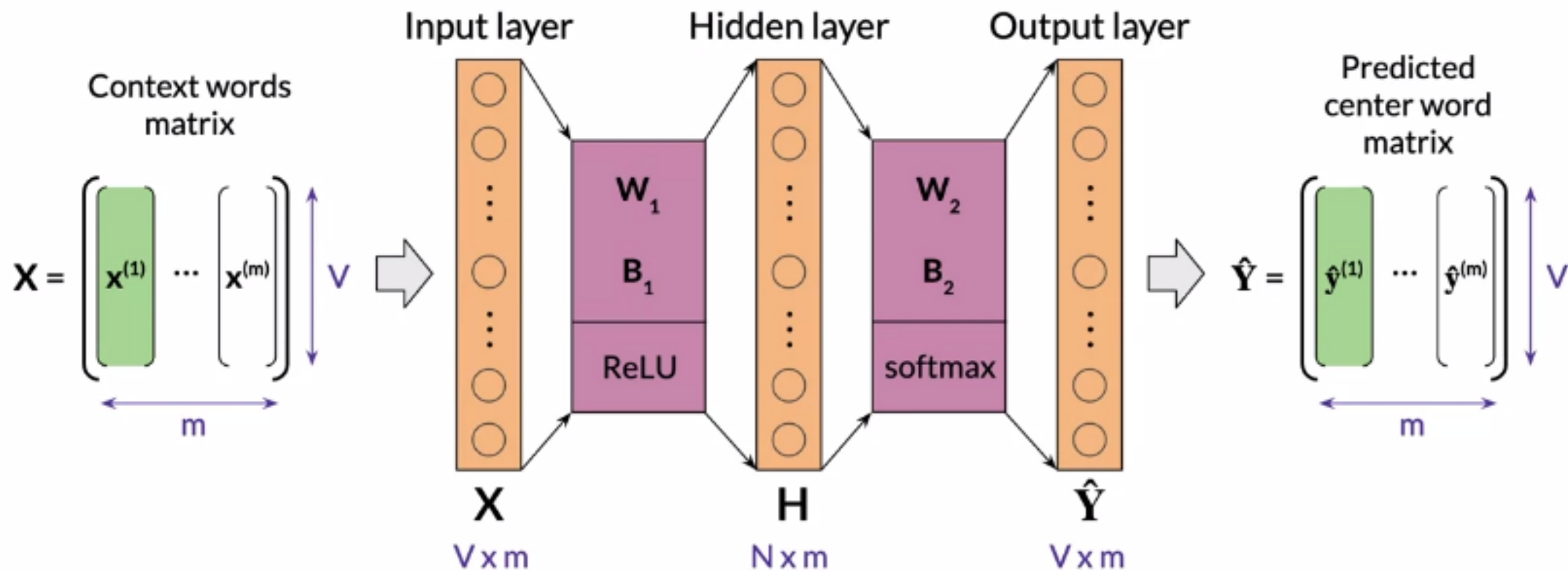
# Dimensions (batch input)

$$\begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \rightarrow \mathbf{B}_1 = \begin{bmatrix} \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{b}_1 \end{bmatrix} \end{bmatrix} \begin{matrix} \updownarrow N \\ \text{broadcasting} \end{matrix}$$

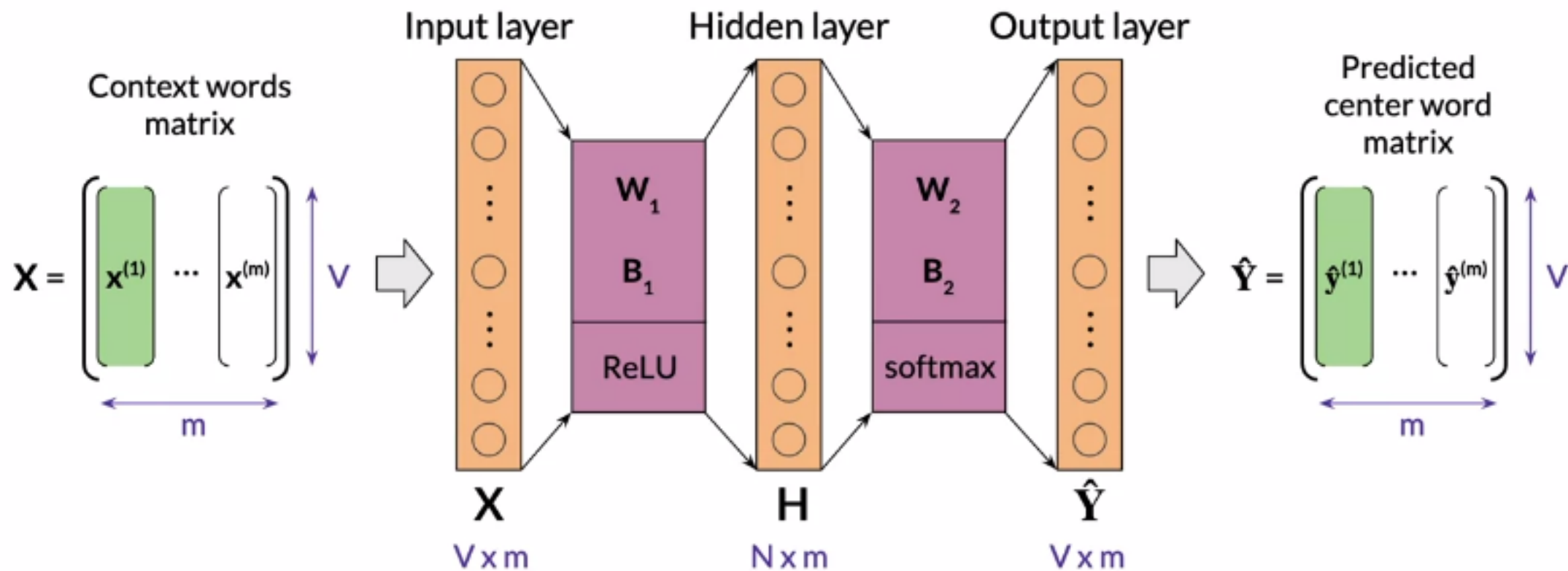
$\xleftrightarrow{m}$



# Dimensions (batch input)



# Dimensions (batch input)

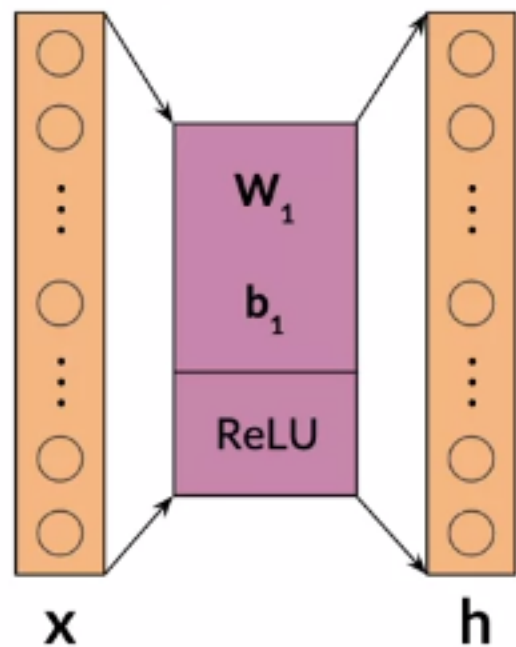




# Rectified Linear Unit (ReLU)

# Rectified Linear Unit (ReLU)

Input layer      Hidden layer



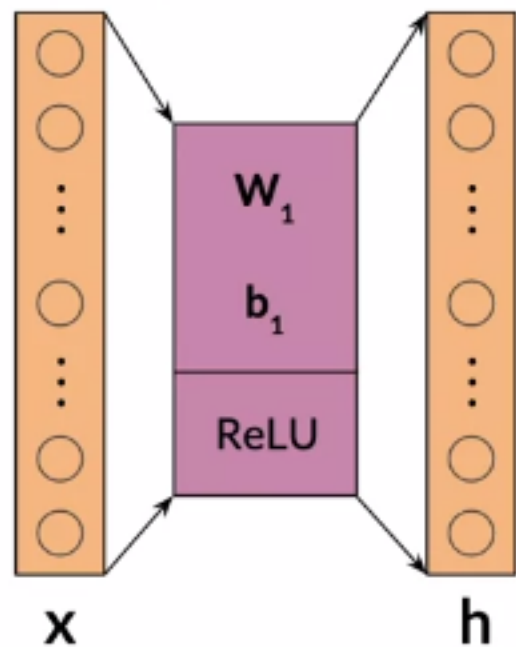
$$z_1 = W_1 x + b_1$$

$$h = \text{ReLU}(z_1)$$

# Rectified Linear Unit (ReLU)

$$\text{ReLU}(x) = \max(0, x)$$

Input layer      Hidden layer



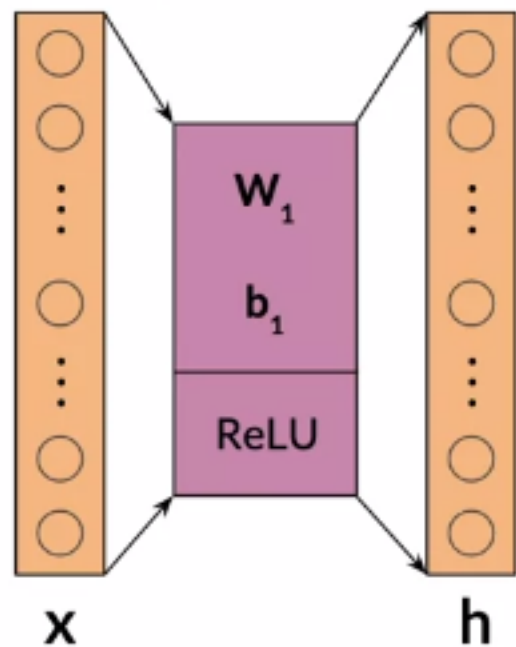
$$z_1 = W_1 x + b_1$$

$$h = \text{ReLU}(z_1)$$

# Rectified Linear Unit (ReLU)

$$\text{ReLU}(x) = \max(0, x)$$

Input layer      Hidden layer

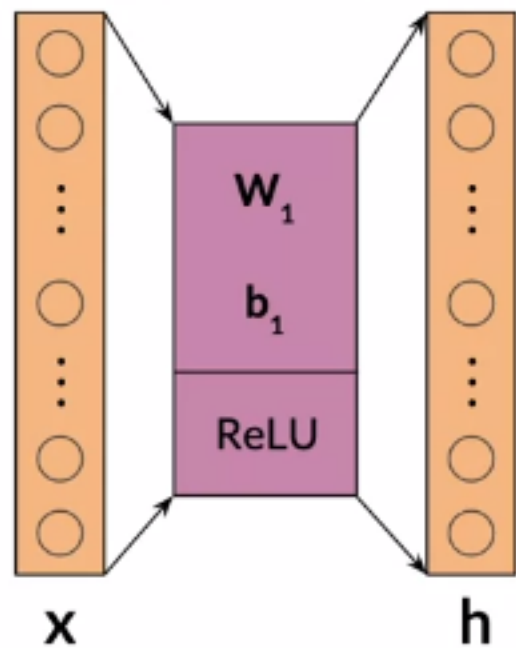


$$z_1 = W_1 x + b_1$$

$$h = \text{ReLU}(z_1)$$

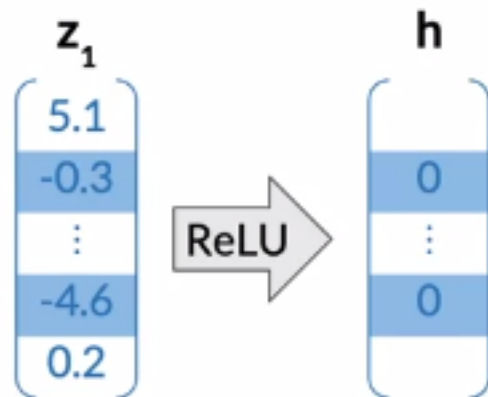
# Rectified Linear Unit (ReLU)

Input layer      Hidden layer

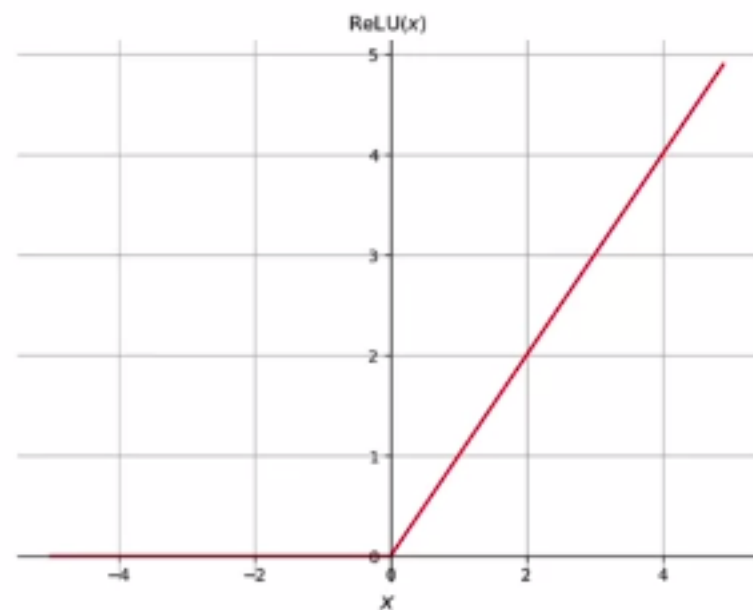


$$z_1 = W_1 x + b_1$$

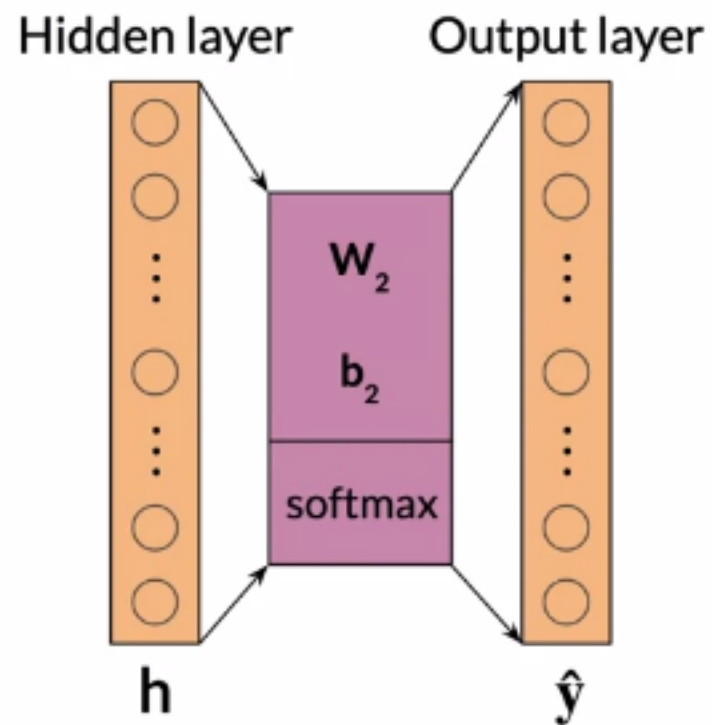
$$h = \text{ReLU}(z_1)$$



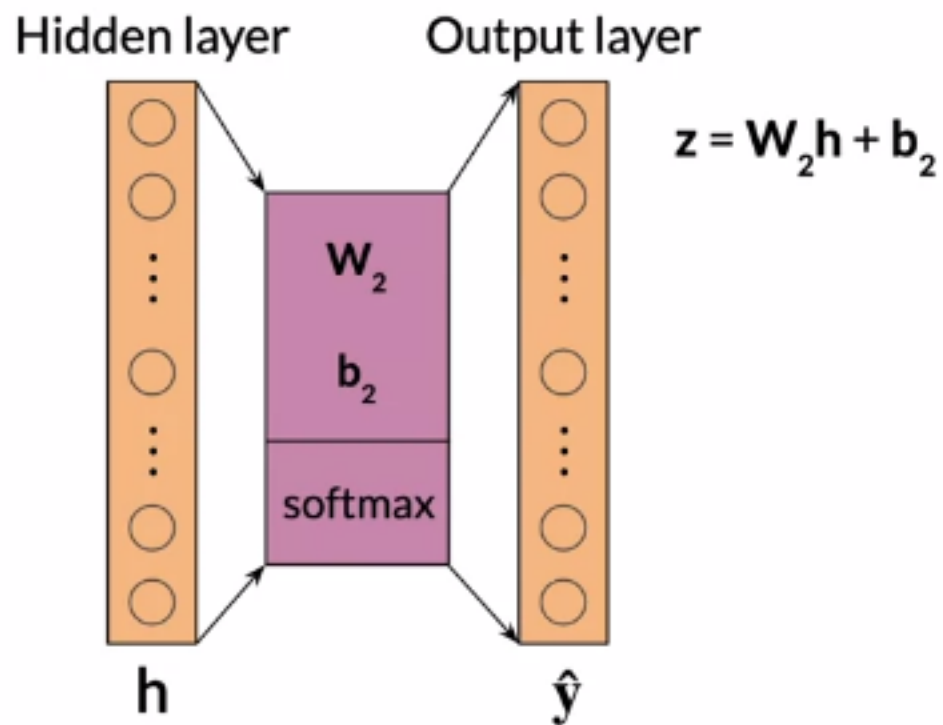
$$\text{ReLU}(x) = \max(0, x)$$



# Softmax



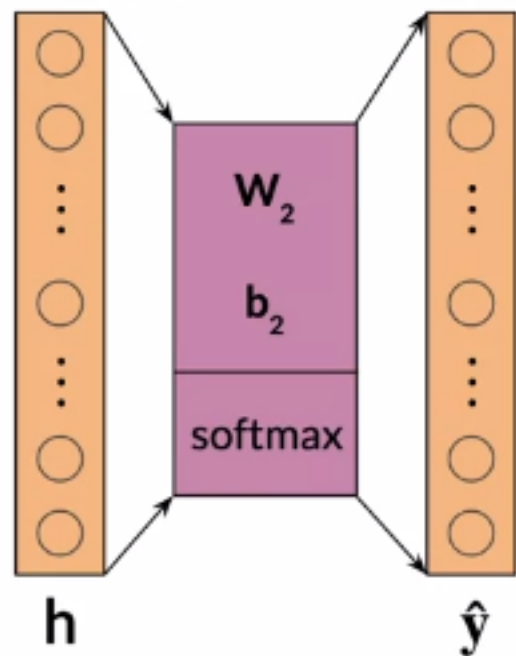
# Softmax



# Softmax

Hidden layer

Output layer



$$z = W_2 h + b_2$$

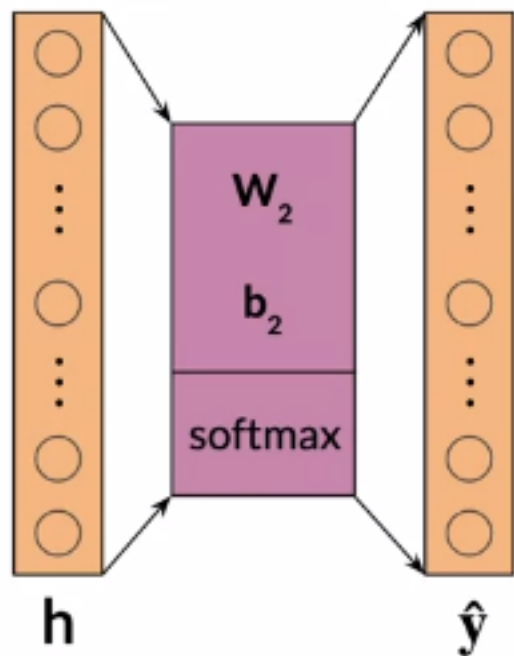
$$\hat{y} = \text{softmax}(z)$$



# Softmax

Hidden layer

Output layer



$$z = W_2 h + b_2$$

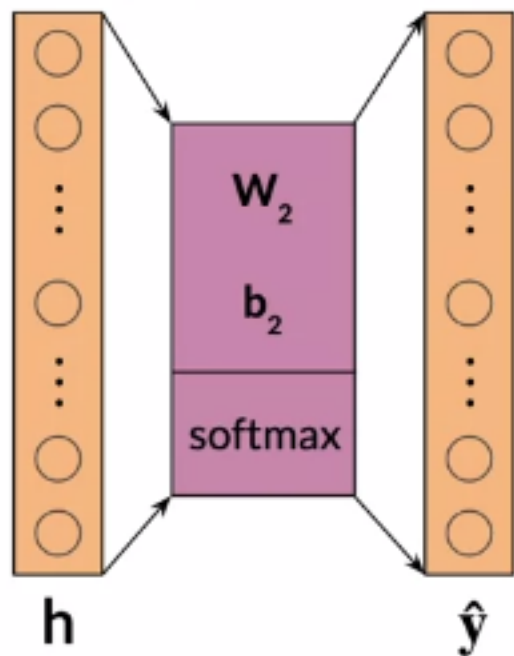
$$\hat{y} = \text{softmax}(z)$$

$$\begin{pmatrix} \end{pmatrix} \in \mathbb{R}^K \xrightarrow{\text{softmax}} \begin{pmatrix} \end{pmatrix} \in [0, 1]^K$$

# Softmax

Hidden layer

Output layer



$$z = W_2 h + b_2$$

$$\hat{y} = \text{softmax}(z)$$

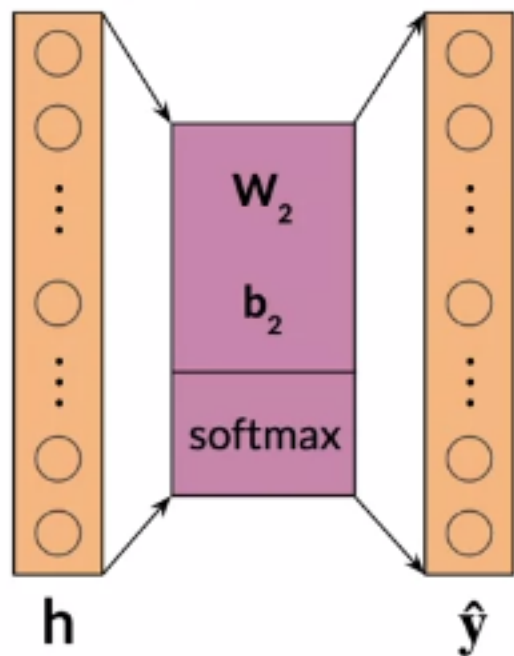
$$\begin{pmatrix} \end{pmatrix} \in \mathbb{R}^K \xrightarrow{\text{softmax}} \begin{pmatrix} \end{pmatrix} \in [0, 1]^K$$

$\downarrow$   
 $\Sigma = 1$

# Softmax

Hidden layer

Output layer



$$z = W_2 h + b_2$$

$$\hat{y} = \text{softmax}(z)$$

$$\begin{pmatrix} \vdots \\ \end{pmatrix} \in \mathbb{R}^K \xrightarrow{\text{softmax}} \begin{pmatrix} \vdots \\ \end{pmatrix} \in [0, 1]^K$$

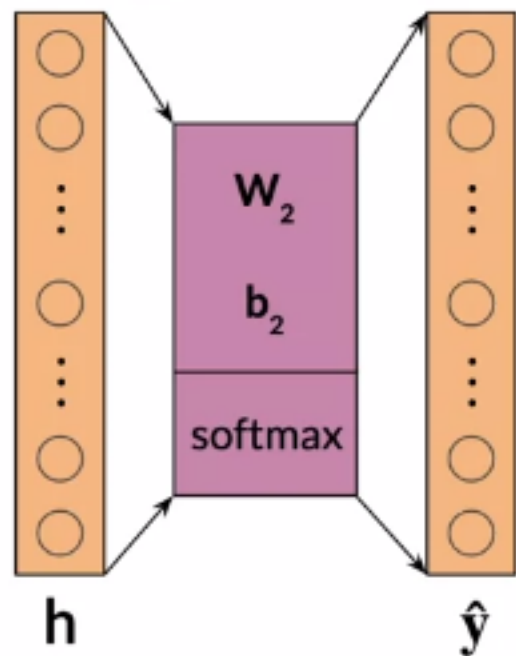
$\downarrow$   
 $\Sigma = 1$

~probabilities

# Softmax

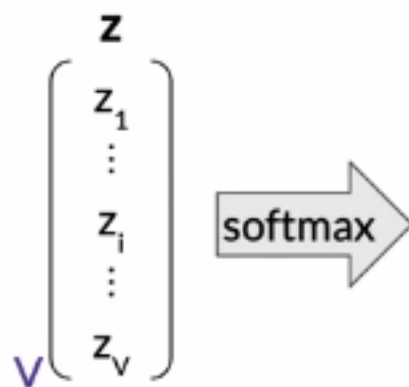
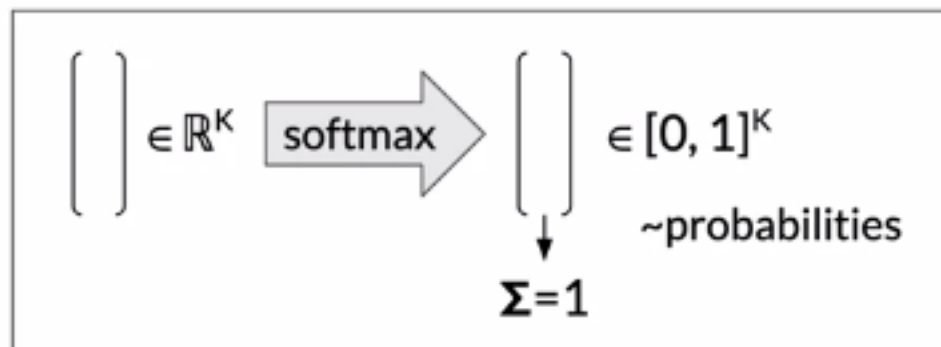
Hidden layer

Output layer



$$z = W_2 h + b_2$$

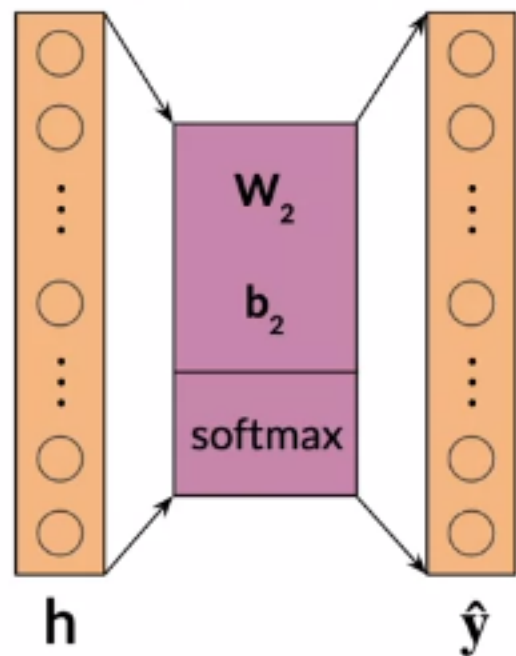
$$\hat{y} = \text{softmax}(z)$$



# Softmax

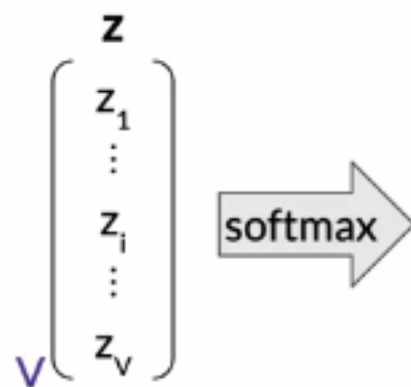
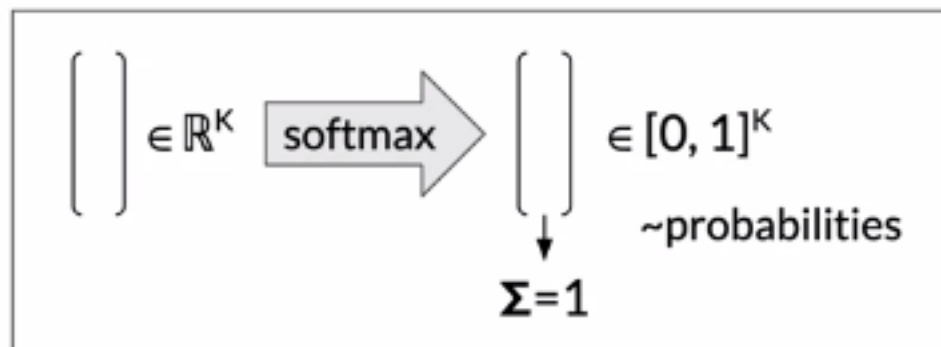
Hidden layer

Output layer



$$z = W_2 h + b_2$$

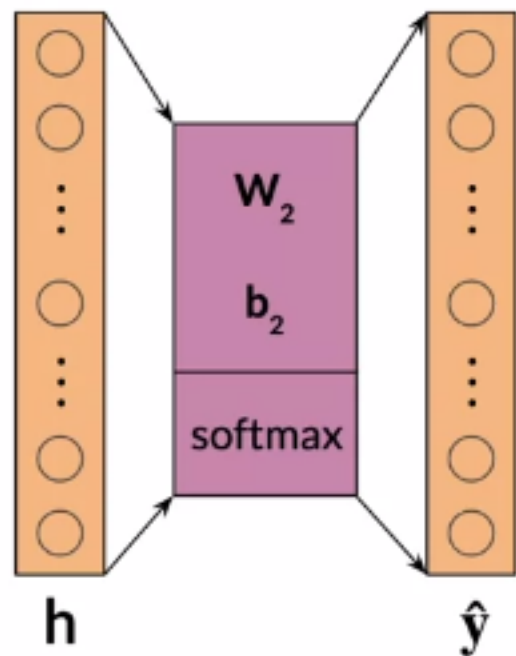
$$\hat{y} = \text{softmax}(z)$$



# Softmax

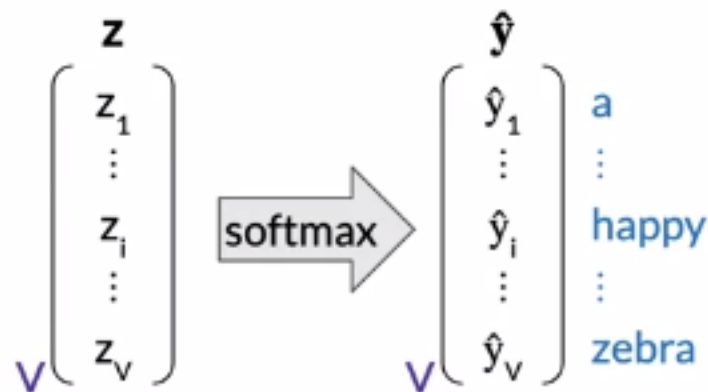
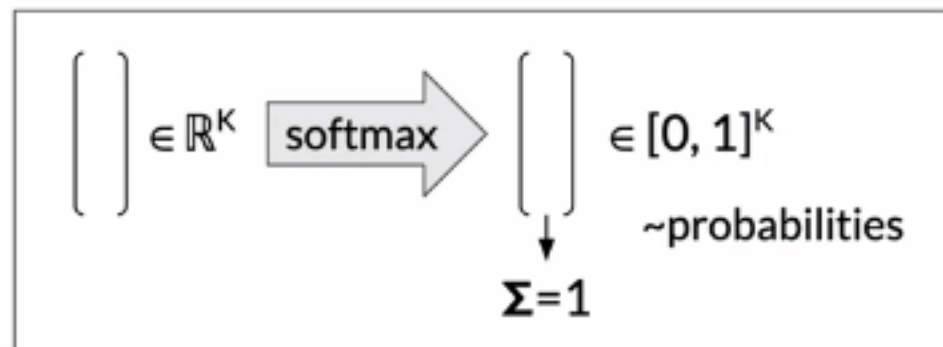
Hidden layer

Output layer



$$z = W_2 h + b_2$$

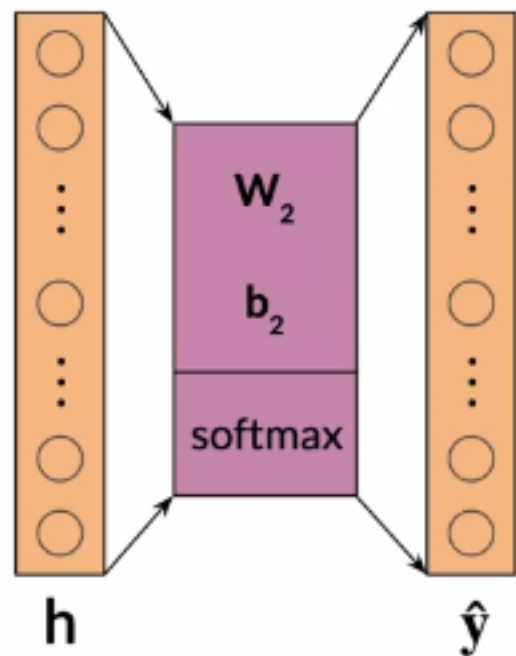
$$\hat{y} = \text{softmax}(z)$$



# Softmax

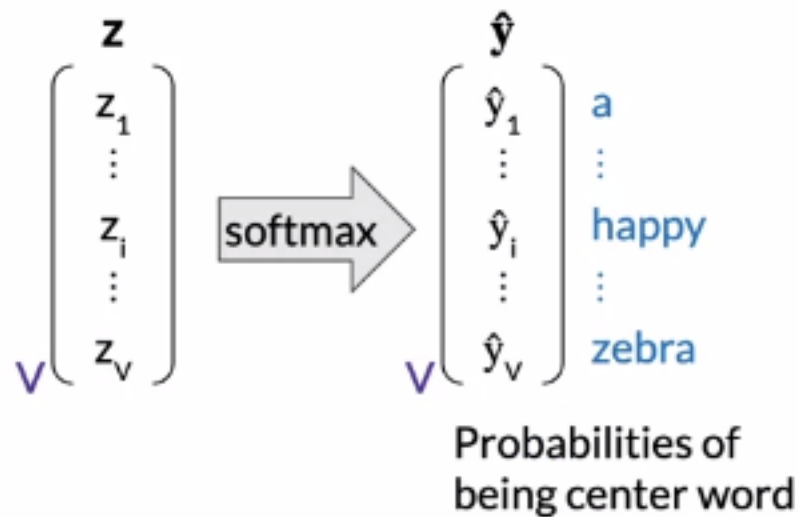
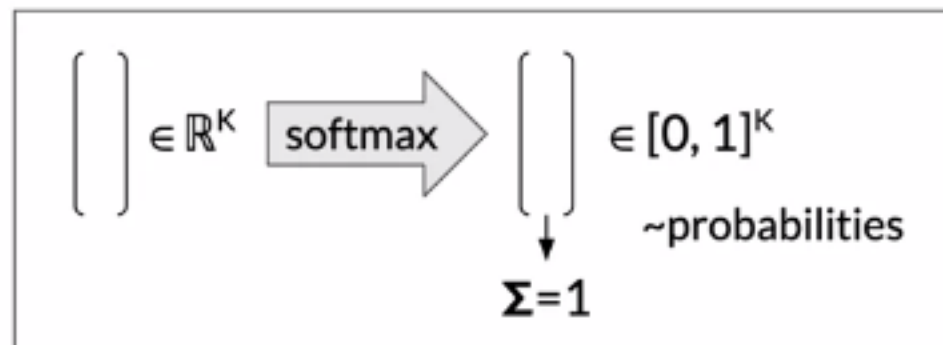
Hidden layer

Output layer



$$\mathbf{z} = \mathbf{W}_2 \mathbf{h} + \mathbf{b}_2$$

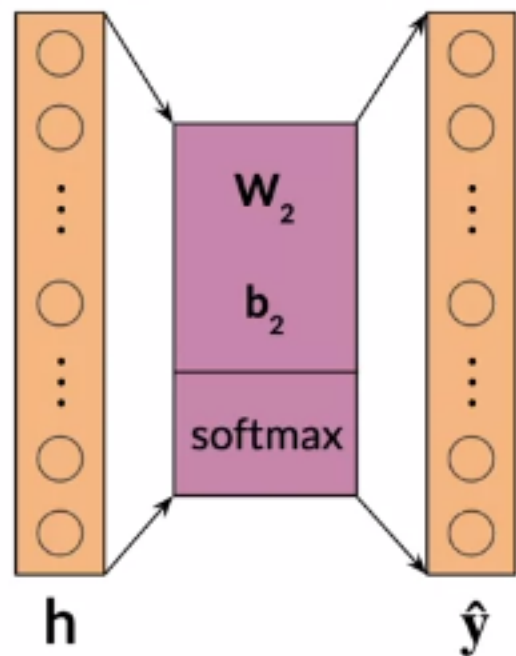
$$\hat{\mathbf{y}} = \text{softmax}(\mathbf{z})$$



# Softmax

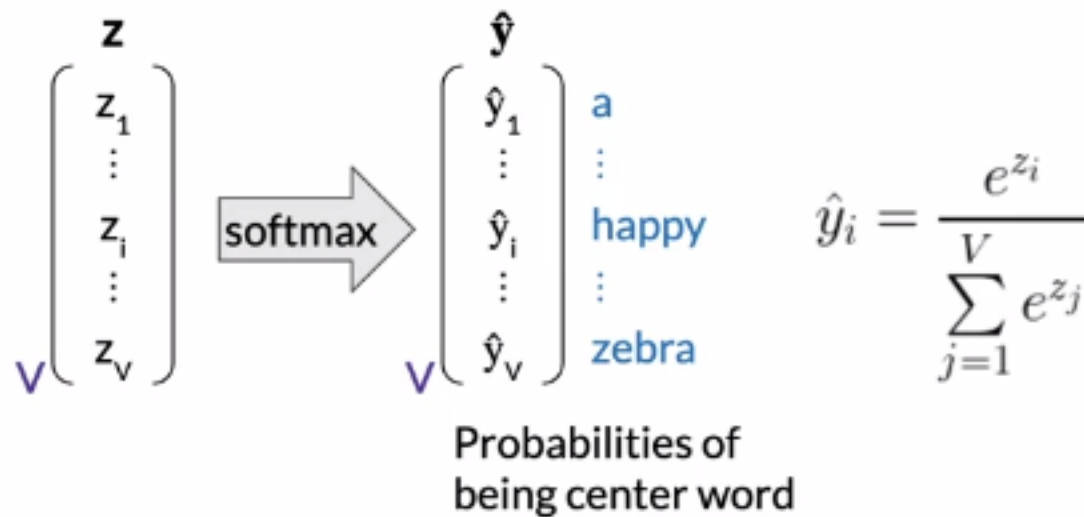
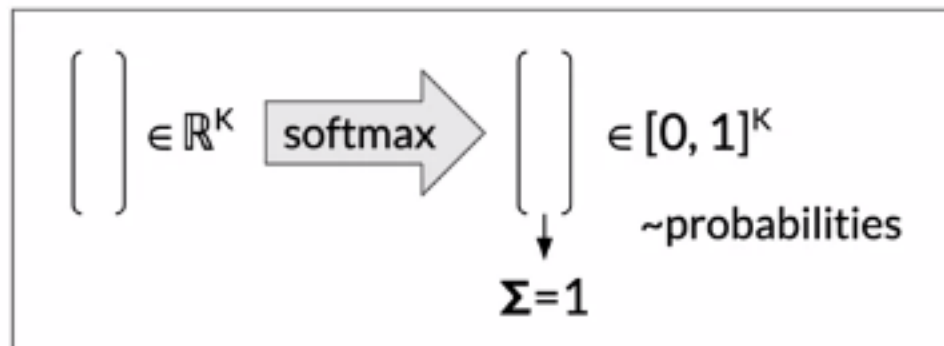
Hidden layer

Output layer



$$\mathbf{z} = \mathbf{W}_2 \mathbf{h} + \mathbf{b}_2$$

$$\hat{\mathbf{y}} = \text{softmax}(\mathbf{z})$$

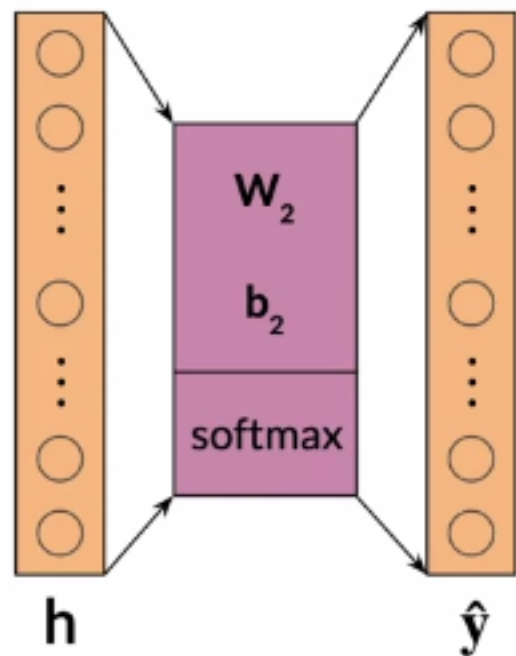




# Softmax

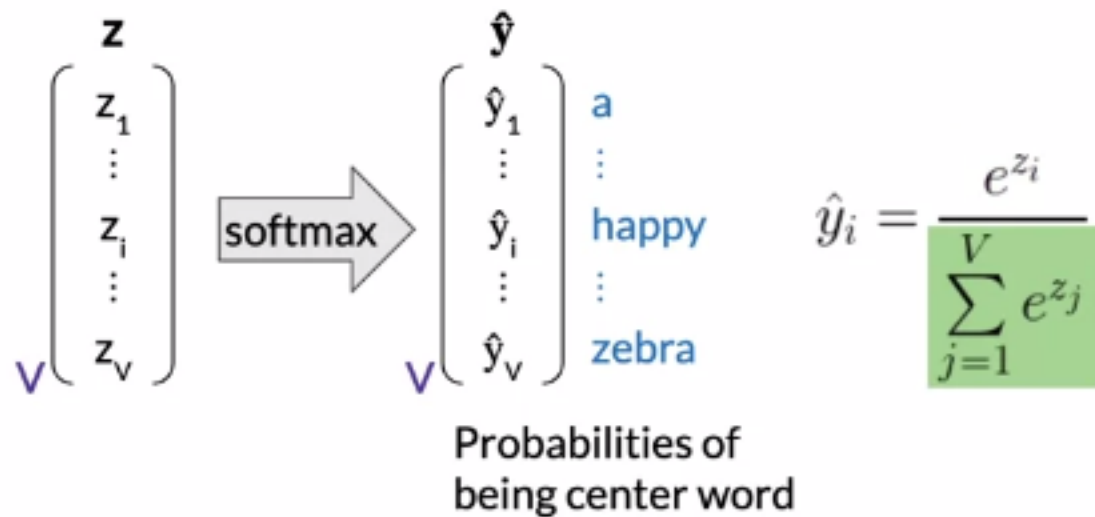
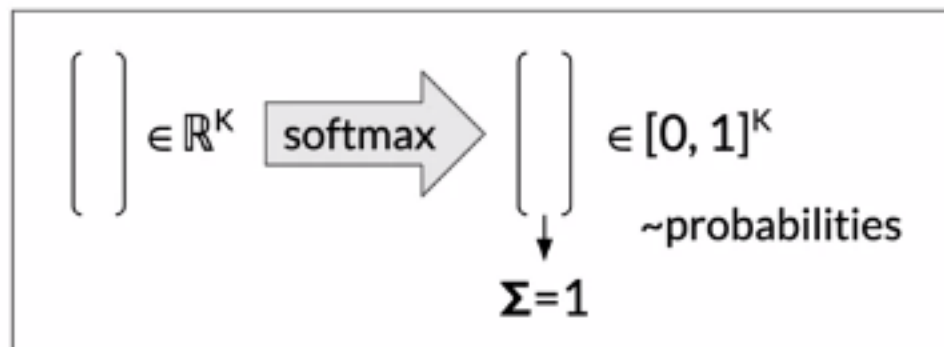
Hidden layer

Output layer



$$\mathbf{z} = \mathbf{W}_2 \mathbf{h} + \mathbf{b}_2$$

$$\hat{\mathbf{y}} = \text{softmax}(\mathbf{z})$$




## Softmax: example

$$\mathbf{z} = \begin{pmatrix} 9 \\ 8 \\ 11 \\ 10 \\ 8.5 \end{pmatrix}$$

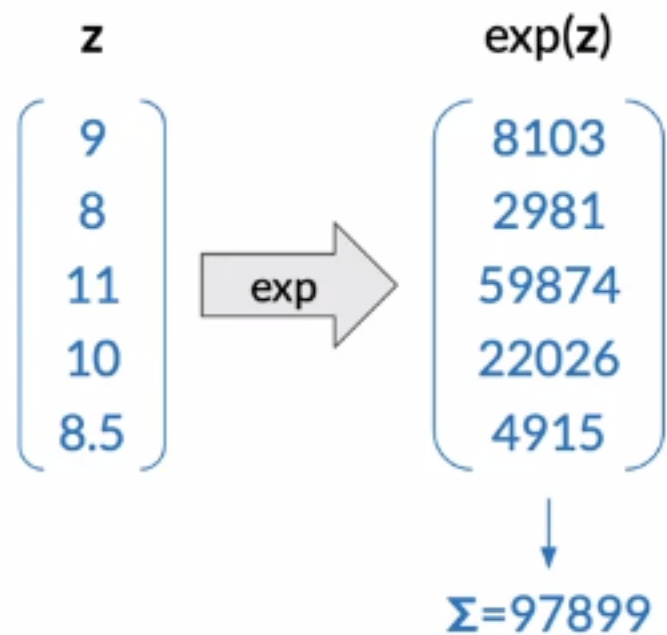
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

## Softmax: example

z		exp(z)
9	 exp	8103
8		2981
11		59874
10		22026
8.5		4915

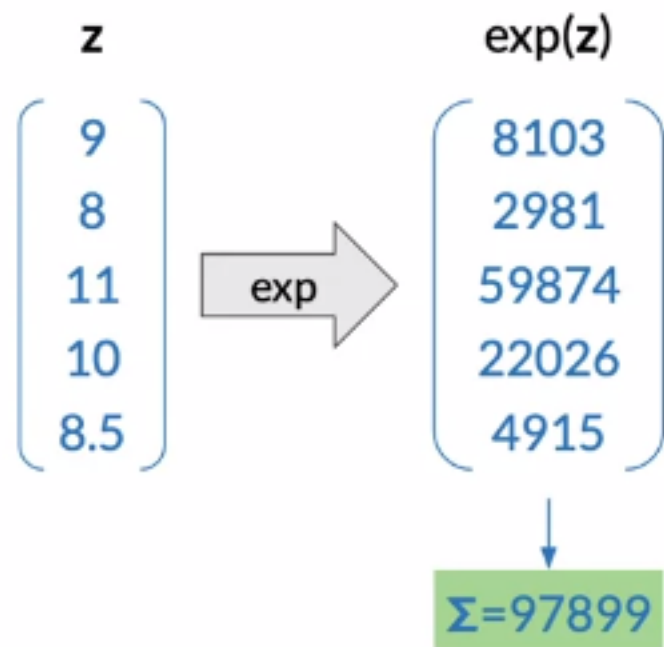
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

## Softmax: example



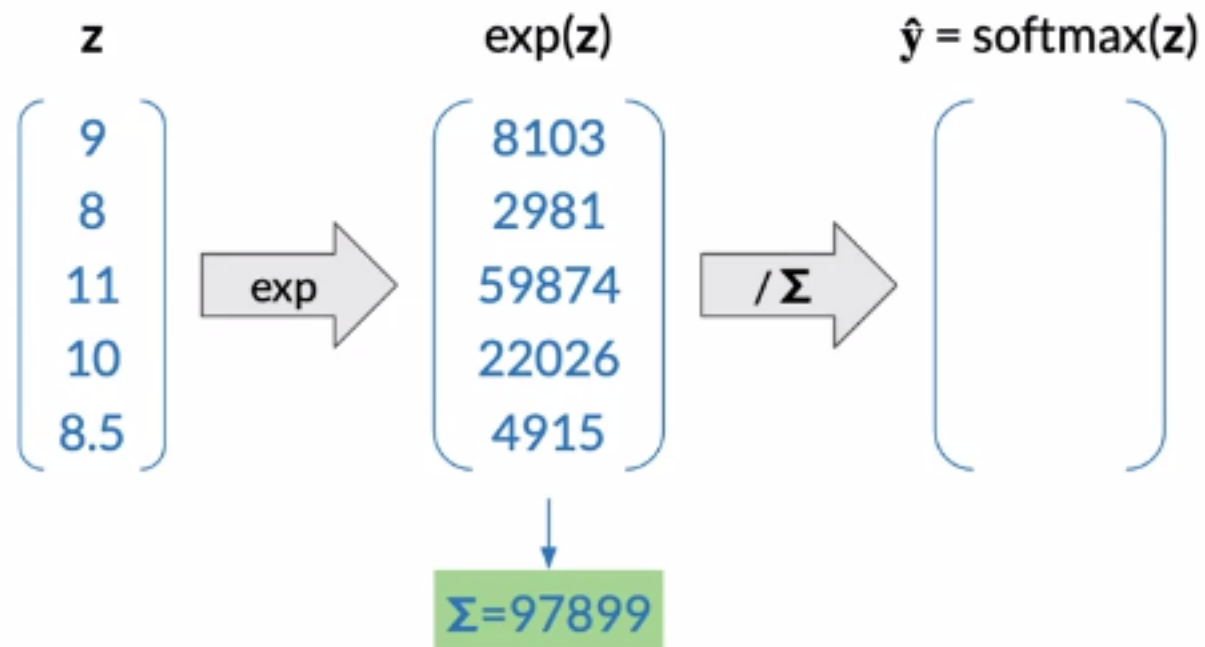
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



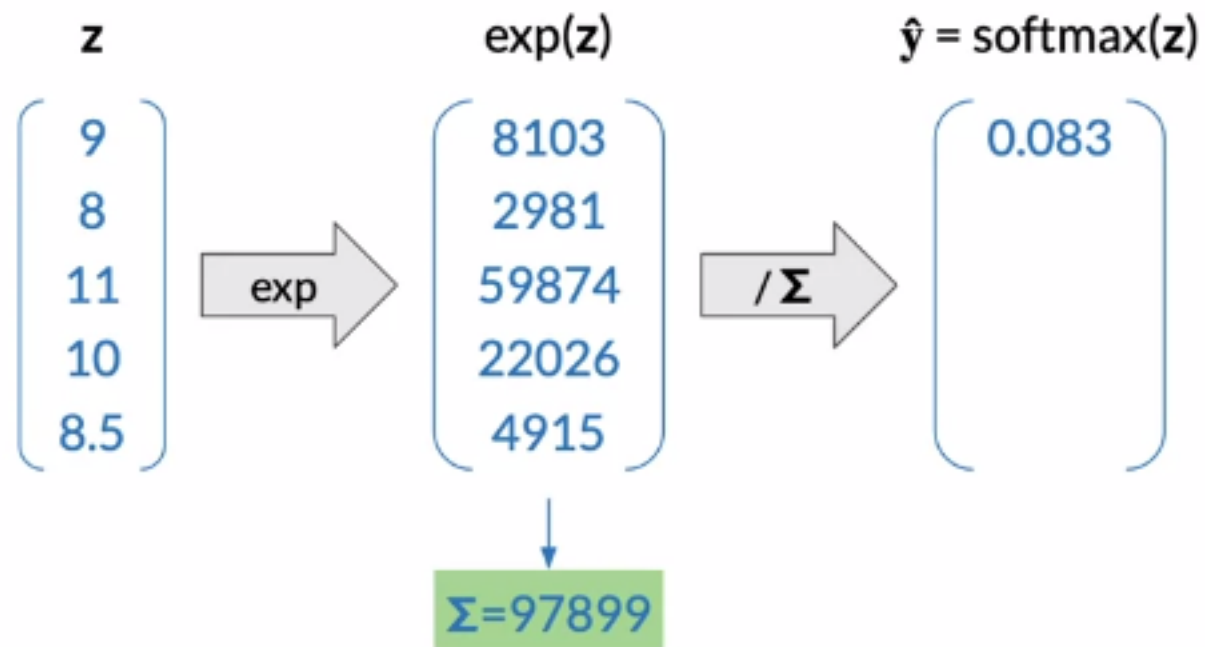
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



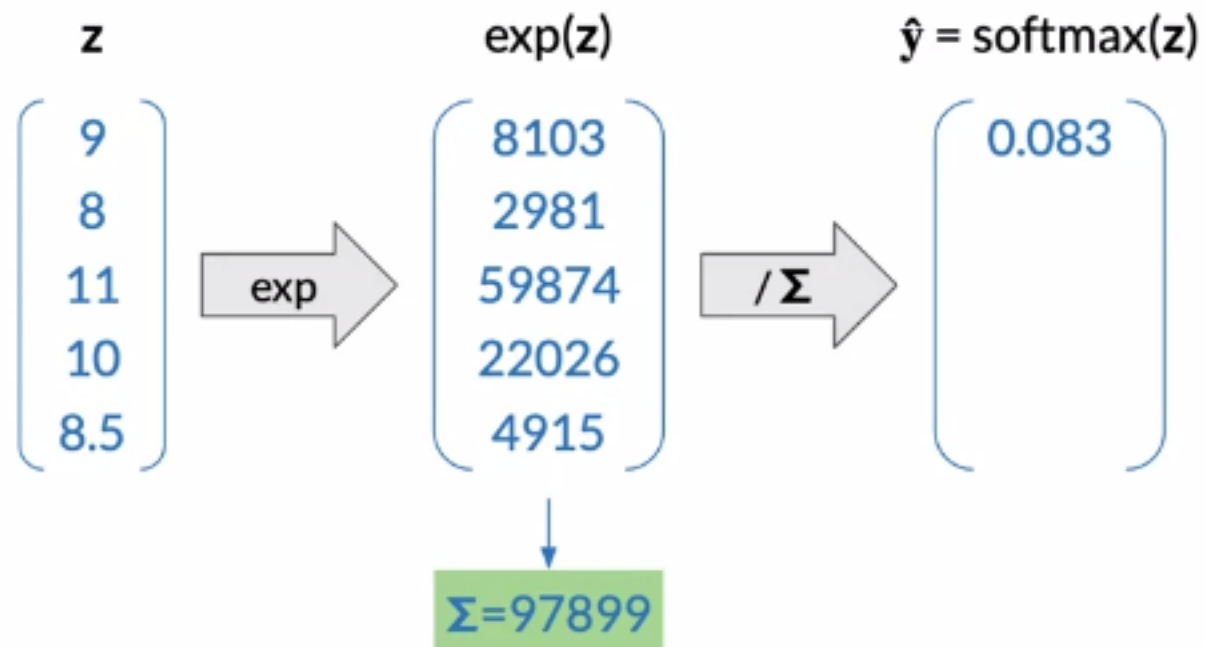
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

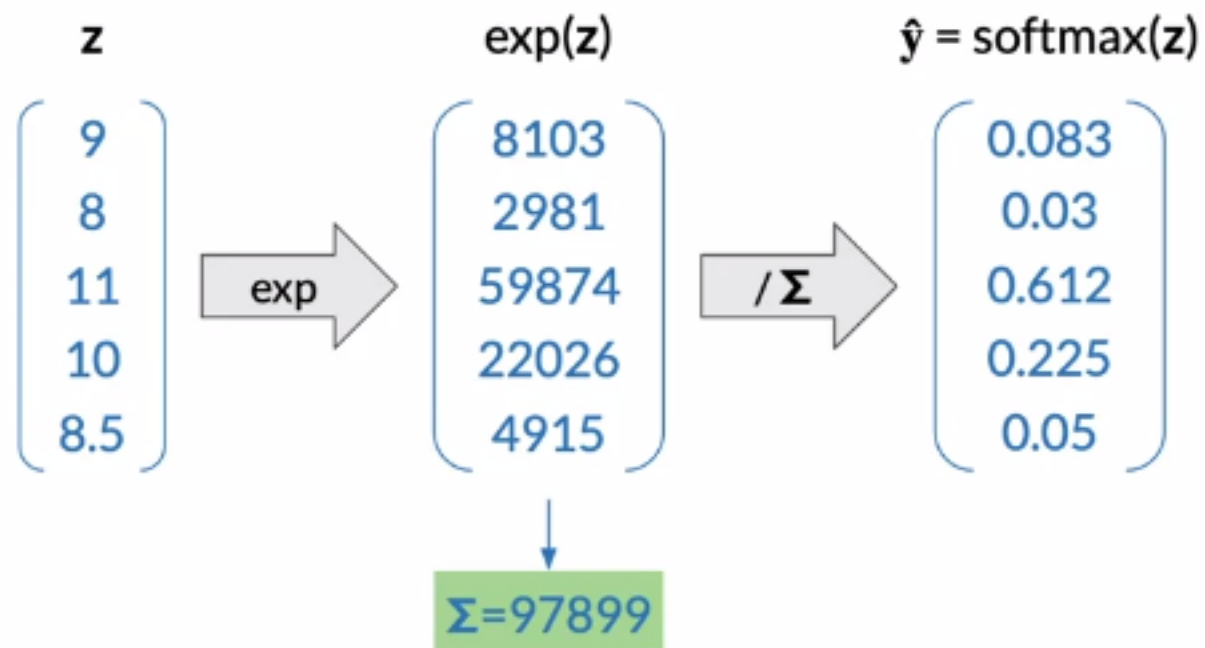
# Softmax: example



$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

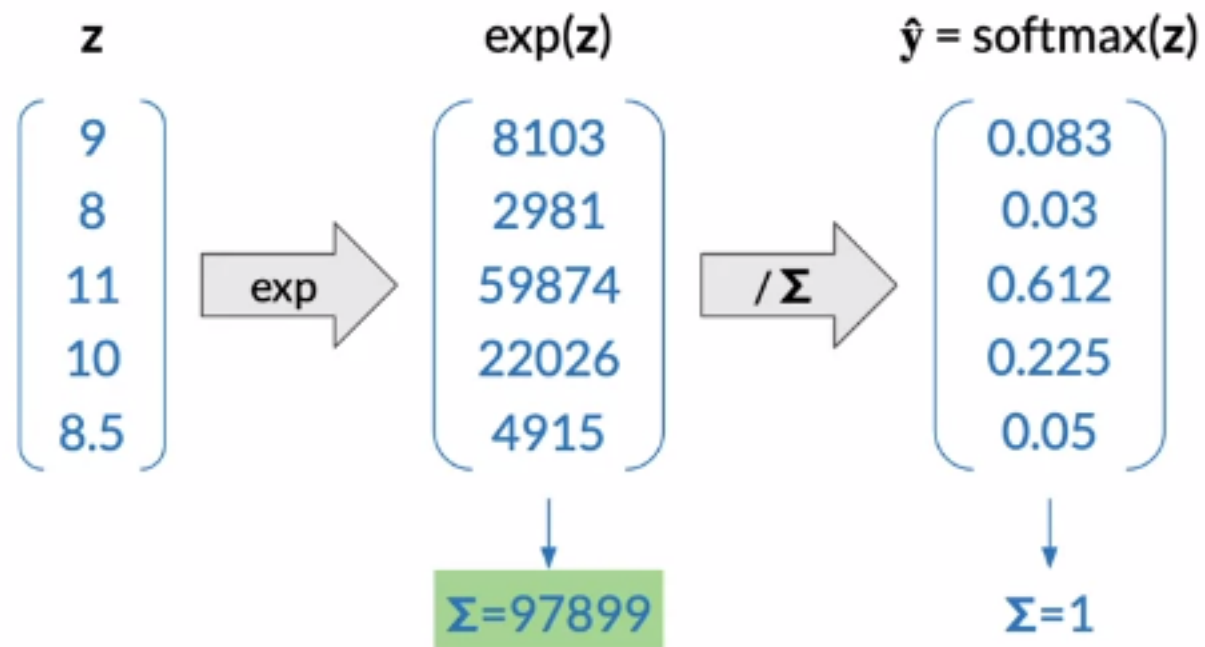


# Softmax: example



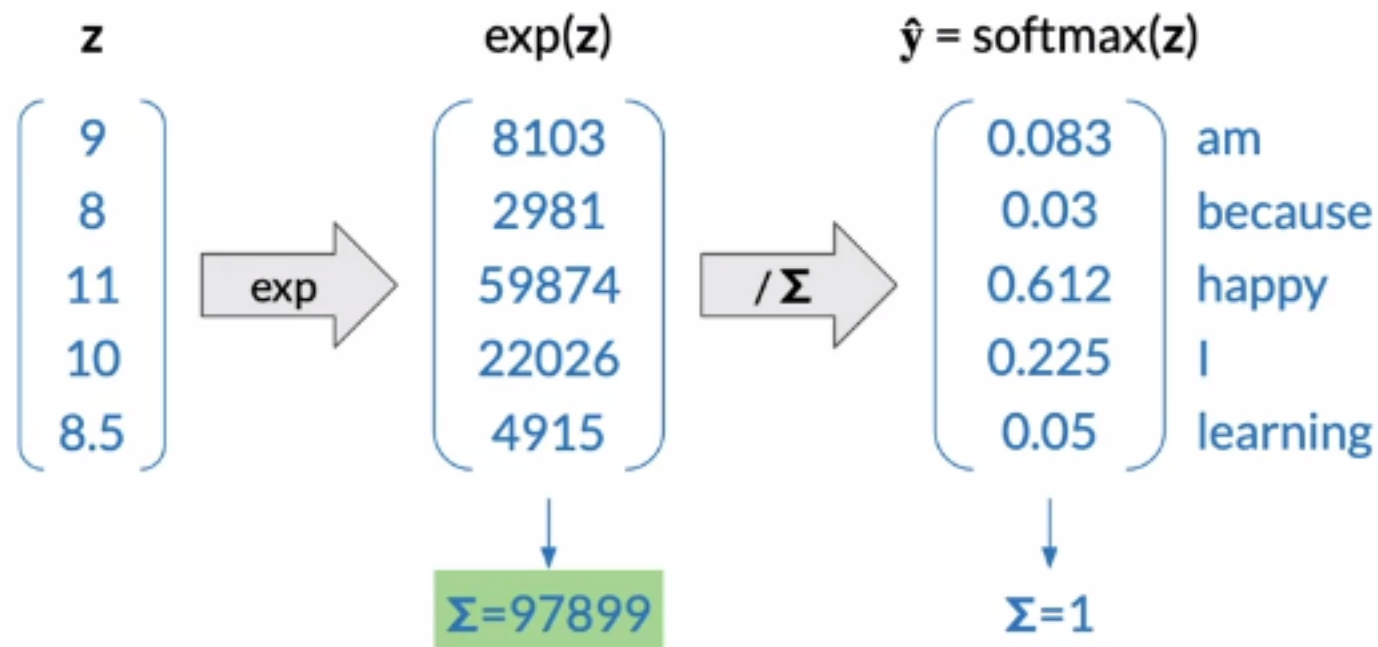
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



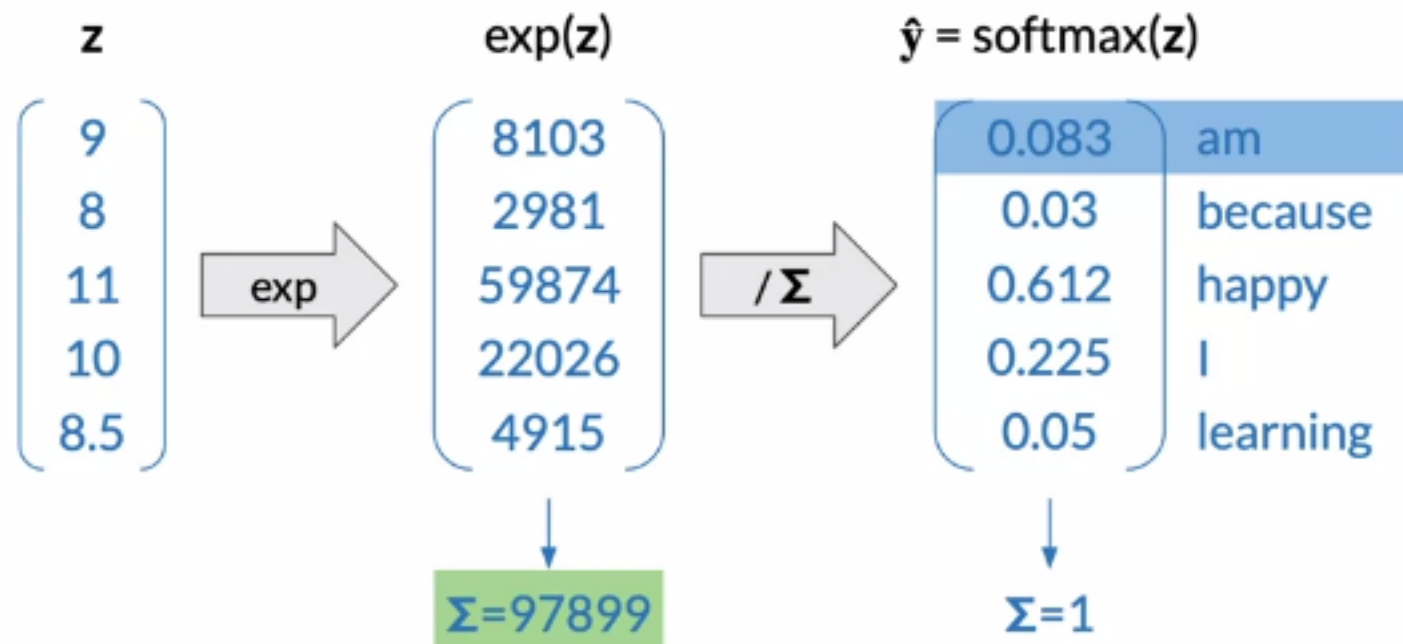
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



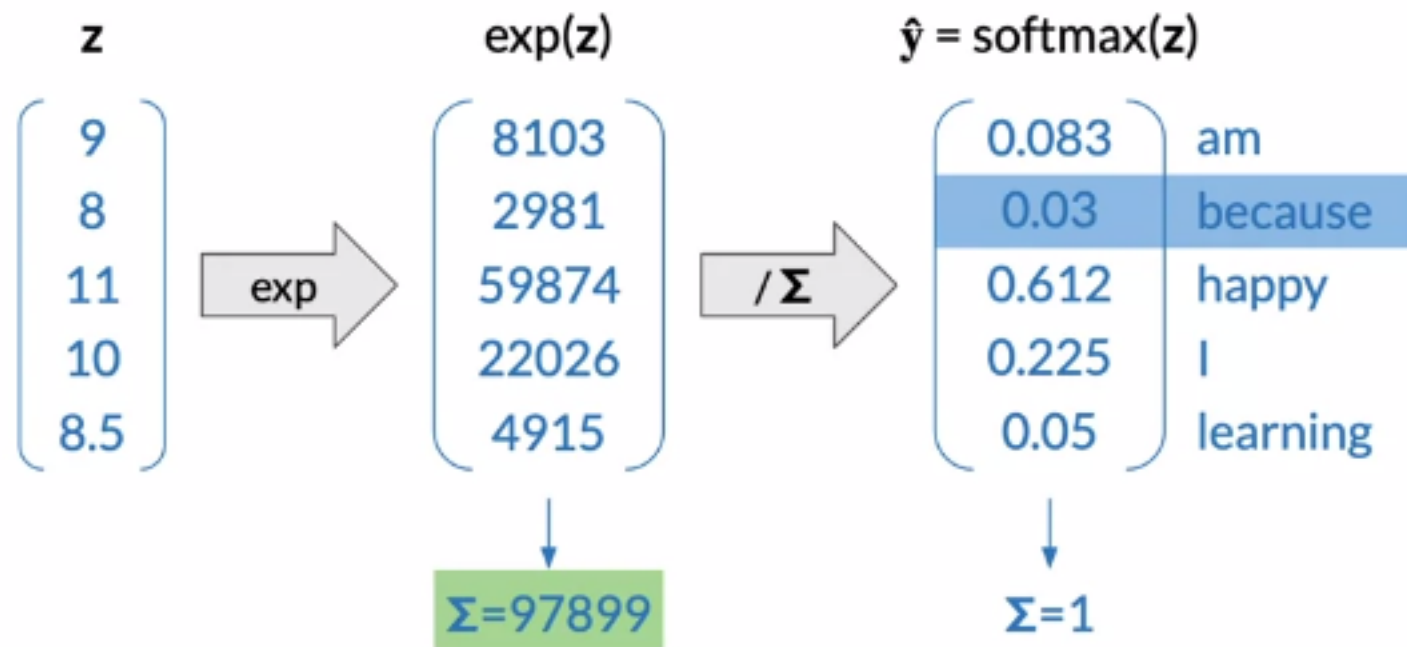
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



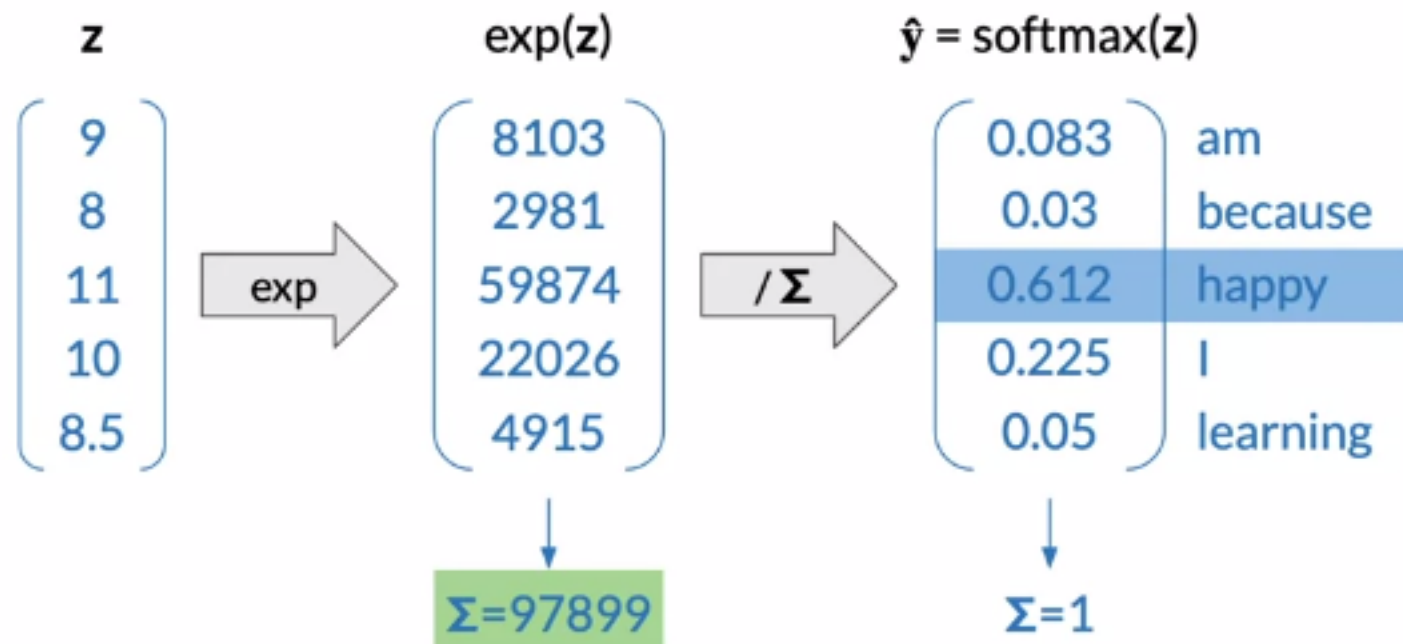
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example



$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

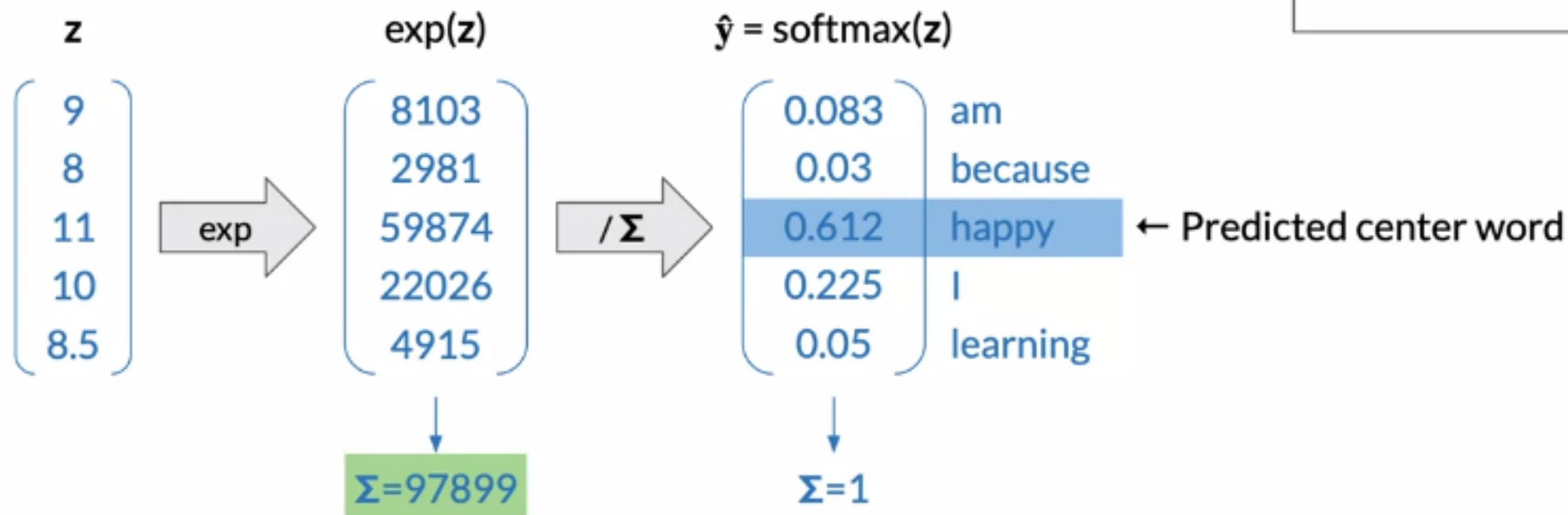
# Softmax: example



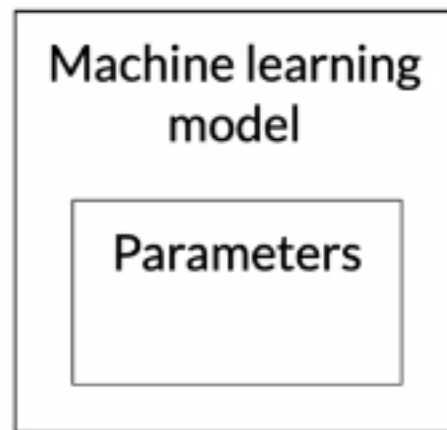
$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

# Softmax: example

$$\hat{y}_i = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

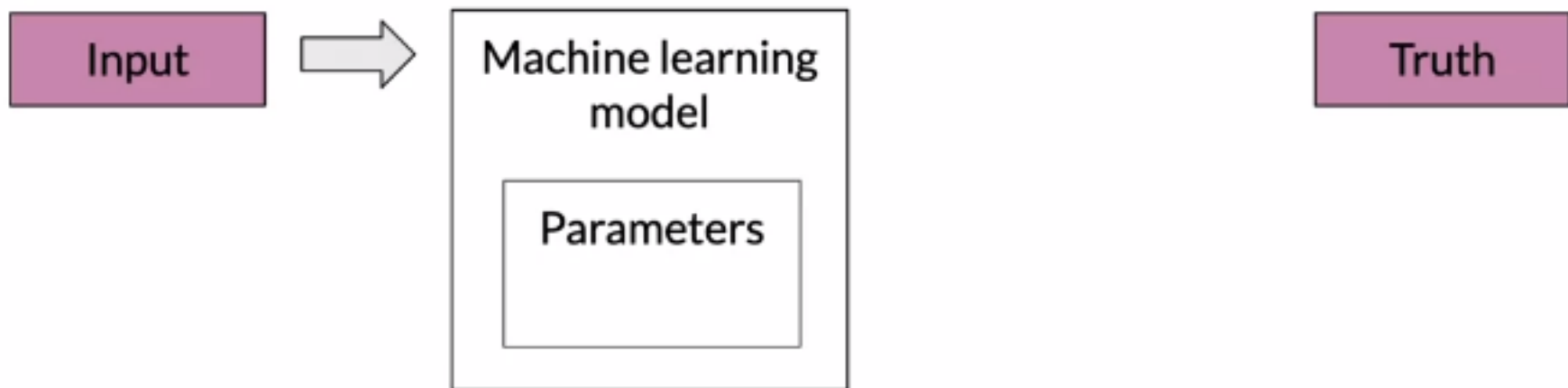


# Loss

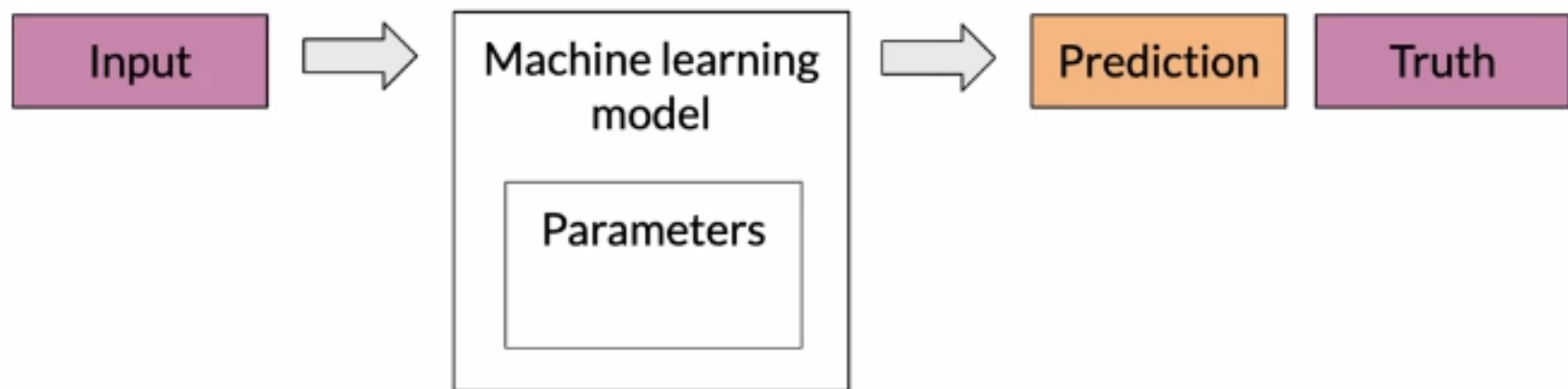




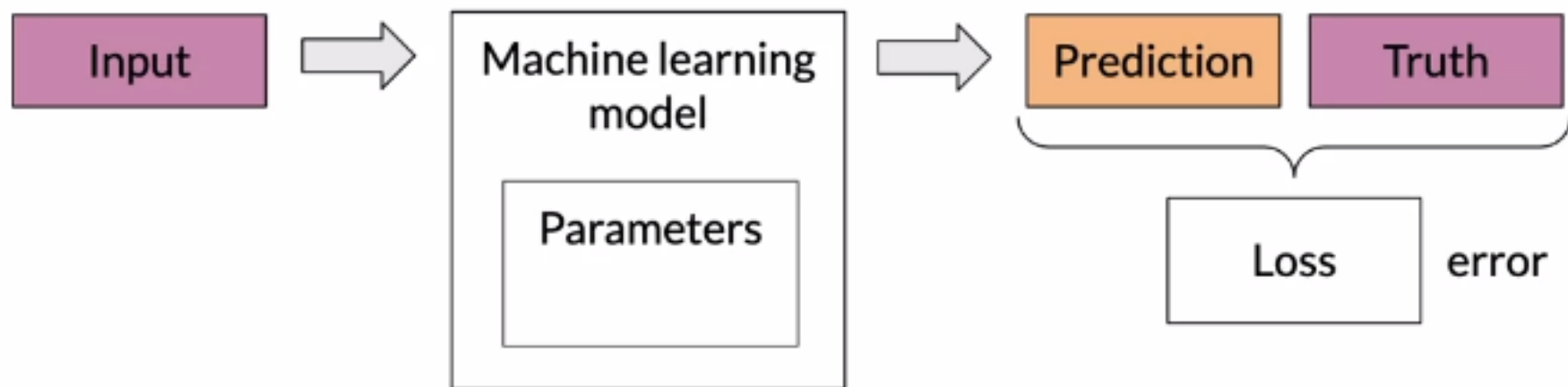
# Loss



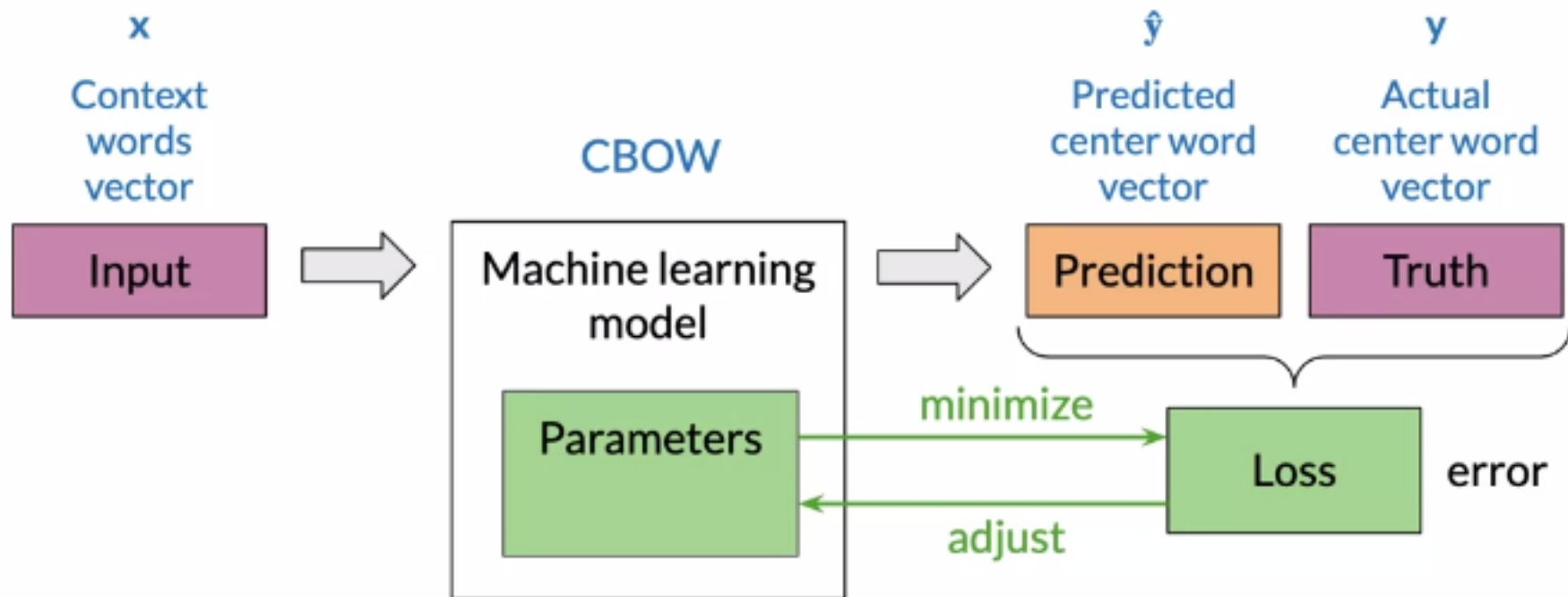
# Loss



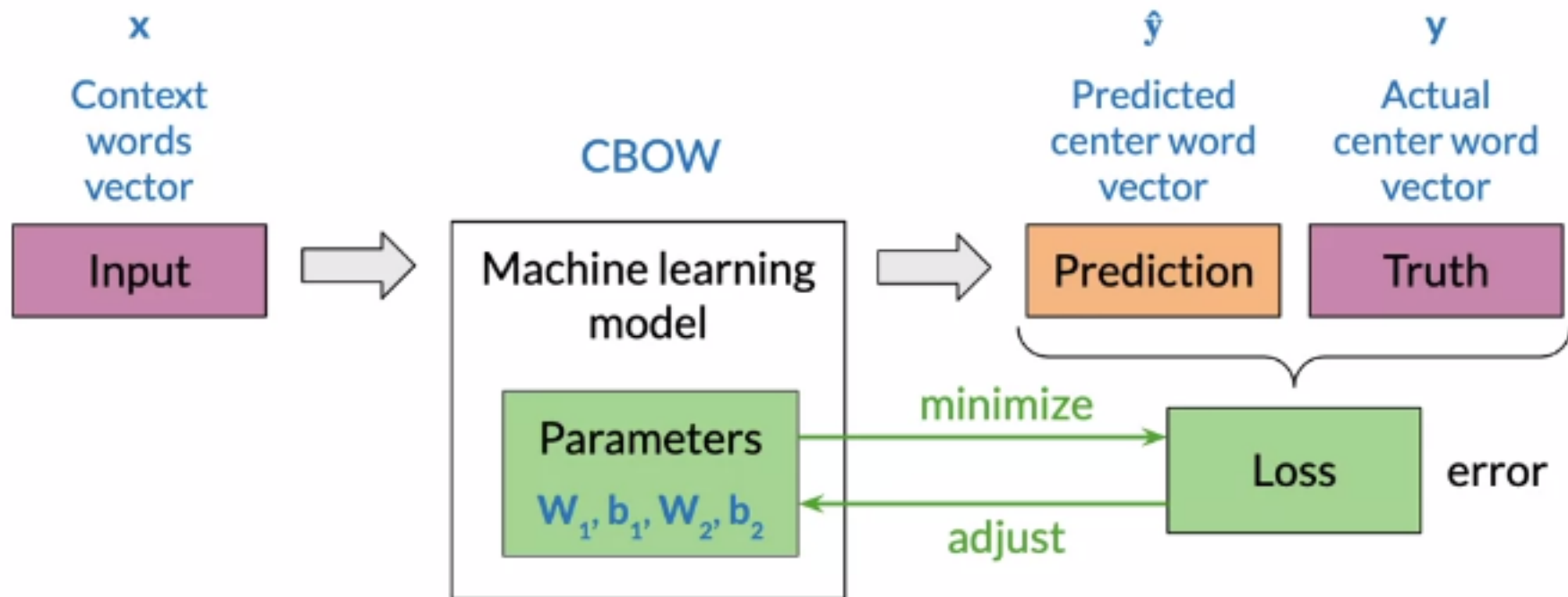
# Loss



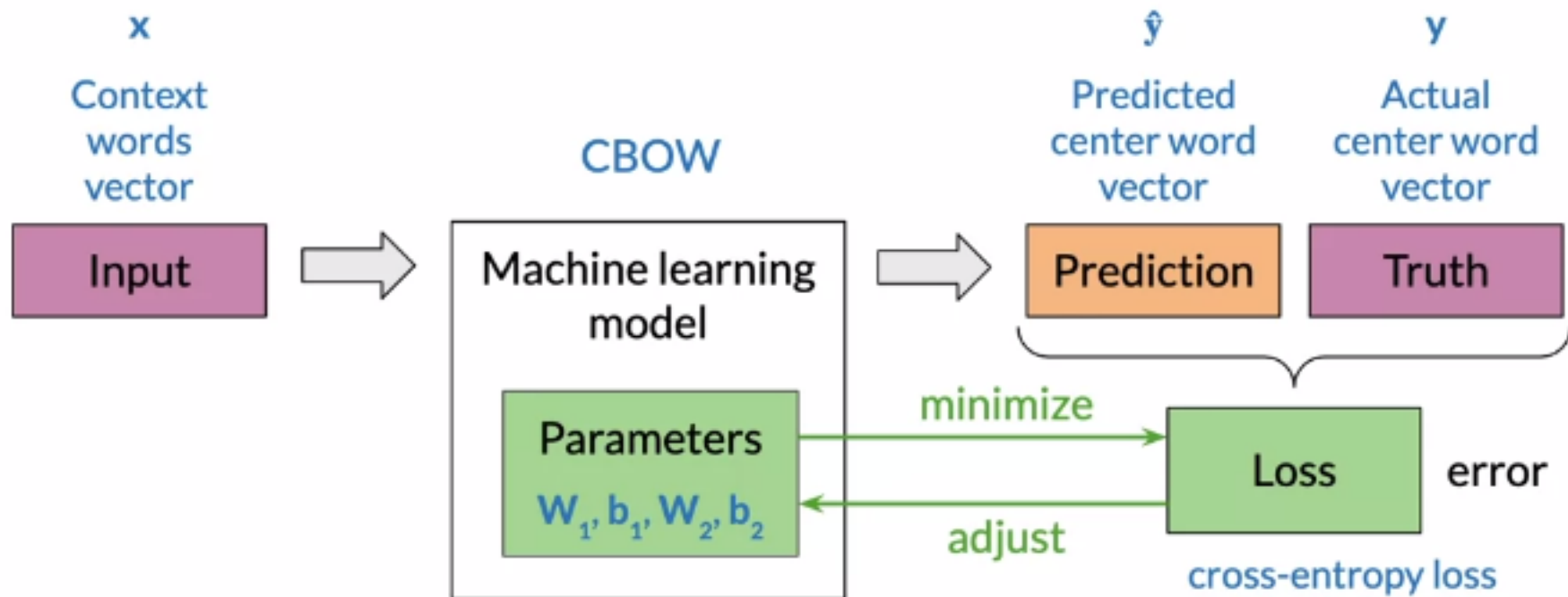
# Loss



# Loss



# Loss



# Cross-entropy loss

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_v \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_v \end{pmatrix}$

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual

$$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$$

Predicted

$$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$$



# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$

I am happy because I am learning

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$

I am happy because I am learning

$\mathbf{y}$

0	am
0	because
1	happy
0	I
0	learning

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$

I am happy because I am learning

$\mathbf{y}$		$\hat{\mathbf{y}}$
0	am	0.083
0	because	0.03
1	happy	0.611
0	I	0.225
0	learning	0.05

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$

I am happy because I am learning

$\mathbf{y}$		$\hat{\mathbf{y}}$
0	am	0.083
0	because	0.03
1	happy	0.611
0	I	0.225
0	learning	0.05

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_v \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_v \end{pmatrix}$

I am happy because I am learning

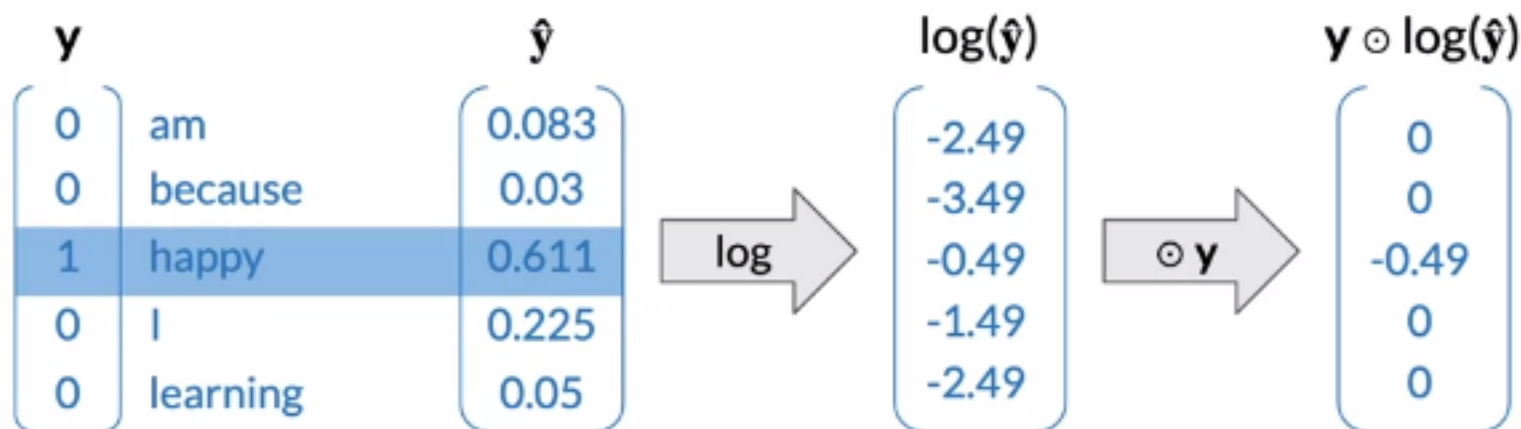
$\mathbf{y}$		$\hat{\mathbf{y}}$		$\log(\hat{\mathbf{y}})$
0	am	0.083		-2.49
0	because	0.03		-3.49
1	happy	0.611	log	-0.49
0	I	0.225		-1.49
0	learning	0.05		-2.49

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{pmatrix} y_1 \\ \vdots \\ y_V \end{pmatrix}$	$\hat{\mathbf{y}} = \begin{pmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{pmatrix}$

I am happy because I am learning



# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{bmatrix} y_1 \\ \vdots \\ y_V \end{bmatrix}$	$\hat{\mathbf{y}} = \begin{bmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{bmatrix}$

I am happy because I am learning

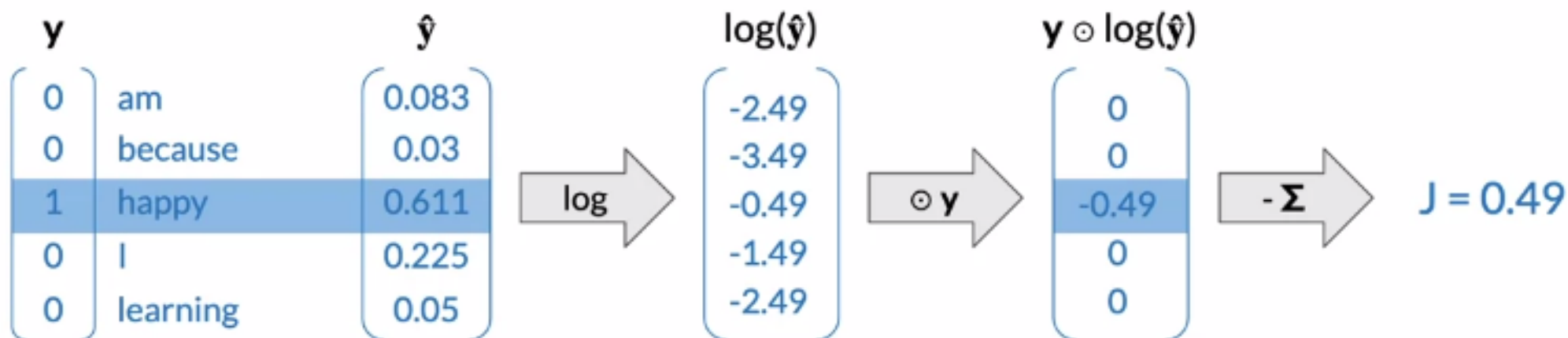
$\mathbf{y}$		$\hat{\mathbf{y}}$		$\log(\hat{\mathbf{y}})$		$\mathbf{y} \odot \log(\hat{\mathbf{y}})$
0	am	0.083		-2.49		0
0	because	0.03		-3.49		0
1	happy	0.611	log	-0.49	$\odot \mathbf{y}$	-0.49
0	I	0.225		-1.49		0
0	learning	0.05		-2.49		0

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Actual	Predicted
$\mathbf{y} = \begin{bmatrix} y_1 \\ \vdots \\ y_V \end{bmatrix}$	$\hat{\mathbf{y}} = \begin{bmatrix} \hat{y}_1 \\ \vdots \\ \hat{y}_V \end{bmatrix}$

I am happy because I am learning





# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

<b>y</b>	
0	am
0	because
1	happy
0	I
0	learning

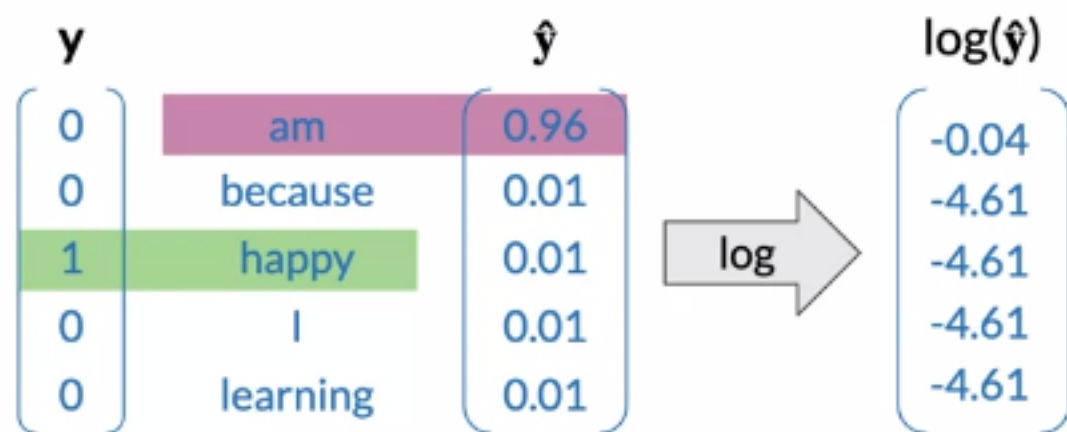
# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

$y$		$\hat{y}$
0	am	0.96
0	because	0.01
1	happy	0.01
0	I	0.01
0	learning	0.01

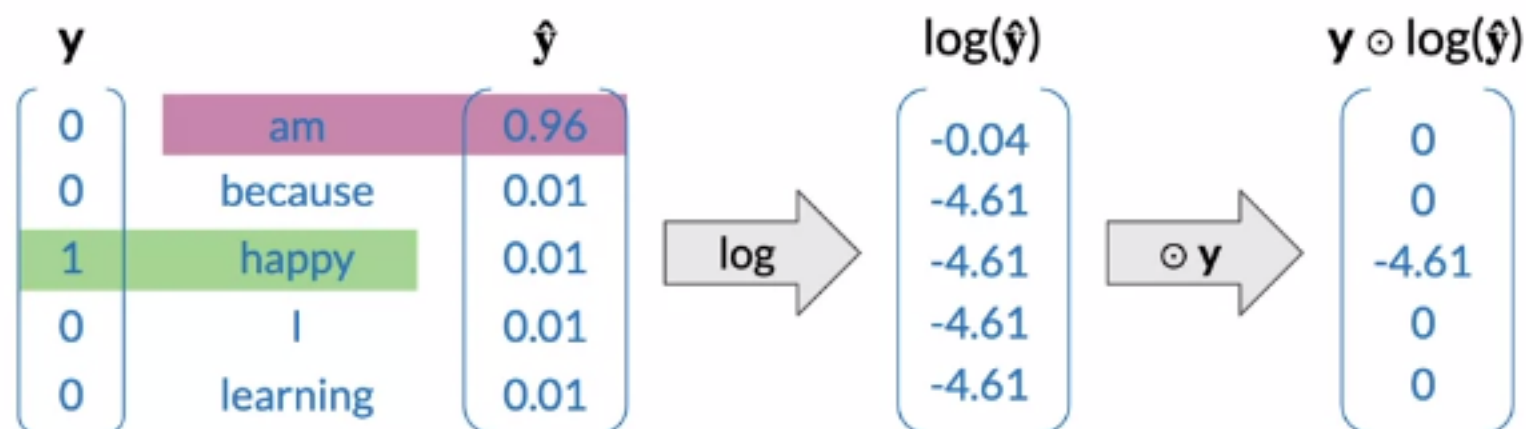
# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$



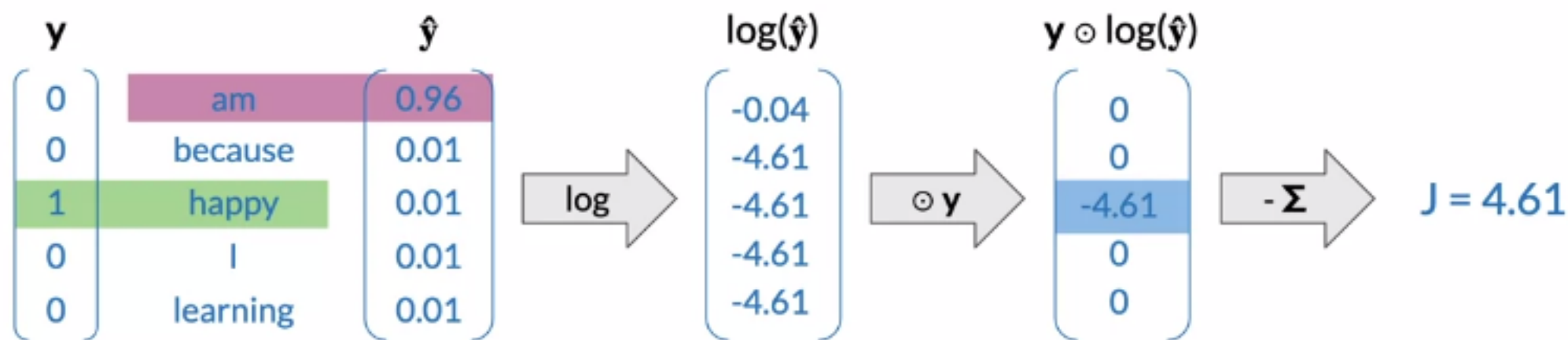
# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$



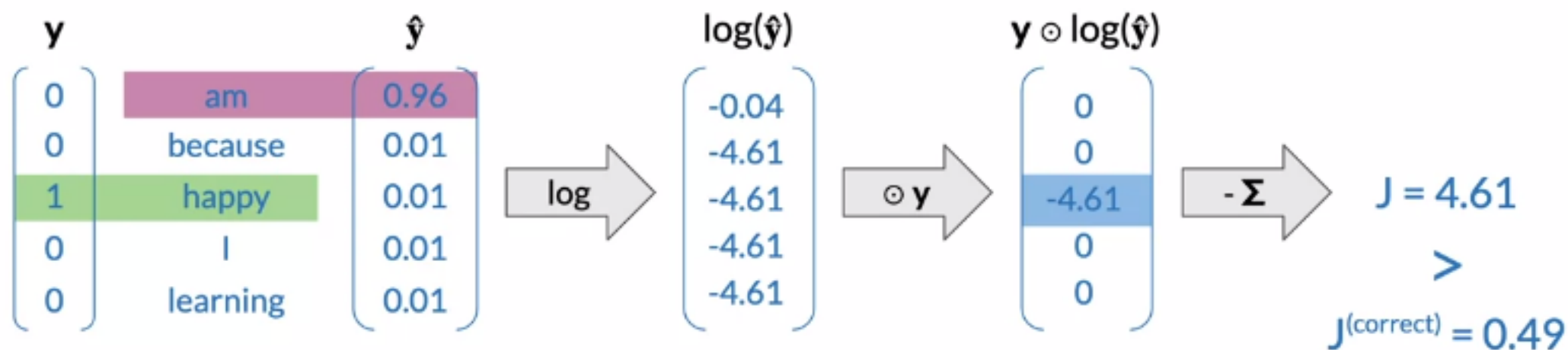
# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$



# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$



# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

$$J = -\log \hat{y}_{\text{actual word}}$$

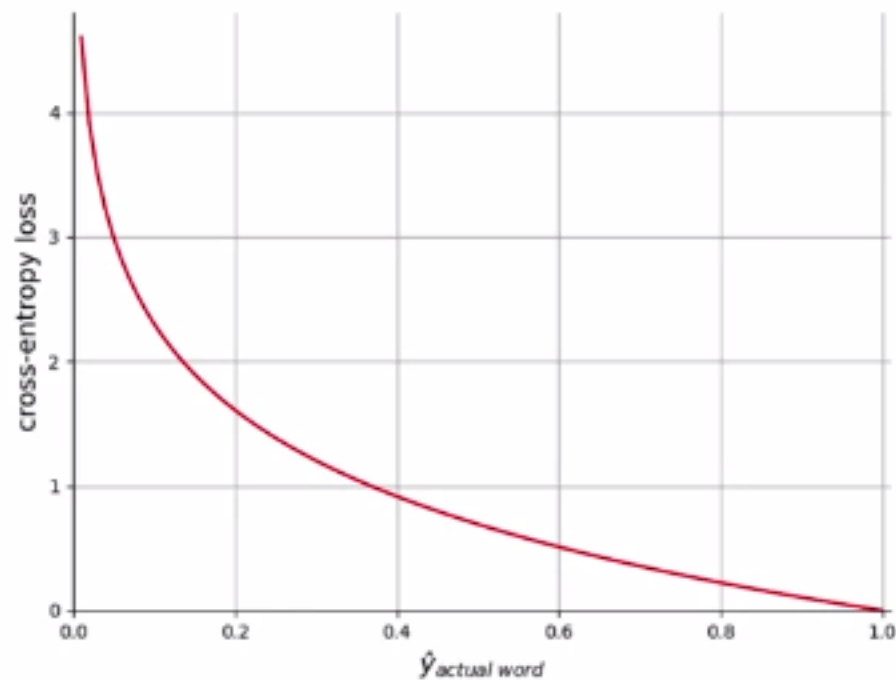
$y$		$\hat{y}$	
0	am	0.96	
0	because	0.01	
1	happy	0.01	$\rightarrow J = 4.61$
0	I	0.01	
0	learning	0.01	

# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

$$J = -\log \hat{y}_{\text{actual word}}$$

$y$		$\hat{y}$	
0	am	0.96	
0	because	0.01	
1	happy	0.01	$\rightarrow J = 4.61$
0	I	0.01	
0	learning	0.01	





# Cross-entropy loss

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

$$J = -\log \hat{y}_{\text{actual word}}$$

$y$		$\hat{y}$	
0	am	0.96	
0	because	0.01	
1	happy	0.01	$\rightarrow J = 4.61$
0	I	0.01	
0	learning	0.01	





deeplearning.ai

# Training a CBOW Model

---

Forward Propagation

# Training process

- Forward propagation

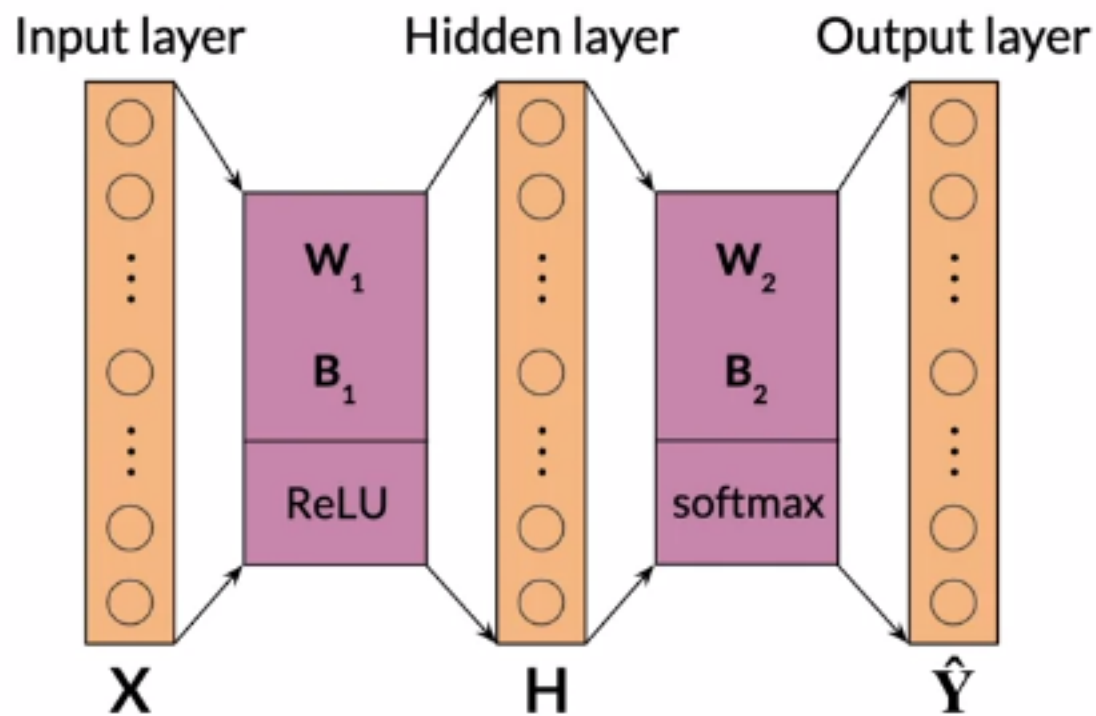
# Training process

- Forward propagation
- Cost

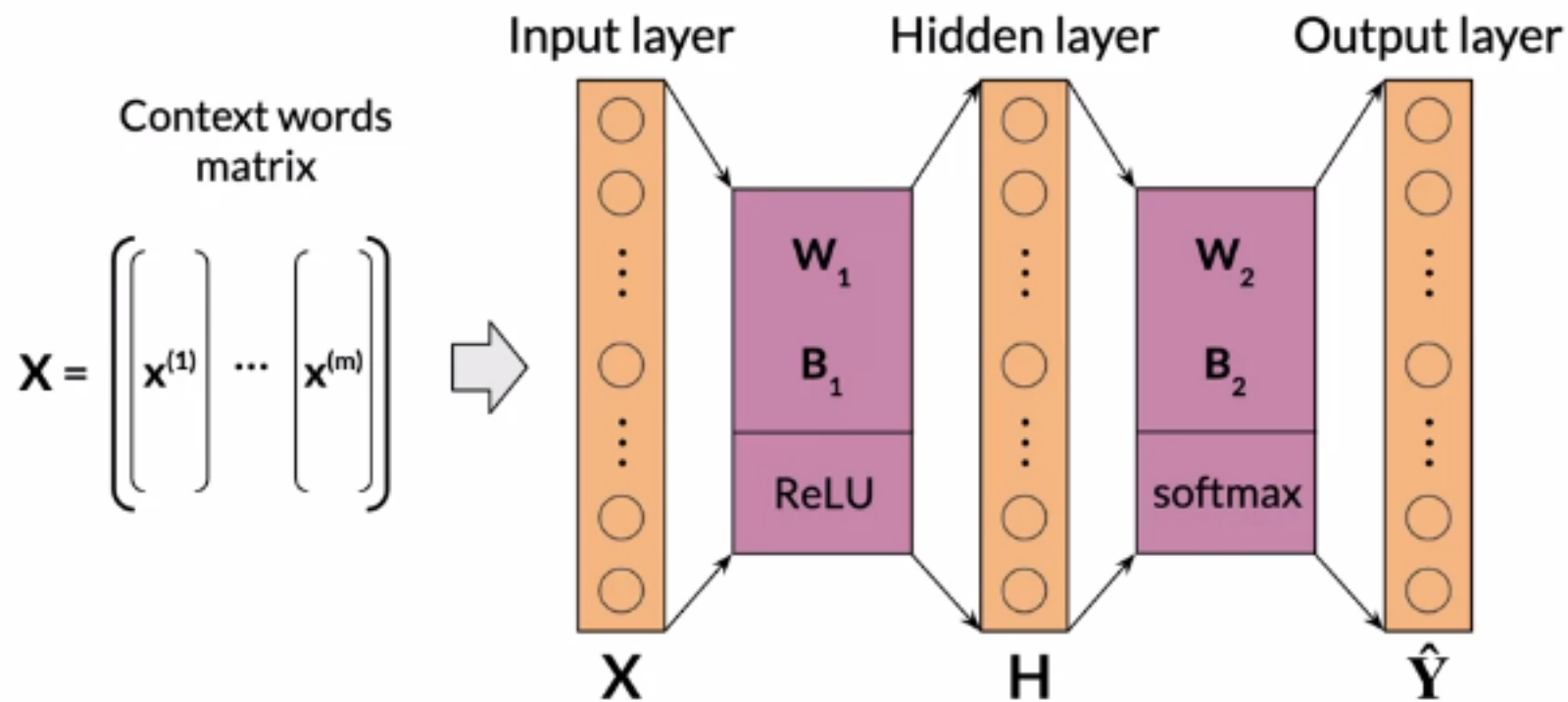
# Training process

- Forward propagation
- Cost
- Backpropagation and gradient descent

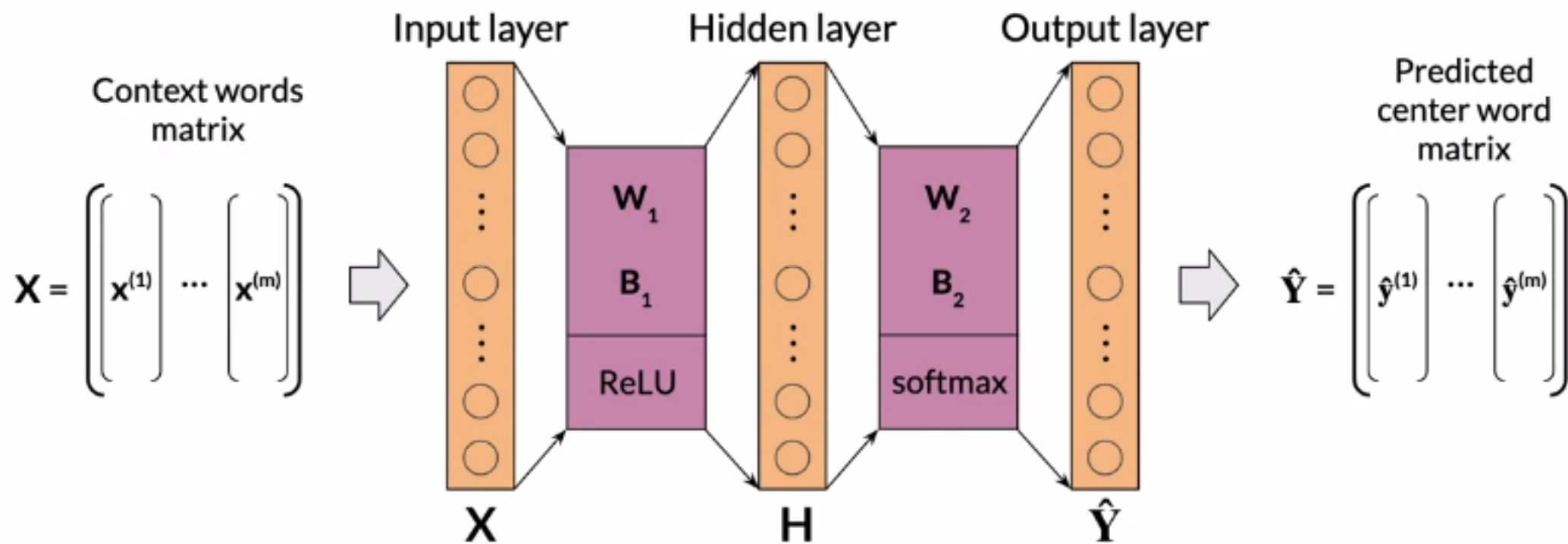
# Forward propagation



# Forward propagation

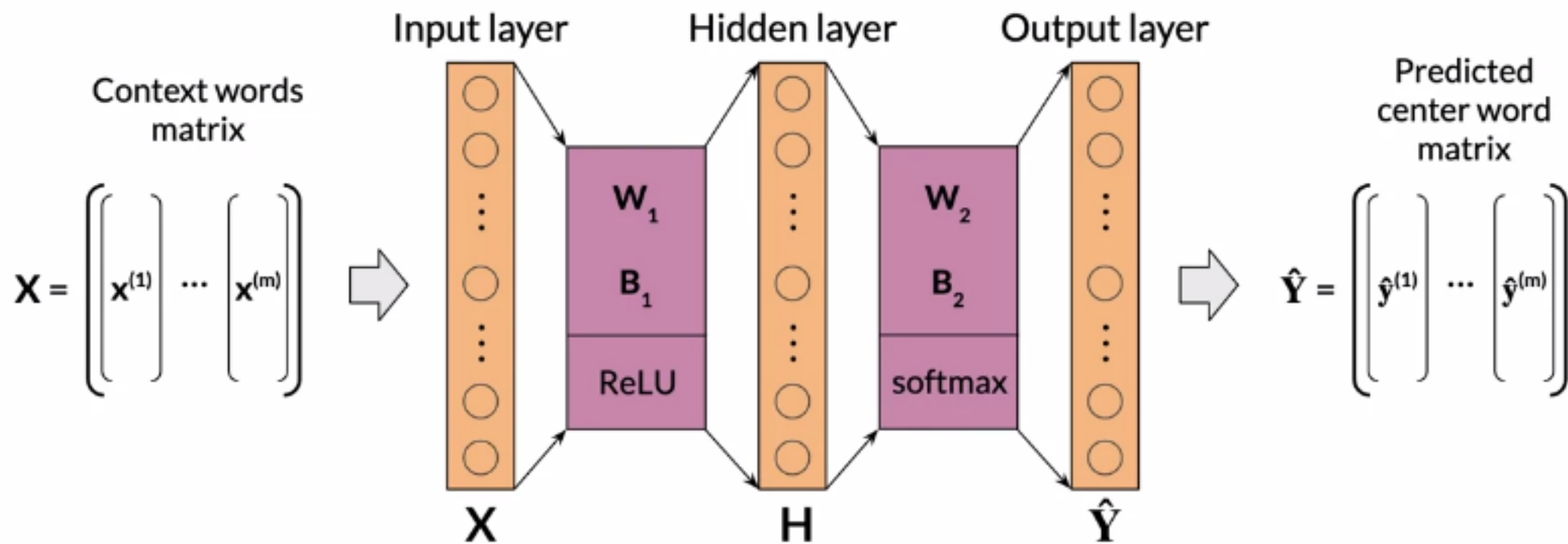


# Forward propagation





# Forward propagation



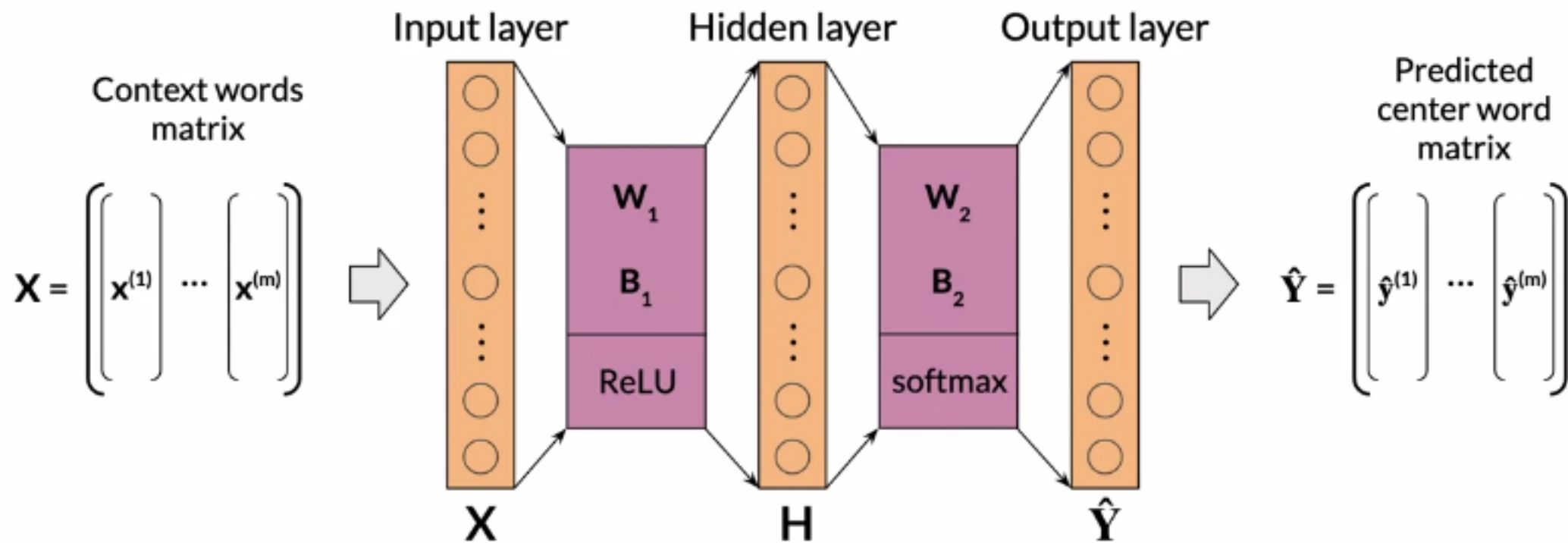
# Forward propagation

$$\mathbf{Z}_1 = \mathbf{W}_1 \mathbf{X} + \mathbf{B}_1$$

$$\mathbf{H} = \text{ReLU}(\mathbf{Z}_1)$$

$$\mathbf{Z}_2 = \mathbf{W}_2 \mathbf{H} + \mathbf{B}_2$$

$$\hat{\mathbf{Y}} = \text{softmax}(\mathbf{Z}_2)$$



# Cost

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

# Cost

Cost: mean of losses

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

# Cost

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Cost: mean of losses

$$J_{batch} = -\frac{1}{m} \sum_{i=1}^m \sum_{j=1}^V y_j^{(i)} \log \hat{y}_j^{(i)}$$

Predicted  
center word  
matrix

$$\hat{\mathbf{Y}} = \begin{pmatrix} \begin{pmatrix} \hat{\mathbf{y}}^{(1)} \end{pmatrix} & \dots & \begin{pmatrix} \hat{\mathbf{y}}^{(m)} \end{pmatrix} \end{pmatrix}$$

Actual center  
word matrix

$$\mathbf{Y} = \begin{pmatrix} \begin{pmatrix} \mathbf{y}^{(1)} \end{pmatrix} & \dots & \begin{pmatrix} \mathbf{y}^{(m)} \end{pmatrix} \end{pmatrix}$$

# Cost

$$J = - \sum_{k=1}^V y_k \log \hat{y}_k$$

Cost: mean of losses

$$J_{batch} = -\frac{1}{m} \sum_{i=1}^m \sum_{j=1}^V y_j^{(i)} \log \hat{y}_j^{(i)}$$

$$J_{batch} = -\frac{1}{m} \sum_{i=1}^m J^{(i)}$$

Predicted  
center word  
matrix

$$\hat{\mathbf{Y}} = \begin{bmatrix} \begin{bmatrix} \hat{\mathbf{y}}^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} \hat{\mathbf{y}}^{(m)} \end{bmatrix} \end{bmatrix}$$

Actual center  
word matrix

$$\mathbf{Y} = \begin{bmatrix} \begin{bmatrix} \mathbf{y}^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{y}^{(m)} \end{bmatrix} \end{bmatrix}$$

# Minimizing the cost

# Minimizing the cost

- Backpropagation: calculate partial derivatives of cost with respect to weights and biases

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1}, \frac{\partial J_{batch}}{\partial \mathbf{W}_2}, \frac{\partial J_{batch}}{\partial \mathbf{b}_1}, \frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$



## Minimizing the cost

$$J_{batch} = f(\mathbf{W}_1, \mathbf{W}_2, \mathbf{b}_1, \mathbf{b}_2)$$

- Backpropagation: calculate partial derivatives of cost with respect to weights and biases

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1}, \frac{\partial J_{batch}}{\partial \mathbf{W}_2}, \frac{\partial J_{batch}}{\partial \mathbf{b}_1}, \frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Minimizing the cost

- Backpropagation: calculate partial derivatives of cost with respect to weights and biases

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1}, \frac{\partial J_{batch}}{\partial \mathbf{W}_2}, \frac{\partial J_{batch}}{\partial \mathbf{b}_1}, \frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

- Gradient descent: update weights and biases

# Backpropagation

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{H}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1}$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{H}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{1}_m^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{H}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{1}_m^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

The diagram illustrates the calculation of the bias gradient term  $\mathbf{A} \cdot \mathbf{1}_m^\top$ . At the top, the vector  $\mathbf{1}_m$  is defined as  $\begin{bmatrix} 1, \dots, 1 \end{bmatrix}$  with a double-headed arrow below it indicating its size is  $m$ . Below this, the expression  $\mathbf{A} \cdot \mathbf{1}_m^\top$  is shown. The matrix  $\mathbf{A}$  is represented by a column vector with a green-outlined box for its top row. This is multiplied by the vector  $\mathbf{1}_m^\top = \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix}$ . A green arrow points from the top row of  $\mathbf{A}$  to the top element of the resulting vector  $\Sigma$ , which is highlighted in green. The final result is shown as a column vector  $\begin{bmatrix} \Sigma \\ \vdots \\ \end{bmatrix}$ .

$$\mathbf{A} \cdot \mathbf{1}_m^\top = \begin{bmatrix} \boxed{\phantom{0}} \\ \vdots \\ \end{bmatrix} \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix} = \begin{bmatrix} \Sigma \\ \vdots \\ \end{bmatrix}$$



# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{H}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{1}_m^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

$$\mathbf{1}_m = \left[ 1, \dots, 1 \right]$$

$\longleftrightarrow$   
 $m$

$$\mathbf{A} \cdot \mathbf{1}_m^\top = \left[ \boxed{\phantom{000000}} \right] \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix} = \begin{bmatrix} \Sigma \\ \phantom{000000} \end{bmatrix}$$

```
import numpy as np
# code to initialize matrix a omitted
np.sum(a, axis=1, keepdims=True)
```

# Backpropagation

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{X}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{W}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{H}^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_1} = \frac{1}{m} \text{ReLU} \left( \mathbf{W}_2^\top (\hat{\mathbf{Y}} - \mathbf{Y}) \right) \mathbf{1}_m^\top$$

$$\frac{\partial J_{batch}}{\partial \mathbf{b}_2} = \frac{1}{m} (\hat{\mathbf{Y}} - \mathbf{Y}) \mathbf{1}_m^\top$$

$$\mathbf{1}_m = \left[ \underset{\substack{\longleftrightarrow \\ m}}{1, \dots, 1} \right]$$

$$\mathbf{A} \cdot \mathbf{1}_m^\top = \begin{bmatrix} \boxed{\phantom{000}} \end{bmatrix} \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix} = \begin{bmatrix} \boxed{\Sigma} \end{bmatrix}$$

```
import numpy as np
# code to initialize matrix a omitted
np.sum(a, axis=1, keepdims=True)
```

# Gradient descent

Hyperparameter: learning rate  $\alpha$

$$\mathbf{W}_1 := \mathbf{W}_1 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{W}_1}$$

$$\mathbf{W}_2 := \mathbf{W}_2 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{W}_2}$$

$$\mathbf{b}_1 := \mathbf{b}_1 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{b}_1}$$

$$\mathbf{b}_2 := \mathbf{b}_2 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

# Gradient descent

Hyperparameter: learning rate  $\alpha$

$$\mathbf{W}_1 := \mathbf{W}_1 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{W}_1}$$

$$\mathbf{W}_2 := \mathbf{W}_2 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{W}_2}$$

$$\mathbf{b}_1 := \mathbf{b}_1 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{b}_1}$$

$$\mathbf{b}_2 := \mathbf{b}_2 - \alpha \frac{\partial J_{batch}}{\partial \mathbf{b}_2}$$

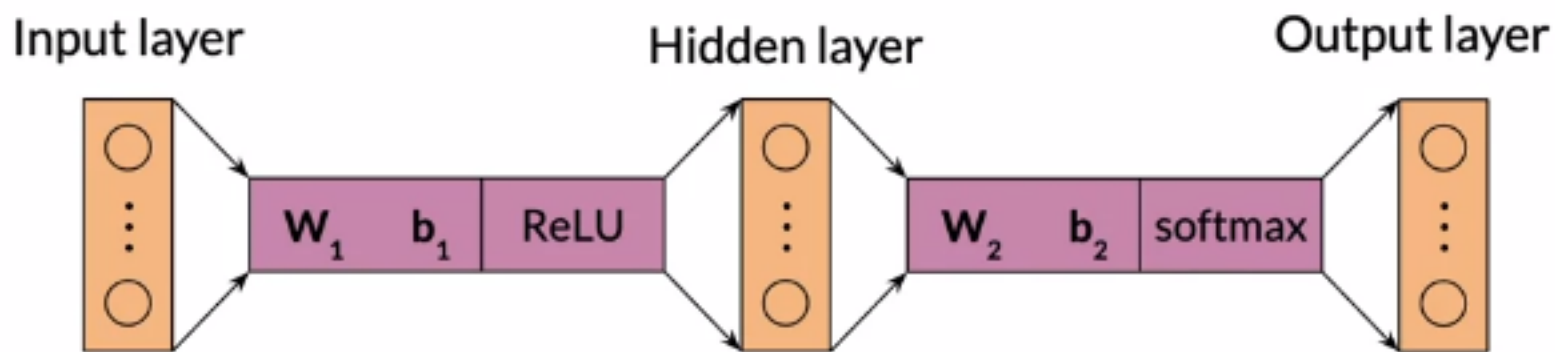


deeplearning.ai

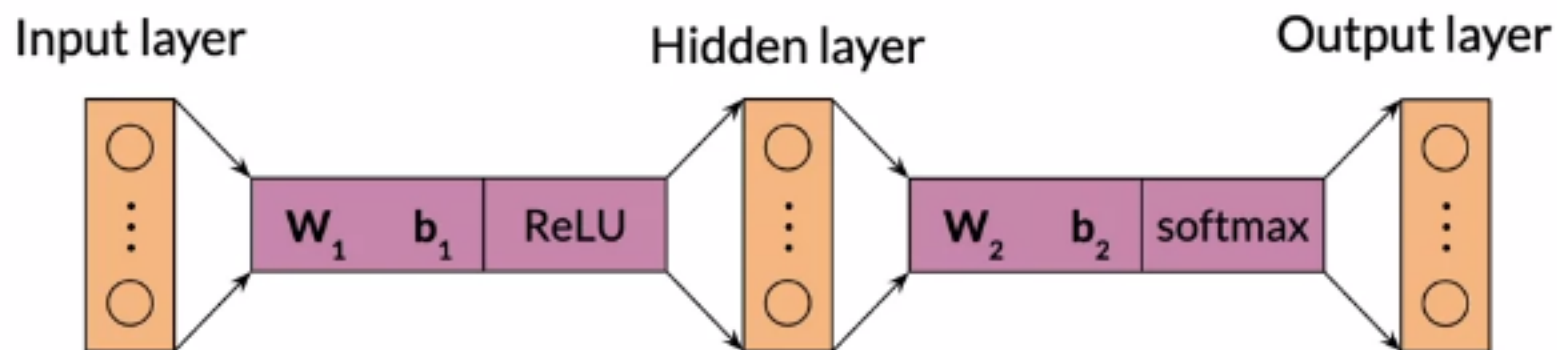
# Extracting Word Embedding Vectors

---

# Extracting word embedding vectors: option 1



# Extracting word embedding vectors: option 1

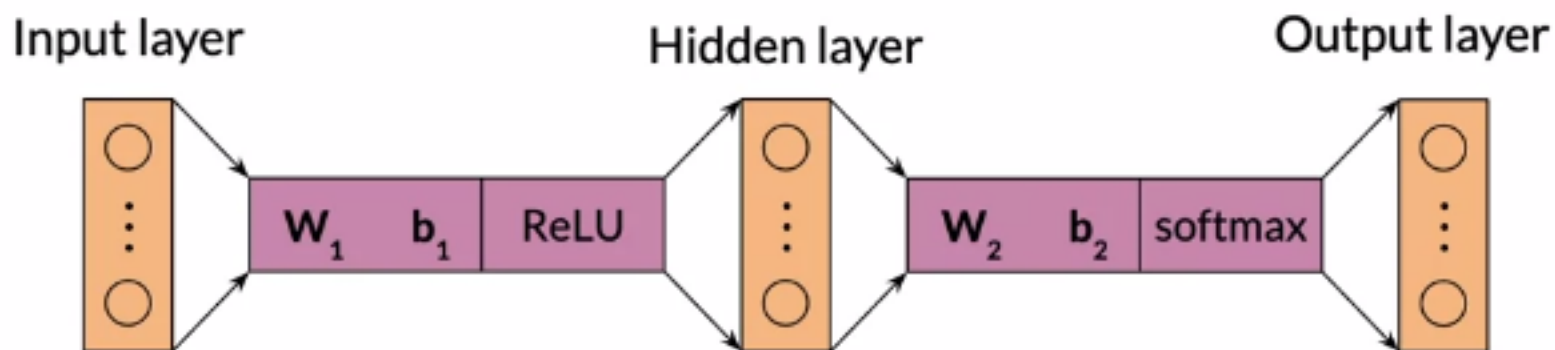


$$W_1 = \begin{bmatrix} \begin{bmatrix} w^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} w^{(V)} \end{bmatrix} \end{bmatrix}$$

$\xleftrightarrow{V}$

$\updownarrow N$

# Extracting word embedding vectors: option 1

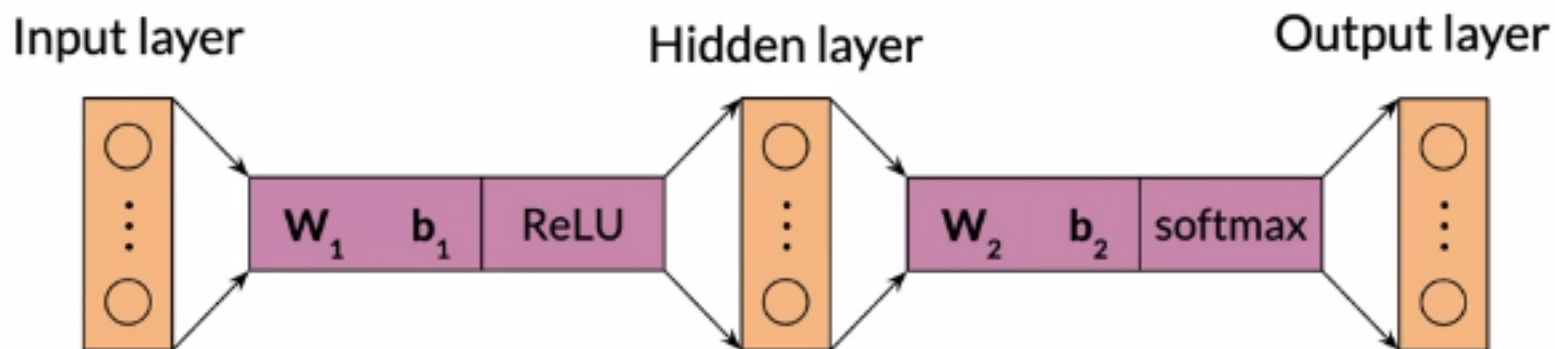


$$W_1 = \begin{bmatrix} \begin{bmatrix} w^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} w^{(V)} \end{bmatrix} \end{bmatrix} \begin{matrix} \updownarrow N \\ \leftarrow V \end{matrix}$$

$$x = \begin{bmatrix} \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{bmatrix} \begin{matrix} \updownarrow V \end{matrix}$$



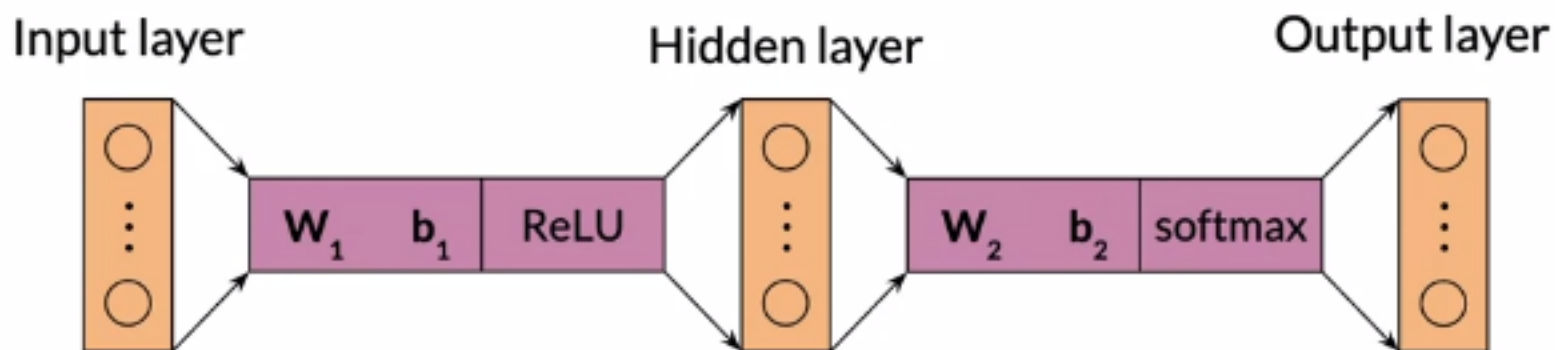
# Extracting word embedding vectors: option 1



$$W_1 = \begin{bmatrix} \text{am} \\ \boxed{w^{(1)}} & \dots & \boxed{w^{(V)}} \end{bmatrix} \begin{matrix} \updownarrow N \\ \leftarrow V \end{matrix}$$

$$x = \begin{bmatrix} \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{bmatrix} \begin{matrix} \updownarrow V \end{matrix}$$

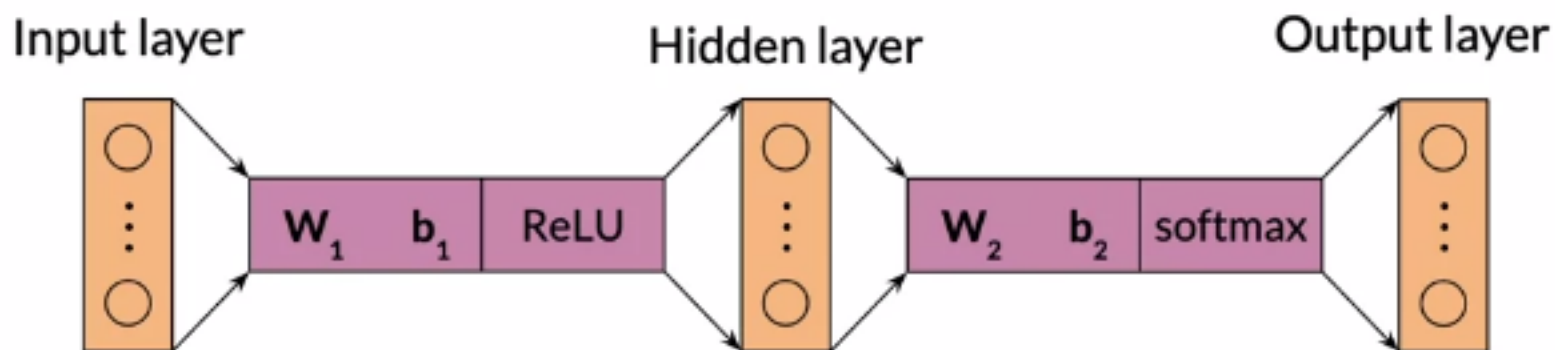
## Extracting word embedding vectors: option 2



$$W_2 = \begin{bmatrix} \begin{bmatrix} w^{(1)} \end{bmatrix} \\ \vdots \\ \begin{bmatrix} w^{(N)} \end{bmatrix} \end{bmatrix}$$

$\xleftrightarrow{N}$        $\xleftrightarrow{V}$

## Extracting word embedding vectors: option 2



$$W_2 = \begin{bmatrix} \begin{bmatrix} w^{(1)} \end{bmatrix} \\ \vdots \\ \begin{bmatrix} w^{(N)} \end{bmatrix} \end{bmatrix} \begin{matrix} \updownarrow V \\ \leftarrow N \end{matrix}$$

$$x = \begin{bmatrix} \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{bmatrix} \begin{matrix} \updownarrow V \end{matrix}$$

## Extracting word embedding vectors: option 3

$$\mathbf{W}_1 = \begin{bmatrix} \begin{bmatrix} \mathbf{w}_1^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{w}_1^{(M)} \end{bmatrix} \end{bmatrix} \quad \mathbf{W}_2 = \begin{bmatrix} \begin{bmatrix} \mathbf{w}_2^{(1)} \end{bmatrix} \\ \dots \\ \begin{bmatrix} \mathbf{w}_2^{(M)} \end{bmatrix} \end{bmatrix}$$

## Extracting word embedding vectors: option 3

$$\mathbf{W}_1 = \begin{bmatrix} \begin{bmatrix} \mathbf{w}_1^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{w}_1^{(M)} \end{bmatrix} \end{bmatrix} \quad \mathbf{W}_2 = \begin{bmatrix} \begin{bmatrix} \mathbf{w}_2^{(1)} \end{bmatrix} \\ \dots \\ \begin{bmatrix} \mathbf{w}_2^{(M)} \end{bmatrix} \end{bmatrix}$$

$\swarrow$

$$\mathbf{W}_3 = 0.5 (\mathbf{W}_1 + \mathbf{W}_2^T) = \begin{bmatrix} \begin{bmatrix} \mathbf{w}_3^{(1)} \end{bmatrix} & \dots & \begin{bmatrix} \mathbf{w}_3^{(M)} \end{bmatrix} \end{bmatrix}$$

$\underbrace{\hspace{10em}}_V \quad \underbrace{\hspace{1em}}_N$

## Extracting word embedding vectors: option 3

$$\mathbf{W}_1 = \begin{bmatrix} \mathbf{w}_1^{(1)} & \dots & \mathbf{w}_1^{(M)} \end{bmatrix} \quad \mathbf{W}_2 = \begin{bmatrix} \mathbf{w}_2^{(1)} \\ \dots \\ \mathbf{w}_2^{(M)} \end{bmatrix}$$

$$\mathbf{W}_3 = 0.5 (\mathbf{W}_1 + \mathbf{W}_2^T) = \begin{bmatrix} \mathbf{w}_3^{(1)} & \dots & \mathbf{w}_3^{(M)} \end{bmatrix}$$

$\underbrace{\hspace{10em}}_V \quad \quad \quad \underbrace{\hspace{1em}}_N$

$$\mathbf{x} = \begin{bmatrix} \text{am} \\ \text{because} \\ \text{happy} \\ \text{I} \\ \text{learning} \end{bmatrix}$$

$\updownarrow V$

# Intrinsic evaluation

# Intrinsic evaluation

Test relationships between words



# Intrinsic evaluation

Test relationships between words

- Analogies

# Intrinsic evaluation

Test relationships between words

- Analogies

Semantic analogies

# Intrinsic evaluation

Test relationships between words

- Analogies

Semantic analogies

“France” is to “Paris” as “Italy” is to <?>

Syntactic analogies

# Intrinsic evaluation

Test relationships between words

- Analogies

Semantic analogies

“France” is to “Paris” as “Italy” is to <?>

Syntactic analogies

“seen” is to “saw” as “been” is to <?>

# Intrinsic evaluation

Test relationships between words

- Analogies

Semantic analogies

“France” is to “Paris” as “Italy” is to <?>

Syntactic analogies

“seen” is to “saw” as “been” is to <?>

⚡ Ambiguity

# Intrinsic evaluation

Test relationships between words

- Analogies

Semantic analogies

“France” is to “Paris” as “Italy” is to <?>

Syntactic analogies

“seen” is to “saw” as “been” is to <?>

⚡ Ambiguity

“wolf” is to “pack” as “bee” is to <?> → swarm? colony?

# Intrinsic evaluation

## Test relationships between words

- Analogies

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

# Intrinsic evaluation

## Test relationships between words

- Analogies

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza



# Intrinsic evaluation

Test relationships between words

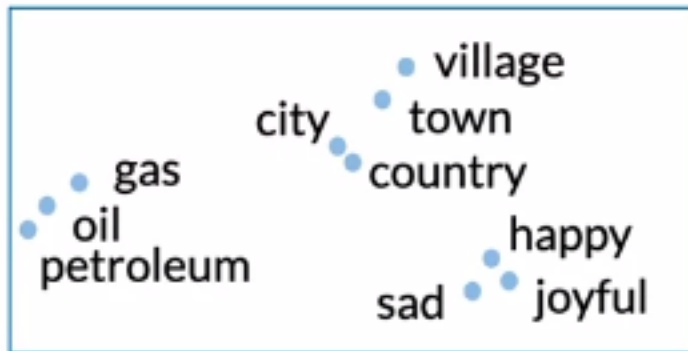
- Analogies
- Clustering



# Intrinsic evaluation

Test relationships between words

- Analogies
- Clustering
- Visualization





deeplearning.ai

# Evaluating Word Embeddings

---

Extrinsic Evaluation

# Extrinsic evaluation

Test word embeddings on external task

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

Named entity

[Andrew works at deeplearning.ai](#)

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

Named entity

Andrew works at deeplearning.ai

*person*



# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

Named entity

Andrew works at deeplearning.ai

*person*

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

Named entity

Andrew works at deeplearning.ai

*person*

*organization*

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

- + Evaluates actual usefulness of embeddings

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

- + Evaluates actual usefulness of embeddings
- Time-consuming

# Extrinsic evaluation

Test word embeddings on external task

e.g. named entity recognition, parts-of-speech tagging

- + Evaluates actual usefulness of embeddings
- Time-consuming
- More difficult to troubleshoot



deeplearning.ai

# Conclusion

---

# Recap and assignment

# Recap and assignment

- Data preparation
- Word representations



# Recap and assignment

- Data preparation
- Word representations
- Continuous bag-of-words model

# Recap and assignment

- Data preparation
- Word representations
- Continuous bag-of-words model
- Evaluation

## Going further

- Advanced language modelling and word embeddings

## Going further

- Advanced language modelling and word embeddings
- NLP and machine learning libraries

# Going further

- Advanced language modelling and word embeddings
- NLP and machine learning libraries

Keras

```
# from keras.layers.embeddings import Embedding  
embed_layer = Embedding(10000, 400)
```

PyTorch

```
# import torch.nn as nn  
embed_layer = nn.Embedding(10000, 400)
```